

Bank Credit Cycles*

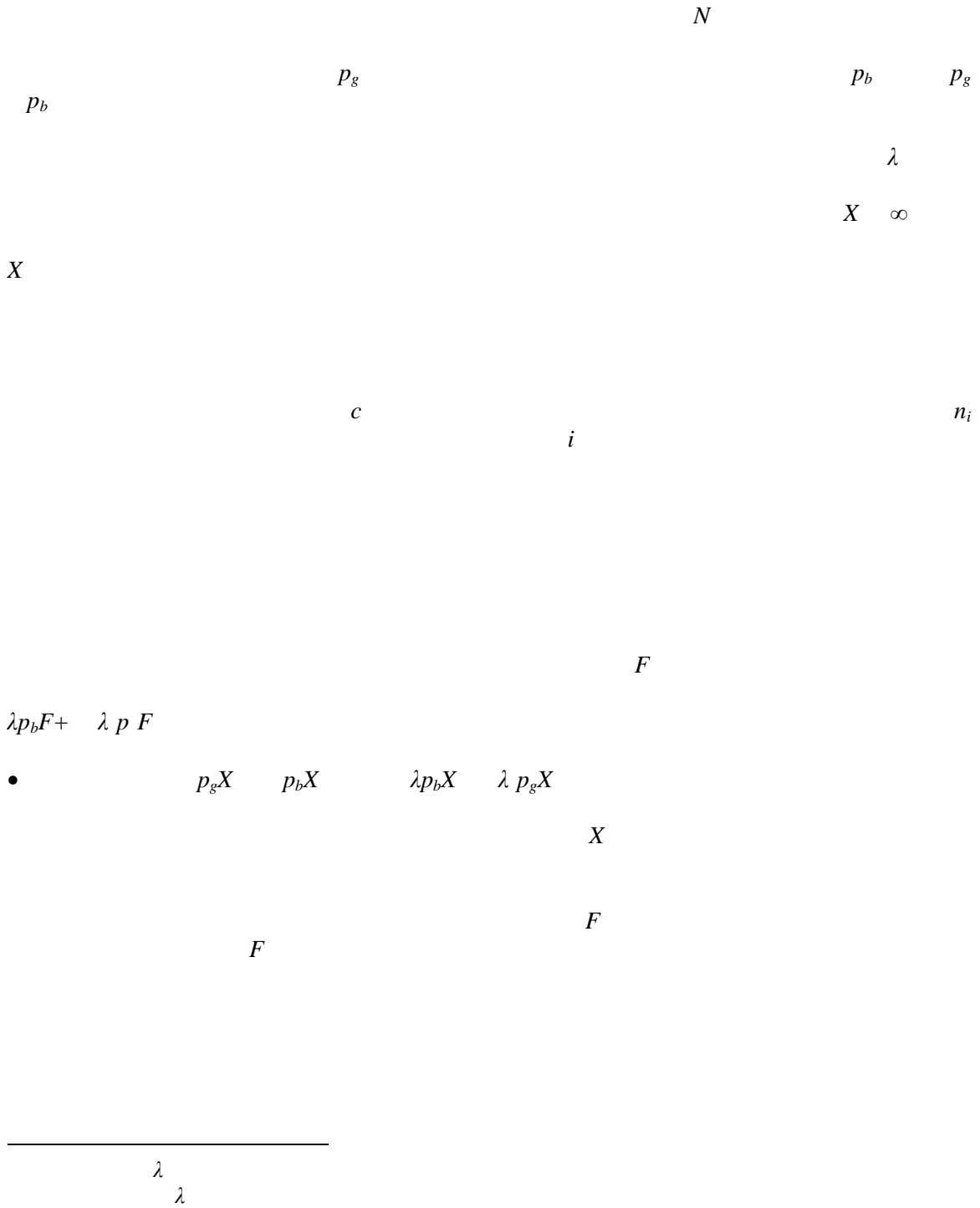
Abstract

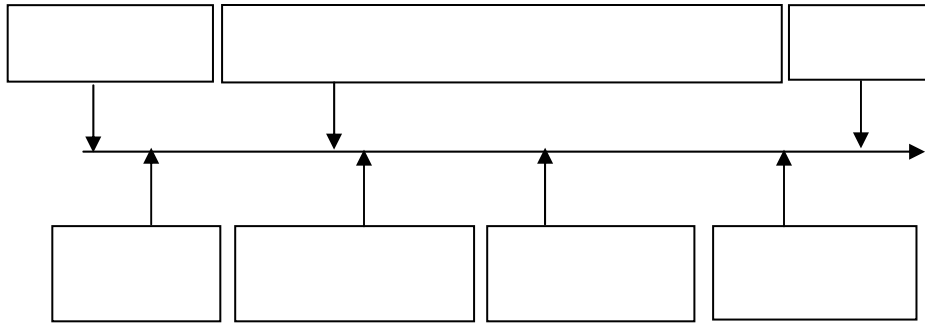
1. Introduction

PDI

PDI

2. The Lending Market Game





2.1 Stage Nash Equilibrium

Proposition 1 *If and only if $c \geq \frac{\lambda - \lambda p_g - p_b}{\lambda p_b + -\lambda p_g}$, does there exist a symmetric Nash equilibrium in which no bank conducts credit worthiness testing and both banks earn zero profits.*

$$c \geq \frac{\lambda - \lambda p_g - p_b}{\lambda p_b + -\lambda p_g}$$

- $c \geq \frac{\lambda - \lambda p_g - p_b}{\lambda p_b + -\lambda p_g}$.

Proposition 2 *There is no symmetric Nash equilibrium in which both banks test at least some of the applicants.*

$$\pi = \lambda p_b F + (1 - \lambda) p_g F - c$$

$F \quad X$

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$F \quad X$

2.2 Repeated Competition

$F \quad X$

$F \quad X$

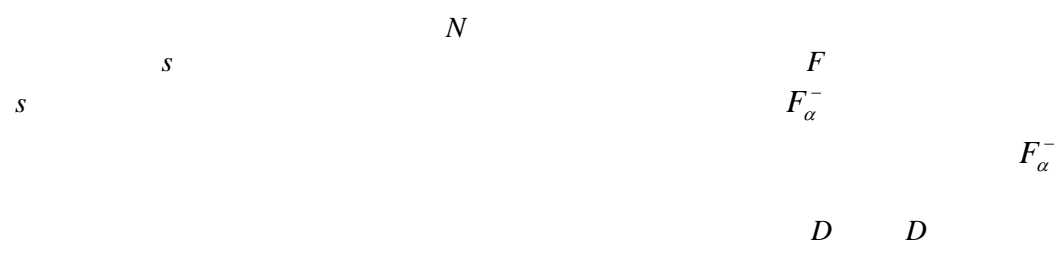
$$\pi = \lambda p_b F + (1 - \lambda) p_g F - c$$

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$\pi \quad \pi$

$$u - u = u - u$$

$$u + u + u = u$$



$$q = \lambda - p_b + -\lambda - p_g$$

s

$$q = \lambda - p_b + -\lambda \lambda - p_b + -\lambda - p_g$$

$$\Delta q = q - q = \lambda - \lambda p_g - p_b <$$

$D \quad D$

$$q_r = \lambda - p_b + -\lambda - p_g \lambda p_b + -\lambda p_g < q$$

s

$$q_r = \lambda - p_b \lambda p_b + -\lambda p_g + -\lambda \lambda - p_b + -\lambda - p_g p_g$$

$$\Delta q_r = q_r - q_r = \lambda - \lambda p_g - p_b = \Delta q$$

$q \quad q \quad q \quad q$

$n \quad N$

$$\theta \equiv \frac{\frac{n}{N} \lambda + \frac{n}{N} - \lambda}{\frac{n}{N} \lambda + \frac{n}{N} -}$$

$n \quad N \theta$

3. Empirical Tests

RV

TL

LL CO-RV LS

LR LS TL

UMP

DPI

FFR

3.1.2 Pairwise Tests of Rival Banks

$$y_{it} = \alpha_{ij}x_{it} + \beta_{ij}z_{ijt} + \varepsilon_{ijt} \quad j \neq i,$$

$$x_{it} = \text{Const } DPI_t \ UMP_t \ LL_{it-} \ LL_{it-} \ LL_{it-} \ LL_{it-}$$

$$z_{ijt} = \Delta LL_{ijt-} \ \Delta LL_{ijt-} \ \Delta LL_{ijt-} \ \Delta LL_{ijt-}$$

LL_{ij}

LL_{ij}

LL_{ij}

I

I

γ

j

Step $y_{it} = \alpha_i x_{it} + u_{it}$ u_{it} x_{it} z_{ijt} LL_{it} LR_{it} LL_{it}
Step LL_{jt} y_{it} x_{it} z_{it} H
Step p SI SI SI

i x_{it} x_{ijt} LL LL_{ij}
 $x_{ijt} = C \text{ DPI UMP } LL_{it-} \text{ } LL_{it-} \text{ } LL_{it-} \text{ } LL_{it-} \text{ } LL_{jt-} \text{ } LL_{jt-} \text{ } LL_{jt-} \text{ } LL_{jt-}$

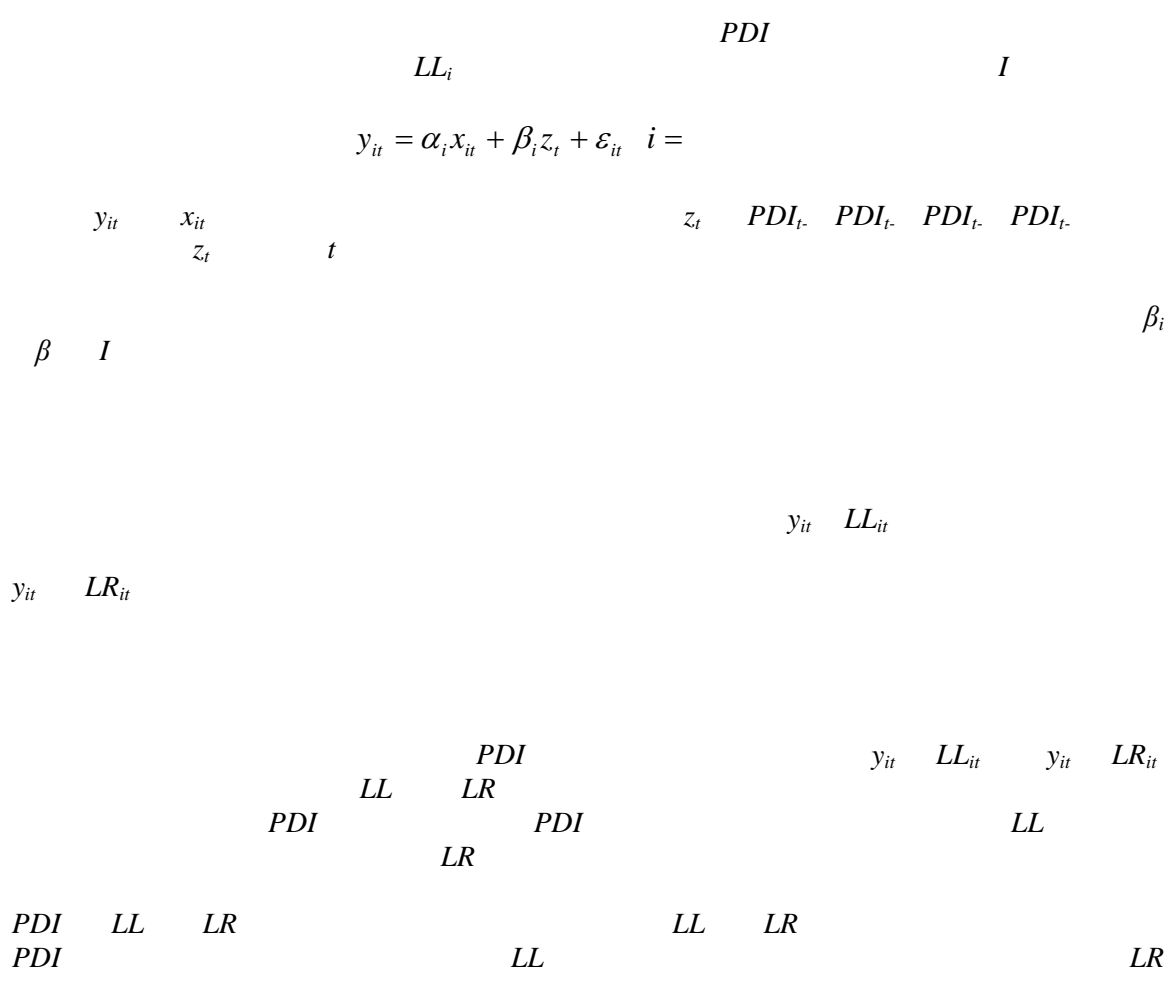
z_{ijt}

p

3.1.3 An Aggregate Performance Difference Index

PDI

$$PDI_t = \frac{\sum_{i>j} LL_{it} - LL_{jt}}{\dots}$$



3.1.4. Bank Stock Returns and Performance Differences

PDI

$$\beta_i \beta \quad I$$

PDI *PDI*

3.1.5 Rajan's Reputation Hypothesis

$$AGLL_t = \frac{\sum_i CO_{it} - RV_{it}}{\sum_i LS_{it}}$$

$AGLL_t$ $AGLL_t$ PDI_t PDI_t z_t $AGLL_t$ $AGLL_t$ $AGLL_t$ PDI $AGLL_t$ z_t $AGLL_t$ $AGLL_t$

z_t t z_t

PDI $AGLL$ $AGLL$ PDI

$AGLL$

3.2 An Aggregate Performance Difference Index for Commercial and Industrial Loans

3.2.1 VAR Analysis of the Fed's Lending Standards Index

PDI

PDI

STAND

$r_m r_f$

SMB

HML

PDI

PDI

PDI

PDI

	Coefficient on	-statistics
	-238.90	-0.90
	-49.79	-0.29
	-6.98	-0.03

PDI

PDI

PDI

R_{it}

$$PDI_t = \lambda + \sum_{i=1}^I \lambda_i R_{it} + \varepsilon_t$$

$$w_i = \frac{\lambda_i}{\sum_{i=1}^I \lambda_i}$$

$$R_{PDI_t} = \sum_{i=1}^I w_i R_{it}$$

R_{PDI}
 R_{PDI}

R_{PDI}

R_{PDI} PDI

SML HML
 PDI
 SML HML

4. Conclusion

Appendix

A. Formalization of the Stage Strategy

$$\begin{array}{ccccccc}
 & & n_i & & & & i \\
 & & & N_{ai} & N n_i & & \\
 & & F_{ai} & & & & \\
 & & & i & & & \\
 N_{gi} & n_i & & & N_{\beta i} & N_{gi} & \\
 & & & & & F_{\beta i} & i \\
 & & N_{\gamma i} & n_i & N_{gi} & & \\
 & & & F_{\gamma i} & & & F_{ai} \\
 F_{\beta i} & F_{\gamma i} & & & & & \\
 & & F_{ai} & F_{\beta i} & F_{\gamma i} & &
 \end{array}$$

$$s_i = n_i N_{\alpha} n_i N_{gi} N_{\beta} n_i N_{gi} N_{\gamma i} n_i N_{gi} F_{ai} n_i N_{gi} F_{\beta i} n_i N_{gi} F_{\gamma i} n_i N_{gi}$$

$$\begin{array}{cccc}
 n_i & & & i \\
 N_{gi} & & & & i \\
 N_{ai} & & & i & \\
 N_{\beta i} & & & & i \\
 N_{\gamma i} & & & & i \\
 F_{ai} & & & i & \\
 F_{\beta i} & & & i & \\
 F_{\gamma i} & & & i &
 \end{array}$$

B. Proof of Proposition 1

Lemma 1 *If it exists, in any symmetric stage Nash equilibrium in which neither bank conducts credit worthiness testing, each bank offers loans to all the loan applicants at the same interest rate.*

Proof.

$$\begin{array}{cccc}
 s_i = n_i = N_{ai} < N F_{ai} & & & -i \\
 s_{-i} = n_{-i} = N_{\alpha-i} = N F_{\alpha-i} & & & s_{-i} \\
 F'_{\alpha-i} & F_{ai} & N_{ai} & \\
 & & & X & F^*
 \end{array}$$

$$E\pi_i = \frac{N}{\lambda p_b + -\lambda p_g} F + -\lambda p_g F - =$$

$$F = \frac{N}{\lambda p_b + -\lambda p_g} < X$$

$$\begin{array}{ccccccc}
 F^* & j & & N & & & F_j \\
 & & F_k & F^* & & & \\
 s_i = n_i = N_{ai} < N F_{ai} & & & & F_{ai} = F & F & F_N \\
 & & & & & F_j & F_k & F_j
 \end{array}$$

$$s_{-i} = n_{-i} = N \frac{F_k}{F^*} \alpha_{-i} = N F \alpha_{-i} \quad F_{ai} = F \quad F_{k-} \quad F_k^- \quad F_{k+} \quad F_N \quad F_k$$

Proof Proposition

$$F = \frac{X}{\lambda p_b + -\lambda p_g} < X$$

$$c < \frac{-\lambda \lambda p_g - p_b}{\lambda p_b + -\lambda p_g}$$

$$F \quad F$$

$$E\pi_i^d = -\lambda p_g F - c$$

$$E\pi_i^d > c < -\lambda p_g F - c = \frac{-\lambda \lambda p_g - p_b}{\lambda p_b + -\lambda p_g}$$

$$c \geq \frac{-\lambda \lambda p_g - p_b}{\lambda p_b + -\lambda p_g} \quad F$$

C. Proof of Proposition 2

Lemma 2 *In any symmetric stage Nash equilibrium in which both banks test all the applicants, each bank offers loans to all the applicants that pass the test at the same interest rate.*

Lemma 1

Lemma 3 *If it exists, in any symmetric stage Nash equilibrium in which both banks test $n < N$ applicants, each bank offers loans to all applicants that pass the test (good types) at $F = \frac{X}{P_g}$.*

Lemma 1

Lemma 4 *If it exists, in any symmetric stage Nash equilibrium in which both banks test $n < N$ applicants, each bank either offers loans to all non-tested applicants at the same interest rate or offers loans to none of them.*

Proof.

$$F \quad X$$

$$F$$

$$F$$

F

Proof Proposition 2

$$\begin{aligned}
 & N_\beta \quad N_g \quad N_g \quad N_\gamma \\
 E\pi & \quad F_\beta \quad N \quad N_g \quad N_g \quad N_g \\
 & N_g \quad p_k \\
 E\pi_i & = E \sum_{k=1}^N -k p_k \quad p_g F_\beta \quad N \quad k \quad - \quad -Nc \geq \\
 & F_\beta \quad N_g \quad F_\beta^d \quad N_g = F_\beta^- \quad N_g \\
 E\pi_i^d & = E \sum_{k=1}^N k p_k \quad p_g F_\beta^- \quad N \quad k \quad - \quad -Nc \geq E\pi_i \\
 & F_\beta \quad F^{**} \quad F_\alpha \quad F_n \\
 & F_n \quad F^{**} \quad F_\beta \quad F^{**} \quad F_\alpha \quad F_n \\
 & F^{**}
 \end{aligned}$$

D. Formalization of the Repeated Game

$$\begin{aligned}
 & i \\
 & ii \\
 & iii \\
 & iv \\
 & v \\
 & i \\
 s_{it} & \stackrel{\infty}{t=} i \\
 & i \\
 K_{it} & = D_{\alpha it} \quad D_{\beta it} \quad D_{\gamma it} \quad \chi_{\alpha it} \quad \chi_{\beta it} \quad \chi_{\gamma it}
 \end{aligned}$$

F
 F

D

$\alpha \quad \beta \quad \gamma$
 β

χ

α

γ

$$D_{it} = D_{\alpha it} + D_{\beta it} + D_{\gamma it}$$

$$\chi_{it} = \chi_{\alpha it} + \chi_{\beta it} + \chi_{\gamma it}$$

$t \quad \kappa_t \quad \kappa_t \quad \kappa_t \quad \kappa_{it} \quad D_{it} \quad \chi_{it} \quad i$

$T \quad i$

i

i

Lemma 5 *In a Symmetric Perfect Public Equilibrium, if on the equilibrium path, banks make offers to all loan applicants without credit worthiness test at an interest rate higher than*

$F = \frac{\lambda p_b + (1-\lambda) p_g}{\lambda p_b + (1-\lambda) p_g}$, and the continuation payoffs only depend on loan portfolio distribution (D_1, D_2) , then for any value of D we have:

$$\delta u_i (D, N-D) - \delta u_i (D, N-D) = \lambda p_b + (1-\lambda) p_g F_\alpha -$$

Proof:

$$s = n = N_\alpha = N F_\alpha$$

F_α

$$F = \frac{\lambda p_b + (1-\lambda) p_g}{\lambda p_b + (1-\lambda) p_g}$$

$\chi \chi$

i

$$s, D = n = N_\alpha = D F_\alpha^- \quad D, N \quad D, D'$$

$$\pi_i (s, D, s) + \delta u_i (D, N-D) = \pi_i (s, D, s) + \delta u_i (D, N-D)$$

$$\delta u_i (D, N-D) - \delta u_i (D, N-D) = \pi_i (s, D, s) - \pi_i (s, D, s)$$

s', D

s', D

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Policy Review

Economic

Economic Policy Review

Journal of Money, Credit & Banking

The Quarterly Journal of Economics

Hand

Table II

$\alpha_i x_{it} + \beta_i z_t + \varepsilon_{it}$ $y_{it} = LL_{it}$ LR_{it} x_{it} C UMP DPI LL_{it} LL_{it} LL_{it} LL_{it} z_t PDI_{it} PDI_{it} PDI_{it} PDI_{it} y_{it} $\alpha_i x_{it} + \beta_i z_t + \varepsilon_{it}$ $y_{it} = LL_{it}$ LR_{it} x_{it} C UMP DPI LL_{it}

		Panel A												Panel B: Pooled			
		CHAS		CITI		BONE		BOAM		MBNA		WACH		OLS		SUR	
		Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat
1		-0.942	-2.10	-0.279	-0.50	-1.392	-1.42	-1.380	-2.48	-0.089	-0.47	-0.679	-3.13	-0.818	-4.30	-0.563	-4.38
2		0.039	0.09	0.140	0.27	-0.786	-0.81	-0.040	-0.07	0.080	0.41	-0.393	-1.65	-0.169	-0.88	-0.202	-1.51
3		0.161	0.35	0.161	0.31	0.135	0.14	0.099	0.17	-0.005	-0.03	-0.048	-0.20	-0.028	-0.14	-0.017	-0.13
4		-0.098	-0.22	-0.117	-0.24	-1.100	-1.19	-0.453	-0.75	0.095	0.53	-0.546	-2.31	-0.341	-1.81	-0.036	-0.27
2		0.77		0.75		0.83		0.71		0.88		0.83					
		Panel C												Panel D: Pooled			
		CHAS		CITI		BONE		BOAM		MBNA		WACH		OLS		SUR	
		Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat
1		0.144	0.30	-1.746	-2.48	-1.880	-0.78	-0.710	-2.45	0.616	0.52	0.933	0.12	-0.535	-1.32	-0.403	-2.23
2		-0.068	-0.14	-1.407	-2.16	-3.784	-1.58	-0.386	-1.33	-0.353	-0.29	-0.498	-0.58	-0.823	-2.02	-0.578	-3.19
3		-0.214	-0.44	-1.557	-2.40	-3.826	-1.61	-0.315	-1.04	-0.697	-0.57	-0.727	-0.83	-1.149	-2.79	-0.665	-3.57
4		0.187	0.39	-1.579	-2.60	-5.909	-2.61	-0.862	-2.74	1.030	0.92	-0.578	-0.67	-0.932	-2.32	-0.741	-4.02
2		0.74		0.89		0.75		0.92		0.88		0.83					

Table III

$$r_{it} = \alpha_i x_{it} + \beta_i z_t + \varepsilon_{it} \quad x_{it} \quad C \quad C \quad \text{Dividend Yield}_{it} \quad z_t \quad PDI_t \quad PDI_t \quad PDI_t \quad PDI_t$$

$$\beta_i \quad r_{it} \quad \alpha_i x_{it} + \beta_i z_t + \varepsilon_{it} \quad i$$

$$z_t \quad t$$

Without Dividend Yield	Panel A												Panel B: Pooling			
	CHAS		CITI		BONE		BOAM		MBNA		WACH		OLS		SUR	
	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat
1	-3.66	-0.75	3.53	0.66	1.46	0.39	1.35	0.36	-8.28	-1.60	-1.66	-0.48	-1.21	-0.68	-0.82	-0.32
2	-2.56	-0.53	-1.73	-0.32	-2.53	-0.67	-3.09	-0.82	1.56	0.30	-6.76	-1.95	-2.50	-1.40	-3.77	-1.48
3	-9.78	-2.02	-4.80	-0.90	-8.91	-2.37	-9.97	-2.63	-6.87	-1.33	2.00	0.57	-6.45	-3.59	-4.66	-1.83
4	-1.60	-0.32	-4.97	-0.91	-7.13	-1.86	-5.91	-1.53	-4.71	-0.90	-5.80	-1.65	-5.04	-2.77	-6.24	-2.41
2	0.13		0.07		0.14		0.25		0.13		0.16					
With Dividend Yield	Panel C												Panel D: Pooling			
	CHAS		CITI		BONE		BOAM		MBNA		WACH		OLS		SUR	
	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat	Coeff.	-stat
1	-2.72	-0.54	4.62	0.80	4.38	1.28	1.13	0.29	-8.20	-1.56	-2.71	-0.74	-0.83	-0.45	-0.69	-0.28
2	-1.65	-0.33	-1.97	-0.36	-0.66	-0.20	-3.20	-0.84	1.65	0.31	-6.96	-2.00	-2.15	-1.20	-3.48	-1.41

Table IV

C	UMP	DPI	LL_{it}	LL_{it}	LL_{it}	LL_{it}	z_t	$AGLL_t$	$AGLL_t$	$AGLL_t$	$AGLL_t$	$y_{it} = LL_{it}$	LR_{it}	x_{it}
												i		
												y_{it}	$\alpha_i x_{it} + \beta z_t + \varepsilon_{it}$	

Table VI

Variance Decomposition of :						Variance Decomposition of :					
Period	St. Error					Period	St. Error				
1	6.64	100.0	0.0	0.0	0.0	1	0.00094	0.2	99.8	0.0	0.0
3	8.03	89.5	2.9	6.9	0.8	3	0.00101	6.0	86.2	4.8	3.0
5	9.53	65.6	2.7	27.7	4.0	5	0.00134	14.5	76.6	6.5	2.4
10	11.13	50.0	13.6	32.6	3.8	10	0.00170	14.7	57.5	24.2	3.6
15	12.49	45.4	18.0	33.3	3.3	15	0.00188	14.1	58.6	23.2	4.1

Variance Decomposition of :						Variance Decomposition of :					
Period	St. Error					Period	St. Error				
1	0.231	10.7	4.7	84.6	0.0	1	0.0050	23.8	0.5	8.1	67.7
3	0.527	10.6	12.5	76.1	0.8	3	0.0131	6.6	17.9	51.8	23.7
5	0.692	13.9	21.3	64.2	0.5	5	0.0212	14.1	34.6	40.8	10.5
10	0.869	12.9	27.2	57.6	2.3	10	0.0363	23.5	50.7	21.7	4.1
15	1.017	11.6	20.7	65.2	2.6	15	0.0519	25.1	32.4	39.0	3.5

Table VII

$$r_i - r_f = \alpha + \beta_1 r_m - r_f + \beta_2 SMB + \beta_3 HML + \beta_4 R_{PDI} + \varepsilon$$

R_{PDI}

t

Coefficient (t-stat)	α Commercial Banks (using equal weighted)						α Commercial Banks (using value weighted)					
	1.556 (2.54)	1.163 (13.27)	-0.070 (-0.54)	0.464 (4.67)	0.021 (0.95)	0.72	1.628 (2.65)	1.173 (12.52)	-0.041 (-0.33)	0.488 (4.88)	0.000 (0.01)	0.72
	Non-Financial Firms (using equal weighted)						Non-Financial Firms (using value weighted)					
Decile 1 (Small)	4.940 (4.08)	0.629 (3.63)	1.657 (6.53)	-0.042 (-0.21)	0.192 (4.37)	0.65	5.146 (4.04)	0.518 (2.67)	1.983 (7.60)	0.020 (0.10)	0.208 (2.96)	0.61
Decile 2	-0.398 (-0.50)	0.766 (6.76)	1.517 (9.15)	0.108 (0.84)	0.126 (4.41)	0.79	-0.256 (-0.31)	0.696 (5.47)	1.731 (10.13)	0.151 (1.11)	0.134 (2.90)	0.76
Decile 3	-0.534 (-0.89)	0.867 (10.04)	1.445 (11.44)	0.093 (0.95)	0.078 (3.57)	0.86	-0.495 (-0.81)	0.802 (8.59)	1.585 (12.64)	0.103 (1.03)	0.105 (3.11)	0.85
Decile 4	-0.702 (-1.31)	0.946 (12.28)	1.370 (12.15)	0.160 (1.83)	0.065 (3.34)	0.88	-0.649 (-1.18)	0.901 (10.74)	1.483 (13.16)	0.175 (1.96)	0.078 (2.58)	0.88
Decile 5	-0.120 (-0.27)	1.014 (15.80)	1.284 (13.68)	0.126 (1.73)	0.049 (3.01)	0.91	-0.049 (-0.11)	0.994 (14.10)	1.364 (14.41)	0.148 (1.97)	0.044 (1.75)	0.91
Decile 6	0.287 (0.90)	1.005 (20.90)	1.322 (19.68)	0.054 (1.03)	0.011 (0.97)	0.95	0.270 (0.85)	0.985 (20.33)	1.346 (20.66)	0.047 (0.91)	0.026 (1.46)	0.95
Decile 7	0.604 (2.57)	1.081 (32.08)	1.063 (21.57)	0.033 (0.86)	-0.004 (-0.43)	0.97	0.588 (2.50)	1.077 (30.05)	1.059 (21.99)	0.027	0.001	0.97

Table VIII