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The Elasticity of Trade: Estimates and Evidence

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ABSTRACT

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1. Introduction

Quantitative results from a large class of structural gravity models of international trade depend critically on a single parameter that governs the elasticity of trade with respect to trade frictions.¹ To illustrate how important this parameter is, consider three examples: Anderson and van Wincoop (2003) find that the estimate of the tariff equivalent of the U.S.-Canada border varies between 48 and 19 percent, depending on the assumed elasticity of trade with respect to trade frictions. Yi (2003) points out that observed reductions in tariffs can explain almost all or none of the growth in world trade, depending on this elasticity. Arkolakis, Costinot, and Rodriguez-Clare (2011) argue that this parameter is one of only two parameters needed to measure the welfare cost of autarky in a large and important class of trade models. Therefore, this elasticity is key to understanding the size of the frictions to trade, the response of trade to changes in tariffs, and the welfare gains or losses from trade.

Estimating this parameter is difficult because quantitative trade models can rationalize small trade flows with either large trade frictions and small elasticities, or small trade frictions and large elasticities. Thus, one needs satisfactory measures of trade frictions *independent* of trade flows to estimate this elasticity. Eaton and Kortum (2002) (henceforth EK) provide an innovative and simple solution to this problem by arguing that, with product-level price data, one could use the maximum price difference across goods between countries as a proxy for bilateral trade frictions. The maximum price difference between two countries is meaningful because it is bounded by the trade friction between the two countries via simple no-arbitrage arguments.

We develop a new simulated method of moments estimator for the elasticity of trade incorporating EK's intuition. The argument for a new estimator is that their method results in estimates that are biased upward by economically significant magnitudes. We prove this result and then provide quantitative measures of the bias via Monte Carlo simulations of the EK model. Finally, we apply our estimator to novel disaggregate price and trade-flow data for the year 2004, spanning 123 countries that account for 98 percent of world output. Our benchmark estimate for the elasticity of trade is 4.12, rather than approximately eight, as EK's estimation strategy suggests. This difference doubles the measured welfare gains from international trade across various models.

Since the elasticity of trade plays a key role in quantifying the welfare gains from trade, it is important to understand why our estimates of the parameter differ substantially from EK's.

¹These models include Krugman (1980), Anderson and van Wincoop (2003), Eaton and Kortum (2002), and Melitz (2003) as articulated in Chaney (2008), which all generate log-linear relationships between bilateral trade flows and trade frictions.

We show that the reason behind the difference is that their estimator is biased in finite samples of price data. The bias arises because the model's equilibrium no-arbitrage conditions imply that the maximum operator over a finite sample of prices underestimates the trade cost with positive probability and overestimates the trade cost with zero probability. Consequently, the maximum price difference lies strictly below the true trade cost, in expectation. This implies that EK's estimator delivers an elasticity of trade that lies strictly above the true parameter, in expectation. As the sample size grows to infinity, EK's estimator can uncover the true elasticity of trade, which necessarily implies that the bias in the estimates of the parameter is eliminated.

Quantitatively, the bias is substantial. To illustrate its severity, we discretize EK's model, simulate trade flows and product-level prices under an assumed elasticity of trade, and apply their estimating approach on artificial data. Assuming a trade elasticity of 8.28, EK's preferred estimate for 19 OECD countries in 1990, the procedure suggests an estimate of 12.5, nearly 50-percent higher than originally postulated. Moreover, in practice, the true parameter can be recovered when 50,000 goods are sampled across the 19 economies, which constitutes an extreme data requirement to produce unbiased estimates of the elasticity of trade.

Based on these arguments, we propose an estimator that is applicable when the sample size of prices is small. Our approach builds on our insight that one can use observed bilateral trade flows to recover all sufficient parameters to simulate EK's model and obtain trade flows and prices as functions of the parameter of interest. This insight then suggests a simulated method of moments estimator that minimizes the distance between the moments obtained by applying EK's approach on real and artificial data. We explore the properties of this estimator numerically using simulated data and show that it can uncover the true elasticity of trade.

Applying our estimator to alternative data sets and conducting several robustness exercises allows us to establish a range for the elasticity of trade between 2.47 and 4.42. In contrast, EK's approach would have found a range of 4.17 and 7.75. Thus, our method finds elasticities that are roughly half the size of EK's approach. Because the inverse of this elasticity linearly controls changes in real income necessary to compensate a representative consumer for going to autarky, resolving this bias doubles the welfare gains from international trade.

The elasticity of trade has been a focus of many studies; see for example the seminal works of Feenstra (1994) and Broda and Weinstein (2006), and Anderson and van Wincoop (2004) for a survey. Like the existing literature, our estimation approach relies on the gravity equation of trade. Unlike the literature, our paper's methodological insight is to exploit the

particular micro-level structure of the EK model to correct for data limitations. As we show quantitatively, this insight is powerful and has large welfare implications.

Finally, our estimation approach would not have been possible in models without heterogeneous outcomes such as Krugman (1980) and the Armington model of Anderson and van Wincoop (2003). This is an important point in light of Arkolakis, Costinot, and Rodriguez-Clare's (2011) arguments. While the new international trade models of EK, Melitz (2003) and Chaney (2008) give the same formula for the welfare gains from trade as Krugman (1980) or a simple Armington model would, their heterogeneous micro-level structure enables researchers to better estimate the elasticity of trade with a gravity-based estimator. Our paper illustrates this point and thus provides an alternative rationale for the value added of new heterogeneous production models of trade.

2. Model

We outline the environment of the multi-country Ricardian model of trade introduced by EK. We consider a world with N countries, where each country has a tradable final-goods sector. There is a continuum of tradable goods indexed by $j \in [0, 1]$.

Within each country i , there is a measure of consumers L_i . Each consumer has one unit of time supplied inelastically in the domestic labor market and enjoys the consumption of a CES bundle of final tradable goods with elasticity of substitution $\rho > 1$:

$$U_i = \left[\int_0^1 x_i(j)^{\frac{\rho-1}{\rho}} dj \right]^{\frac{\rho}{\rho-1}}.$$

To produce quantity $x_i(j)$ in country i , a firm employs labor using a linear production function with productivity $z_i(j)$. Country i 's productivity is, in turn, the realization of a random variable (drawn independently for each j) from its country-specific Fréchet probability distribution:

$$F_i(z_i) = \exp(-T_i z_i^{-\theta}). \tag{1}$$

The country-specific parameter $T_i > 0$ governs the location of the distribution; higher values of it imply that a high productivity draw for any good j is more likely. The parameter $\theta > 1$ is common across countries and, if higher, it generates less variability in productivity across goods.

Having drawn a particular productivity level, a perfectly competitive firm from country

i incurs a marginal cost to produce good j of $w_i/z_i(j)$, where w_i is the wage rate in the economy. Shipping the good to a destination n further requires a per-unit iceberg trade cost of $\tau_{ni} > 1$ for $n \neq i$, with $\tau_{ii} = 1$. We assume that cross-border arbitrage forces effective geographic barriers to obey the triangle inequality: For any three countries i, k, n , $\tau_{ni} \leq \tau_{nk}\tau_{ki}$.

Below, we describe equilibrium prices, trade flows, and welfare.

Perfect competition forces the price of good j from country i to destination n to be equal to the marginal cost of production and delivery:

$$p_{ni}(j) = \frac{\tau_{ni}w_i}{z_i(j)}.$$

So, consumers in destination n would pay $p_{ni}(j)$, should they decide to buy good j from country i .

Consumers purchase good j from the low-cost supplier; thus, the actual price consumers in n pay for good j is the minimum price across all sources k :

$$p_n(j) = \min_{k=1, \dots, N} \left\{ p_{nk}(j) \right\}. \quad (2)$$

The pricing rule and the productivity distribution allow us to obtain the following CES exact price index for each destination n :

$$P_n = \gamma \Phi_n^{-\frac{1}{\theta}} \quad \text{where} \quad \Phi_n = \left[\sum_{k=1}^N T_k (\tau_{nk} w_k)^{-\theta} \right]. \quad (3)$$

In the above equation, $\gamma = [\Gamma(\frac{\theta+1-\rho}{\theta})]^{-\frac{1}{1-\rho}}$ is the Gamma function, and parameters are restricted such that $\theta > \rho - 1$.

To calculate trade flows between countries, let X_n be country n 's expenditure on final goods, of which X_{ni} is spent on goods from country i . Since there is a continuum of goods, computing the fraction of income spent on imports from i , X_{ni}/X_n , can be shown to be equivalent to finding the probability that country i is the low-cost supplier to country n given the joint distribution of efficiency levels, prices, and trade costs for any good j . The expression for the share of expenditures that country n spends on goods from country i or, as we will call it, the trade share is:

$$\frac{X_{ni}}{X_n} = \frac{T_i (\tau_{ni} w_i)^{-\theta}}{\sum_{k=1}^N T_k (\tau_{nk} w_k)^{-\theta}}. \quad (4)$$

Expressions (3) and (4) allow us to relate trade shares to trade costs and the price indices of each trading partner via the following equation:

$$\frac{X_{ni}/X_n}{X_{ii}/X_i} = \frac{\Phi_i}{\Phi_n} \tau_{ni}^{-\theta} = \left(\frac{P_i \tau_{ni}}{P_n} \right)^{-\theta}, \quad (5)$$

where $\frac{X_{ii}}{X_i}$ is country i 's expenditure share on goods from country i , or its home trade share.

In this model, it is easy to show that the welfare gains from trade are essentially captured by changes in the CES price index a representative consumer faces. Because of the tight link between prices and trade shares, this model generates the following relationship between changes in price indices and changes in home trade shares, as well as, the elasticity parameter:

$$\frac{P'_n}{P_n} - 1 = 1 - \left(\frac{X'_{nn}/X'_n}{X_{nn}/X_n} \right)^{\frac{1}{\theta}}, \quad (6)$$

where the left-hand side can be interpreted as the percentage compensation a representative consumer in country n requires to move between two trading equilibria.

Expression (5) is not particular to EK's model. Several popular models of international trade relate trade shares, prices and trade costs in the same exact manner. These models include the Armington framework of Anderson and van Wincoop (2003), as well as, the monopolistic competition frameworks of firm heterogeneity by Melitz (2003) and Chaney (2008), and firm homogeneity by Krugman (1980). Arkolakis, Costinot, and Rodriguez-Clare (2011) show how equation (6) arises within these same models.

2.1. The Elasticity of Trade

The key parameter determining trade flows (equation (5)) and welfare (equation (6)) is θ . To see the parameter's importance for trade flows, take logs of equation (5) yielding:

$$\log \left(\frac{X_{ni}/X_n}{X_{ii}/X_i} \right) = -\theta \log(\tau_{ni}) - \theta \log(P_i) + \theta \log(P_n). \quad (7)$$

As this expression makes clear, θ controls how a change in the bilateral trade costs, τ_{ni} , will change bilateral trade between two countries. This elasticity is important because if one wants to understand how a bilateral trade agreement will impact aggregate trade or to simply understand the magnitude of the trade friction between two countries, then a stand on this elasticity is necessary. This is what we mean by the elasticity of trade.

To see the parameter's importance for welfare, it is fairly easy to demonstrate that (6) implies that θ represents the inverse of the elasticity of welfare with respect to domestic expenditure shares:

$$\log(P_n) = -\frac{1}{\theta} \log\left(\frac{X_{nn}}{X_n}\right) \quad (8)$$

Hence, decreasing the domestic expenditure share by one percent generates $(1/\theta)/100$ -percent increase in consumer welfare. Thus, in order to measure the impact of trade policy on welfare, it is sufficient to obtain data on realized domestic expenditures and an estimate of the elasticity of trade.

Given θ 's impact on trade flows and welfare, this elasticity is absolutely critical in any quantitative study of international trade.

3. Estimating θ : EK's Approach

Equation (5) suggests that one could easily estimate θ if one had data on trade shares, aggregate prices, and trade costs. The key issue is that trade costs are not observed. In this section, we discuss how EK approximate trade costs and estimate θ . Then, we characterize the statistical properties of EK's estimator. The key result is Proposition 1, which states that their me

relative to country i must satisfy the following inequality:

$$\frac{p_n(\ell)}{p_i(\ell)} \leq \tau_{ni}. \quad (9)$$

That is, the relative price of good ℓ must be less than or equal to the trade friction. This inequality must hold because if it does not, then $p_n(\ell) > \tau_{ni}p_i(\ell)$ and an agent could import ℓ at a lower price. Thus, the inequality in (9) places a lower bound on the trade friction.

Improvements on this bound are possible if we observe a sample of L goods across locations. This follows by noting that the *maximum* relative price difference must satisfy the same inequality:

$$\max_{\ell \in L} \left\{ \frac{p_n(\ell)}{p_i(\ell)} \right\} \leq \tau_{ni}. \quad (10)$$

This suggests a way to exploit *disaggregate* price information across countries and to arrive at an estimate of τ_{ni} by taking the maximum of relative prices over goods. Thus, EK approximate τ_{ni} , in logs, by

$$\log \hat{\tau}_{ni}(L) = \max_{\ell \in L} \{ \log(p_n(\ell)) - \log(p_i(\ell)) \}, \quad (11)$$

where the “hat” denotes the approximated value of τ_{ni} and (L) indexes its dependence on the sample size of prices.

3.2. Estimating the Elasticity

Given the approximation of trade costs, EK simply take equation (7) and run a regression. Thus, for a sample of L goods, they essentially estimate a parameter, β , using the following equations:

$$\log \left(\frac{X_{ni}/X_n}{X_{ii}/X_i} \right) = -\beta \left(\log \hat{\tau}_{ni}(L) + \log \hat{P}_i - \log \hat{P}_n \right), \quad (12)$$

$$\text{where } \log \hat{\tau}_{ni}(L) = \max_{\ell \in L} \{ \log p_n(\ell) - \log p_i(\ell) \},$$

$$\text{and } \log \hat{P}_i = \frac{1}{L} \sum_{\ell=1}^L \log(p_i(\ell)).$$

As discussed, the second line of expression (12) approximates the trade cost. The third line approximates the aggregate price indices. The top line relates these observables to the regression they run.

To recover β , EK employ a method of moments estimator by taking the average of the left-hand side of (12) divided by the average of the right-hand side of (12), with the averages across all country pairs.³

Mathematically, their estimator is:

$$\hat{\beta} = -\frac{\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)}{\sum_n \sum_i \left(\log \hat{\tau}_{ni}(L) + \log \hat{P}_i - \log \hat{P}_n\right)}. \quad (13)$$

The value of β is EK's preferred estimate of the elasticity θ .⁴ Throughout, we will denote by $\hat{\beta}$ the estimator defined in equation (13) to distinguish it from the value θ .

3.3. Properties of EK's Estimator

Before proving properties of the estimator $\hat{\beta}$, we want to be clear about the sources of randomness in equation (12). We view the trade data on the left-hand side of (12) as being fixed. The variables on the right-hand side of (12) are random variables. That is, we are treating the micro-level prices as being randomly sampled from the equilibrium distribution of prices. The parameterization of productivity draws in equation (1), marginal cost pricing, and equation (2) are sufficient to characterize these distributions. This interpretation is consistent with EK's interpretation.

Given that random variation in the sampled prices is the source of randomness, we define the following objects.

Definition 1 *Define the following objects*

1. Let $\epsilon_{ni} = \theta[\log p_n - \log p_i]$ be the log price difference of a good between country n and country i , multiplied by θ .
2. Let the vector $\mathbf{S} = \{\log(T_1 w_1^{-\theta}), \dots, \log(T_N w_N^{-\theta})\}$.

³They also propose two other estimators. One uses the approximation in (11) and the gravity equation in (22) — our arguments are applicable to this approach as well. The other approach does not use disaggregate price data and this estimate is remarkably similar to our benchmark results.

⁴To alleviate measurement error, they resort to using the second-order statistic over price differences rather than the first-order statistic. Our estimation approach is robust to the consideration of using the first- or second-order statistic.

3. Let the vector $\tilde{\tau}_i = \{\theta \log(\tau_{i1}), \dots, \theta \log(\tau_{iN})\}$ and let $\tilde{\tau}$ be a matrix with typical row, $\tilde{\tau}_i$.
4. Let $g(p_i; \mathbf{S}, \tilde{\tau}_i)$ be the pdf of prices of individual goods in country i , $p_i \in (0, \infty)$.
5. Let $f_{\max}(\epsilon_{ni}; L, \mathbf{S}, \tilde{\tau}_i, \tilde{\tau}_n)$ be the pdf of $\max(\epsilon_{ni})$, given prices of a sample $L \geq 1$ of goods.
6. Let \mathbb{X} denote the normalized trade share matrix, with typical (n, i) element, $\log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)$.

The first item is simply the scaled log price difference. As we show in Appendix B.1, this happens to be convenient to work with, as the second line in (12) can be restated in terms of scaled log price differences across locations. The second item is a vector in which each element is a function of a country's technology parameter and wage rate. The third item is a matrix of log bilateral trade costs, scaled by θ , with a typical vector row containing the trade costs that country i 's trading partners incur to sell there. The fourth item specifies the probability distribution of prices in each country. The fifth item specifies the probability distribution over the maximum scaled log price difference and its dependence on the sample size of prices of L goods. We derive this distribution in Appendix B.1. Finally, the sixth item summarizes trade data, which we view as constant.

3.4. $\hat{\beta}$ is a Biased Estimator of θ

Given these definitions, we establish two intermediate results and then state Proposition 1, which characterizes the expectation of $\hat{\beta}$, shows that the estimator is biased and discusses the reason why the bias arises. The proof of Proposition 1 can be found in Appendix B.1.

The first intermediate result is the following:

Lemma 1 *Consider an economy of N countries with a sample of L goods' prices observed. The expected value of the maximal difference of logged prices for a pair of countries is strictly less than the true trade cost,*

$$\Psi_{ni}(L; \mathbf{S}, \tilde{\tau}_i, \tilde{\tau}_n) \equiv \frac{1}{\theta} \int_{-\theta \log(\tau_{in})}^{\theta \log(\tau_{ni})} \epsilon_{ni} f_{\max}(\epsilon_{ni}; L, \mathbf{S}, \tilde{\tau}_i, \tilde{\tau}_n) d\epsilon_{ni} < \log(\tau_{ni}). \quad (14)$$

The difference in the expected values of logged prices for a pair of countries equals the difference in the price parameters, Φ , of the two countries,

$$\Omega_{ni}(\mathbf{S}, \tilde{\tau}_n, \tilde{\tau}_i) \equiv \int$$

The key result in Lemma 1 is the strict inequality in (14). It says that Ψ_{ni} , the expected maximal logged price difference, is less than the true trade cost. Two forces drive this result. First, with a finite sample L of prices, there is positive probability that the maximal logged price difference will be less than the true trade cost. In other words, there is always a chance that the weak inequality in (10) does not bind. Second, there is zero probability that the maximal logged price difference can be larger than the true trade cost. This comes from optimality and the definition of equilibrium. These two forces imply that the expected maximal logged price difference lies strictly below the true trade cost.

The second result in Lemma 1 is that the difference in the expected log prices in expression (15) equals the difference in the aggregate price parameters defined in equation (3). This result is important because it implies that any source of bias in the estimator $\hat{\beta}$ does not arise because of systematic errors in approximating the price parameter Φ_n .

The next intermediate step computes the expected value of $1/\hat{\beta}$. This step is convenient because the inverse of $\hat{\beta}$ is linear in the random variables that Lemma 1 characterizes.

Lemma 2 *Consider an economy of N countries with a sample of L goods' prices observed. The expected value of $1/\hat{\beta}$ equals:*

$$E\left(\frac{1}{\hat{\beta}}\right) = \frac{1}{\theta} \left\{ -\frac{\sum_n \sum_i (\theta \Psi_{ni}(L) - (\log \Phi_i - \log \Phi_n))}{\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)} \right\} < \frac{1}{\theta}, \quad (16)$$

with

$$1 > \left\{ -\frac{\sum_n \sum_i (\theta \Psi_{ni}(L) - (\log \Phi_i - \log \Phi_n))}{\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)} \right\} > 0. \quad (17)$$

This results says that the expected value of the inverse of $\hat{\beta}$ equals the inverse of the elasticity multiplied by the bracketed term of (17). The bracketed term is the expected maximal logged price difference minus the difference in expected logged prices, both scaled by theta, and divided by trade data. This term is strictly less than one because Ψ_{ni} does not equal the trade cost, as established in Lemma 1. If Ψ_{ni} did equal the trade cost, then the bracketed term would equal one, and the expected value of the inverse of $\hat{\beta}$ would be equal to the inverse of θ . This can be seen by examining the relation between Φ s and aggregate prices P s in (3), and by substituting expression (7) into (17).

Inverting (16) and then applying Jensen's inequality establishes the main result: that EK's estimator is biased above the true value of θ .

Proposition 1 Consider an economy of N countries with a sample of L goods' prices observed. The expected value of $\hat{\beta}$ is

$$E(\hat{\beta}) \geq \theta \times \left\{ -\frac{\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)}{\sum_n \sum_i (\theta \Psi_{ni}(L) - (\log \Phi_i - \log \Phi_n))} \right\} > \theta. \quad (18)$$

The proposition establishes that the estimator $\hat{\beta}$ provides estimates that exceed the true value of the elasticity θ . The weak inequality in (18) comes from applying Jensen's inequality to the strictly convex function of $\hat{\beta}$, $1/\hat{\beta}$. The strict inequality follows from Lemma 1, which argued that the expected maximal logged price difference is strictly less than the true trade cost. Thus, the bracketed term in expression (18) is always greater than one and the elasticity of trade is always overestimated.

3.5. Consistency and Asymptotic Bias

While the estimator $\hat{\beta}$ is biased in a finite sample, the asymptotic properties of EK's estimator are worth understanding. Proposition 2 summarizes the result. The proof to Proposition 2 can be found in Appendix B.2.

Proposition 2 Consider an economy of N countries. The maximal log price difference is a consistent estimator of the trade cost,

$$\text{plim}_{L \rightarrow \infty} \max_{\ell=1, \dots, L} (\log p_n(\ell) - \log p_i(\ell)) = \log \tau_{ni}. \quad (19)$$

The estimator $\hat{\beta}$ is a consistent estimator of θ ,

$$\text{plim}_{L \rightarrow \infty} \hat{\beta}(L; \mathbf{S}, \tilde{\boldsymbol{\tau}}, \mathbb{X}) = \theta, \quad (20)$$

and the asymptotic bias of $\hat{\beta}$ is zero,

$$\lim_{L \rightarrow \infty} E \left[\hat{\beta}(L; \mathbf{S}, \tilde{\boldsymbol{\tau}}, \mathbb{X}) \right] - \theta = 0. \quad (21)$$

There are three elements to Proposition 2, each building on the previous one. The first statement says that the probability limit of the maximal log price difference equals the true trade cost between two countries. Intuitively, this says that as the sample size becomes large, the probability that the weak inequality in (10) does not bind becomes vanishingly small.

The second statement says that the estimator $\hat{\beta}$ converges in probability to the elasticity of trade—i.e., $\hat{\beta}$ is a consistent estimator of θ . The reasons are the following. Because the maximal price difference converges in probability to the true trade cost, and the difference in averages of log prices converges in probability to the difference in price parameters, $1/\hat{\beta}$ converges in probability to $1/\theta$. Since $1/\hat{\beta}$ is a continuous function of $\hat{\beta}$ (with $\hat{\beta} > 0$), $\hat{\beta}$ must converge in probability to θ because of the preservation of convergence for continuous functions (see Hayashi (2000)).

The third statement says that, in the limit, the bias is eliminated. This follows immediately from the argument that $\hat{\beta}$ is a consistent estimator of θ (see Hayashi (2000)).

The results in Proposition 2 are important for two reasons. First, they suggest that with enough data, EK’s estimator provides informative estimates of the elasticity of trade. However, as we will show in the next section, Monte Carlo exercises suggest that the data requirements are extreme. Second, because EK’s estimator has desirable asymptotic properties, it underlies the simulation-based estimator that we develop in Section 5.

4. How Large is the Bias? How Much Data is Needed?

Proposition 1 shows EK’s estimator is biased in a finite sample. Many estimators have this property, which raises the question: How large is the bias? Furthermore, even if the magnitude of the bias is large, perhaps only moderate increases in the sample size are sufficient to eliminate the bias (in practical terms). The natural question is then: How much data is needed to achieve that?

To answer these questions, we perform Monte Carlo experiments in which we simulate trade flows and samples of micro-level prices under a known θ . Then, we apply EK’s estimator to the artificial data. We employ the same simulation procedure described in Steps 1-3 in Section 5.2 and we estimate all parameters (except for θ) using the trade data from EK. We set the true value of θ equal to 8.28, which is EK’s estimate when employing the approach described above. The sample size of prices is set to $L = 50$, which is the number of prices EK had access to in their data set.

Table 1 presents the findings. The columns of Table 1 present the mean and median estimates of β over 100 simulations. The rows present two different estimation approaches: method of moments and least squares with suppressed constant. Also reported are the true average trade cost and the estimated average trade cost using maximal log price differences.

The first row in Table 1 shows that the estimates using EK’s approach are larger than the

Table 1: Monte Carlo Results, True $\theta = 8.28$

Approach	Mean Estimate of θ (S.E.)	Median Estimate of θ
EK's Estimator	12.5 (0.06)	12.5
Least Squares	11.8 (0.06)	11.8
True Mean $\tau = 1.79$	Estimated Mean $\tau = 1.48$	

Note: S.E. is the standard error of the mean. In each simulation there are 19 countries and 500,000 goods. Only 50 realized prices are randomly sampled and used to estimate θ . 100 simulations performed.

true θ of 8.28, which is consistent with Proposition 1. The key source of bias in Proposition 1 was that the estimates of the trade costs were biased downward, as Lemma 1 argued. The final row in Table 1 illustrates that the estimated trade costs are below the true trade costs, where the latter correspond to an economy characterized by a true elasticity of trade among 19 OECD countries of 8.28.

The second row in Table 1 reports results using a least squares estimator with the constant suppressed rather than the method of moments estimator.⁵ Similar to the method of moments estimates, the least squares estimates are substantially larger than the true value of θ . This is important because it suggests that the key problem with EK's approach is not the method of moment estimator per se, but, instead, the poor approximation of the trade costs.

The final point to note is that the magnitude of the bias is substantial. The underlying θ was set equal to 8.28, and the estimates in the simulation are between 11.8 and 12.5. Equation (8) can be used to formulate the welfare cost of the bias. It suggests that the welfare gains from trade will be underestimated by 50 percent as a result of the bias.

How much data is needed to eliminate the bias? Table 2 provides a quantitative answer. It performs the same Monte Carlo experiments described above, as the sample size of micro-level prices varies.

Table 2 shows that, as the sample size becomes larger, the estimate of θ becomes less biased and begins to approach the true value of θ . The final column shows how the reduction in the bias coincides with the estimates of the trade costs becoming less biased. This is consistent with the arguments of Proposition 2, which describes the asymptotic properties

⁵Including a constant in least squares results in slope coefficient that underestimate the true elasticity. This result is symptomatic of an "errors in variables" problem.

Table 2: Increasing the Sample of Prices Reduces the Bias, True $\theta = 8.28$

Sample Size of Prices	Mean θ (S.E.)	Median θ	Mean τ
50	12.51 (0.06)	12.50	1.48
500	9.34 (0.02)	9.32	1.68
5,000	8.43 (0.01)	8.43	1.77
50,000	8.30 (0.002)	8.30	1.78

Note: S.E. is the standard error of the mean. In each simulation, there are 19 countries and 500,000 goods. The results reported use least squares with the constant suppressed. 100 simulations performed. True Mean $\tau = 1.79$.

of this estimator.

We should note that the rate of convergence is extremely slow; even with a sample size of 5,000, the estimate of β is meaningfully larger than the value generating the data. Only when 50,000 prices are sampled does the estimate approach the true value. This exercise allows us to conclude that the data requirements to minimize the bias in estimates of the elasticity of trade (in practice) are extreme. This motivates our alternative estimation strategy in the next section.

5. A New Approach To Estimating θ

In this section, we develop a new approach to estimating θ and discuss its performance on simulated data.

5.1. The Idea

Our idea is to exploit the structure of the model in the following way. First, in Section 5.2, we show how to recover all parameters necessary to simulate the model up to the unknown scalar θ from trade data only. These parameters are the vector \mathbf{S} and the scaled trade costs in matrix $\tilde{\tau}$. Given these values, we can simulate moments from the model as functions of θ .

Second, Lemma 1 and Lemma 2 actually suggest which moments are informative. Inspection of the integral (14) and the density f_{max} in (b.28) leads to the observation that the expected maximal log price difference monotonically varies with θ and linearly with $1/\theta$. This follows because of the previous point—the vector \mathbf{S} and scaled log trade costs $\tilde{\tau}$ are pinned down by trade data, and these values completely determine all parameters in the integral

(14), except the value $1/\theta$ lying outside the integral. Similarly, the integral (15) is completely determined by these values and scaled in the same way by $1/\theta$ as (14) is.

These observations have the following implication. While the maximum log price difference is biased below the true trade cost, if θ is large, then the value of the maximum log price difference will be small. Similarly, if θ is small, then the value of the maximum log price difference will be large. A large or small maximum log price difference will result in a small or large estimate of $\hat{\beta}$. This suggests that the estimator $\hat{\beta}$ will vary monotonically with the true value of θ . Furthermore, this suggests that $\hat{\beta}$ is an informative moment with regard to θ .⁶

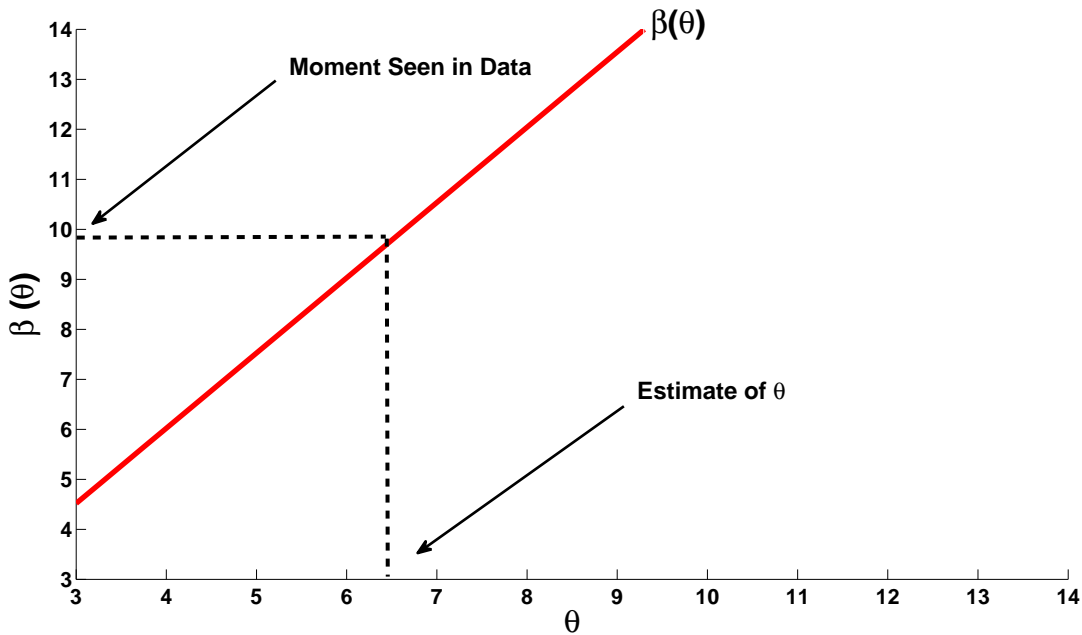


Figure 1: Schematic of Estimation Approach

Figure 1 quantitatively illustrates this intuition by plotting $\beta(\theta)$ from simulations as we varied θ . It is clear that β is a biased estimator because these values do not lie on the 45° line. However, β varies near linearly with θ . These observations suggest an estimation procedure that matches the data moment β to the moment $\beta(\theta)$ implied by the simulated model under a known θ .⁷ Because of the monotonicity implied by our arguments, the known θ must be the unique value that satisfies the moment condition specified.

⁶While we have not shown this formally, it can be shown that the expected value of $1/\hat{\beta}$ is proportional to $1/\theta$. Modulo effects from Jensen's inequality, this suggests that $\hat{\beta}$ is proportional to θ . Figure 1 confirms this.

⁷Another reason for using the moment β is that it is a consistent estimator of θ , as argued in Proposition 2.

5.2. Simulation Approach

We show how to recover all parameters of interest up to the unknown scalar θ from trade data only, and then we describe our simulation approach. This provides the foundations for the simulated method of moments estimator we propose.

Step 1.—We estimate parameters for the country-specific productivity distributions and trade costs from bilateral trade-flow data. We perform this step by following EK and Waugh (2010b) and deriving the gravity equation from expression (4), by dividing the bilateral trade share by the importing country’s home trade share,

$$\log \left(\frac{X_{ni}/X_n}{X_{nn}/X_n} \right) = S_i - S_n - \theta \log \tau_{ni}, \quad (22)$$

where S_i is defined as $\log [T_i w_i^{-\theta}]$ and is the same value in the parameter vector \mathbf{S} in Definition 1. Note that this is a different equation than expression (5), which is derived by dividing the bilateral trade share by the exporting country’s home trade share, and is used to estimate θ . S_i s are recovered as the coefficients on country-specific dummy variables given the restrictions on how trade costs can covary across countries. Following the arguments of Waugh (2010b), trade costs take the following functional form:

$$\log(\tau_{ni}) = d_k + b_{ni} + ex_i + \nu_{ni}. \quad (23)$$

Here, trade costs are a logarithmic function of distance, where d_k with $k = 1, 2, \dots, 6$ is the effect of distance between country i and n lying in the k th distance intervals.⁸ b_{ni} is the effect of a shared border in which $b_{ni} = 1$, if country i and n share a border and zero otherwise. The term ex_i is an exporter fixed effect and allows for the trade-cost level to vary depending upon the exporter. We assume that ν_{ni} reflects other factors and is orthogonal to the regressors and normally distributed with mean zero and standard deviation σ_ν . We use least squares to estimate equations (22) and (23).

Step 2.—The parameter estimates obtained from the first-stage gravity regression are sufficient to simulate trade flows and micro-level prices up to a constant, θ .

The relationship is obvious in the estimation of trade barriers since $\log(\tau_{ni})$ is scaled by θ in (22). To see that we can simulate micro-level prices as a function of θ only, notice that for any good j , $p_{ni}(j) = \tau_{ni} w_i / z_i(j)$. Thus, rather than simulating productivities, it is sufficient

⁸Intervals are in miles: [0, 375); [375, 750); [750, 1500); [1500, 3000); [3000, 6000); and [6000, maximum]. An alternative to specifying a trade-cost function is to recover scaled trade costs as a residual using equation (5), trade data, and measures of aggregate prices as in Waugh (2010a).

to simulate the inverse of marginal costs of production $u_i(j) = z_i(j)/w_i$. In Appendix B.3, we show that u_i is distributed according to:

$$M_i(u_i) = \exp\left(-\tilde{S}_i u_i^{-\theta}\right), \text{ with } \tilde{S}_i = \exp(S_i) = T_i w_i^{-\theta}. \quad (24)$$

Thus, having obtained the coefficients S_i from the first-stage gravity regression, we can simulate the inverse of marginal costs and prices.

To simulate the model, we assume that there are a large number (150,000) of potentially tradable goods. In Section 8.1, we discuss how we made this choice and the motivation behind it. For each country, the inverse marginal costs are drawn from the country-specific distribution (24) and assigned to each good. Then, for each importing country and each good, the low-cost supplier across countries is found, realized prices are recorded, and aggregate bilateral trade shares are computed.

Step 3.—From the realized prices, a subset of goods common to all countries is defined and the subsample of prices is recorded – i.e., we are acting as if we were collecting prices for the international organization that collects the data. We added disturbances to the predicted trade shares with the disturbances drawn from a mean zero normal distribution with the standard deviation set equal to the standard deviation of the residuals from Step 1.

These steps then provide us with an artificial data set of micro-level prices and trade shares mimicking their analogs in the data. Given this artificial data set, we can then compute moments—as a function of θ —to compare to moments in the data.

5.3. Estimation

Below, we describe the moments we try to match and the formalities of our estimation procedure.

5.3.1. Moments

In this section, we define the moments of interest. We perform two estimations: one overidentified procedure with two moments and an exactly identified procedure with one moment.

Define β_k as EK's method of moment estimator defined in (12) using the k th-order statistic

over micro-level price differences. Then, the moments we are interested in are:

$$\beta_k = -\frac{\sum_n \sum_i \log \left(\frac{X_{ni}/X_n}{X_{ii}/X_i} \right)}{\sum_n \sum_i \left(\log \hat{\tau}_{ni}^k(L) + \log \hat{P}_i - \log \hat{P}_n \right)}, \quad k = 1, 2 \quad (25)$$

where $\hat{\tau}_{ni}^k(L)$ is computed as the k th-order statistic over L micro-level price differences between countries n and i . In the exactly identified estimation, we use β_1 as the only moment.

We denote the simulated moments by $\beta_1(\theta, u_s)$ and $\beta_2(\theta, u_s)$, which come from the analogous formula as in (25) and are estimated from artificial data generated by following **Steps 1-3** above. Note that these moments are a function of θ and depend upon a vector of random variables u_s associated with a particular simulation s . There are three components to this vector. First, there are the random productivity draws for production technologies for each good and each country. The second component is the set of goods sampled from all countries. The third component mimics the residuals ν_{ni} from equation (22), which are described in Section 5.2.

Stacking our data moments and averaged simulation moments gives us the following zero function:

$$y(\theta) = \begin{bmatrix} \beta_1 - \frac{1}{S} \sum_{s=1}^S \beta_1(\theta, u_s) \\ \beta_2 - \frac{1}{S} \sum_{s=1}^S \beta_2(\theta, u_s) \end{bmatrix}. \quad (26)$$

5.3.2. Estimation Procedure

We base our estimation procedure on the moment condition:

$$E[y(\theta_o)] = 0,$$

where θ_o is the true value of θ . Thus, our simulated method of moments estimator is

$$\hat{\theta} = \arg \min_{\theta} [y(\theta)' \mathbf{W} y(\theta)], \quad (27)$$

where \mathbf{W} is a 2×2 weighting matrix that we discuss below.

The idea behind this moment condition is that, though β_1 and β_2 will be biased away from θ , the moments $\beta_1(\theta, u_s)$ and $\beta_2(\theta, u_s)$ will be biased by the same amount when evaluated at θ_o , in expectation. Viewed in this language, our moment condition is closely related to the estimation of bias functions discussed in MacKinnon and Smith (1998) and to indirect

inference, as discussed in Smith (2008). The key issue in MacKinnon and Smith (1998) is how the bias function behaves. As we argued in Section 5.1, the bias is monotonic in the parameter of interest and Figure 1 shows that it is basically linear and, thus, is well behaved.

For the weighting matrix, we use the optimal weighting matrix suggested by Gouriéroux and Monfort (1996) for simulated method of moments estimators. Because the weighting matrix depends upon our estimate of θ , we used a standard iterative procedure outlined in the next steps.

Step 4.—We make an initial guess of the weighting matrix \mathbf{W}^0 and solve for $\hat{\theta}^0$. Then, given this value we simulate the model to generate a new estimate of the weighting matrix.⁹ With the new estimate of the weighting matrix we then solve for a new $\hat{\theta}^1$. We perform this iterative procedure until our estimates of the weighting matrix and $\hat{\theta}$ converge. We explicitly consider simulation error because we utilize the weighting matrix suggested by Gouriéroux and Monfort (1996).

Step 5.—We compute standard errors using a bootstrap technique. We compute residuals implied by the estimator in (25) and the fitted values, we resample the residuals with replacement, and we generate a new set of data using the fitted values. Using the data constructed from each resampling b , we computed new estimates β_1^b and β_2^b .

For each bootstrap b , we replace the moments β_1 and β_2 with bootstrap-generated moments β_1^b and β_2^b . To account for simulation error, a new seed is set to generate a new set of model-generated moments. Defining $y^b(\theta)$ as the difference in moments for each b , as in (26), we solve for:

$$\hat{\theta}^b = \arg \min_{\theta} [y^b(\theta)' \mathbf{W} y^b(\theta)]. \quad (28)$$

We repeat this exercise 100 times and compute the estimated standard error of our estimate of $\hat{\theta}$ as:

$$\text{S.E.}(\hat{\theta}) = \left[\frac{1}{100} \sum_{b=1}^{100} (\hat{\theta}^b - \hat{\theta})(\hat{\theta}^b - \hat{\theta})' \right]^{\frac{1}{2}}. \quad (29)$$

This procedure for constructing standard errors is similar in spirit to the approach of Eaton, Kortum, and Kramarz (2011), who use a simulated method of moments estimator to estimate the parameters of a similar trade model from the performance of French exporters.

⁹The computation of this matrix is described in Gouriéroux and Monfort (1996).

5.4. Performance on Simulated Data

In this section, we evaluate the performance of our estimation approach using simulated data when we know the true value of θ .

Table 3 presents the results from the following exercise. We generate an artificial data set of trade flows and disaggregate prices with true value of θ equal to 8.28 and 4.00, and then we apply our estimation routine.¹⁰ We repeat this procedure 100 times. Table 3 reports average estimates. The sequence of artificial data is the same for both the overidentified case and exactly identified case to facilitate comparisons across estimators.

The first row presents the average value of our simulated method of moments estimate, which is 8.29 with a standard error of 0.03. For all practical purposes, the estimation routine recovers the true value of θ generating the data. To emphasize our estimator's performance, the next two rows of Table 3 present the approach of EK (which also corresponds to the moments used). Though not surprising given the discussion above, this approach generates estimates of θ that are significantly (in both their statistical and economic meaning) higher than the true value of θ of 8.28.

Table 3: Estimation Results With Artificial Data

Estimation Approach	True $\theta = 8.28$	True $\theta = 4.00$
Overidentified	Mean Estimate of θ (S.E.)	Mean Estimate of θ (S.E.)
SMM	8.29 (0.03)	3.99 (0.02)
Moment, β_1	12.47 (0.05)	6.03 (0.03)
Moment, β_2	15.20 (0.05)	7.34 (0.03)
Exactly Identified		
SMM	8.24 (0.04)	3.98 (0.02)
Moment, β_1	12.47 (0.05)	6.03 (0.03)

Note: In each simulation there are 19 countries, 150,000 goods and 100 simulations performed. The sequence of artificial data is the same for both the overidentified case and exactly identified case.

The final two rows present the exactly identified case when we use only one moment to estimate θ . In this case, we use β_1 . Similar to the overidentified case, the average value of our simulated method of moments estimate is 8.24 with a standard error of 0.04. Again, this is effectively the true value of θ .

¹⁰To generate the artificial data set, we employ the same simulation procedure described in Steps 1-3 in Section 5.2 using the trade data from EK.

Table 4: Comparison to Alternative Statistical Approaches to Bias Reduction

	True $\theta = 8.28$	True $\theta = 4.00$
Estimation Approach	Mean Estimate of θ (S.E.)	Mean Estimate of θ (S.E.)
SMM	8.29 (0.03)	3.99 (0.02)
Robson and Whitlock (1964)	10.54 (0.07)	5.11 (0.03)
Moment, β_1	12.47 (0.05)	6.03 (0.03)

Note: In each simulation there are 19 countries, 150,000 goods and 100 simulations performed. The sequence of artificial data is the same for all cases.

The second column reports the results when the true value of θ is set equal to 4.00. The estimates using our estimator are 3.99 and 3.98 in the overidentified and the exactly identified case, respectively. Similar to the previous results, these values are effectively the true value of θ

of the model has content because it outperforms a naive statistical procedure.

Overall, we view these results as evidence supporting our estimation approach and empirical estimates of θ presented in Section 6 below.

6. Empirical Results

In this section, we apply our estimation strategy described in section 5 to several different data sets. The key finding of this section is that our estimation approach yields an estimate around four, in contrast to previous estimation strategies, which yield estimates around eight.

6.1. Baseline Results Using New ICP 2005 Data

6.1.1. New ICP 2005 Data

Our sample contains 123 countries. We use trade flows and production data for the year 2004 to construct trade shares. The price data used to compute aggregate price indices and proxies for trade costs come from basic-heading-level data from the 2005 round of the International Comparison Programme (ICP). The ICP collects price data on goods with identical characteristics across retail locations in the participating countries during the 2003-2005 period.¹² The basic-heading level represents a narrowly-defined group of goods for which expenditure data are available. The data set contains a total of 129 basic headings, and we reduce the sample to 62 categories based on their correspondence with the trade data employed. Appendix A.2 provides more details.

On its own, this data set provides two contributions to the existing literature. First, because this is the latest round of the ICP, the measurement issues are less severe than in previous rounds. Furthermore, this data set provides very extensive coverage, as it includes as many as 123 developing and developed countries that account for 98 percent of world output.

The ICP provides a common list of “representative” goods whose prices are to be randomly sampled in each country over a certain period of time. A good is representative of a country if it comprises a significant share of a typical consumer’s bundle there. Thus, the ICP samples the prices of a common basket of goods across countries, where the goods have been pre-selected due to their highly informative content for the purpose of international comparisons.

¹²The ICP Methodological Handbook is available at <http://go.worldbank.org/MW520NNFK0>.

EK’s model gives a natural common basket of goods to be priced across countries. In this model, the agents in all countries consume all goods that lie within a fixed interval, $[0, 1]$. Thus, we consider this common list in the simulated model and randomly sample the prices of its goods across countries, in order to approximate trade barriers, much like it is done in the ICP data.

6.1.2. Results—New ICP 2005 Data

Table 5 presents the results.¹³ The first row simply reports the moments that our estimation procedure targets. As discussed, these values correspond with EK’s estimate of θ .

Table 5: Estimation Results With 2005 ICP Data

	Estimate of θ (S.E.)	β_1	β_2
Data Moments	—	7.75	9.61
Exactly Identified Case	4.12 (0.02)	7.75	—
Overidentified Case	4.06 (0.01)	7.65	9.62

The second row reports the results for exactly identified estimation, where the underlying moment used is β_1 . In this instance, our estimate of θ is 4.12, roughly half of EK’s estimate of θ .

The third row reports the results for the overidentified estimation. The estimate of θ is 4.06—almost the same as in our exactly identified estimation and, again, roughly half of EK’s estimate. The second and third columns report the resulting moments from the estimation routine, which are close to the data moments targeted, given that only one parameter is used to match two moments.

6.2. Estimates Using EK’s Data

In this section, we apply our estimation strategy to the same data used in EK as another
 chep(c)2k98539(618Td(o)3.97808(f)4-391.63(o)3.97502(u)0.751597(h)-28Td(e)-2.79977(s)2.42503(0)3.93724

to our data, the price data are at the basic-heading level and are for goods with identical characteristics across retail locations in the participating countries.

6.2.1. Results—EK’s Data

Table 6 presents the results.¹⁴ The first row simply reports the moments that our estimation procedure targets. The entry in the third column corresponds with β_2 , which is EK’s baseline estimate of θ .

Table 6: Estimation Results With EK’s Data

	Estimate of θ (S.E.)	β_1	β_2
Data Moments	—	5.93	8.28
Exactly Identified Case	3.93 (0.09)	5.93	—
Overidentified Case	4.42 (0.06)	6.64	8.10

The second row reports the results for exactly identified estimation, where the underlying moment used is β_1 . In this instance, our estimate of θ is 3.93, which is, again, roughly half of EK’s estimate of θ . The standard error of our estimate is fairly tight.

The third row reports the results for the overidentified estimation. Here, our estimate of θ is 4.42. Again, this is substantially below EK’s estimate. Unlike our results in Table 5 with

data, as in Bernard, Eaton, Jensen, and Kortum (2003) and Eaton, Kortum, and Kramarz (2011), are in the range of 3.6 to 4.8—exactly in the range of values we find. EK provide an alternative estimate of θ using wage data and find a value of 3.6. Burstein and Vogel (2009) estimate θ matching moments regarding the skill intensity of trade and find a value of five. Simonovska (2010) uses a non-homothetic model of trade featuring variable mark-ups and calibrates θ to a level of 3.8, which allows her model to match average mark-ups in OECD countries.

Donaldson (2009) estimates θ as well, and his approach is illuminating relative to the issues we have raised. His strategy for approximating trade costs is to study differences in the price of salt across locations in India. In principle, his approach is subject to our critique, as well—i.e., how could price differences in one good be informative about trade frictions? However, he argues convincingly that in India, salt was produced in only a few locations and exported everywhere. Thus, by examining salt, Donaldson (2009) finds a “binding” good. Using this approach, he finds estimates in the range of 3.8-5.2, again consistent with the range of our estimates of θ .

Finally, it should be noted that the elasticity of trade, θ , is closely related to the elasticity of substitution between foreign and domestic goods, the Armington elasticity, which determines the behavior between trade flows and relative prices across a large class of models. Ruhl (2008) presents a comprehensive discussion of the puzzle regarding this elasticity. In particular, he argues that international real business-cycle models need low elasticities, in the range of one to two, to match the quarterly fluctuations in trade balances and the terms of trade, but static applied general-equilibrium models need high elasticities, between ten and 15, to account for the growth in trade following trade liberalization. Recently, Imbs and Mejean (2010) estimate import and export price elasticities for 28 countries within a range of three to five. Moreover, using very disaggregate data, Feenstra, Obstfeld, and Russ (2010), Romalis (2007), Broda and Weinstein (2006), and Hummels (2001) provide estimates for the Armington elasticity parameter across a large number of industries. Feenstra, Obstfeld, and Russ’s (2010) median estimate is 4.4; Romalis’s (2007) estimates range between four and 13, Hummels’s (2001) estimates range between three and eight; while the most comprehensive work of Broda and Weinstein (2006), who provide tens of thousands of elasticities using ten-digit HS US data, results in a median value of 3.10.

Given our estimates of θ , it is straightforward to back out the Armington elasticity ρ within the context of the model of Anderson and van Wincoop (2004), where $\rho = \theta + 1$. Using our estimates of the elasticity of trade, the implied Armington elasticity ranges between 4.93 and 5.42. This utility parameter also appears in the heterogeneous firm framework of Melitz (2003) parameterized by Chaney (2008). Together with the elasticity of trade, θ , the utility

parameter governs the distribution of firm sales arising from the model, which has Pareto tails with a slope given by $\theta/(\rho - 1)$. Luttmer (2007) discusses firm-level evidence that this slope takes on the value of 1.65, which given our estimates of θ , provides the range of 3.38-3.68 for ρ . Hence, the Armington elasticity implied by our estimates ranges between 3.38 and 5.42, which falls within the low end of the ranges of estimates of existing studies. Thus, our results close the gap between (implied) estimates of the elasticity of trade stemming from a rich demand structure and the ones obtained from the general-equilibrium structure of a Ricardian model of trade.

7. Why Estimates of θ Matter: The Welfare Gains From Trade

The elasticity parameter θ is key in measuring the welfare gains from trade across a large class of models. In section 2.1, we argued that θ^{-1} represents the elasticity of welfare with respect to trade. Recall expression (6), reproduced below for convenience:

$$\log(P_n) = -\frac{1}{\theta} \log\left(\frac{X_{nn}}{X_n}\right)$$

Consider a trade liberalization episode that results in a one-percent fall in domestic expenditure share, generating $(1/\theta)/100$ percent increase in consumer welfare. Using the estimates for θ obtained from the original procedure and the improved simulated method of moments procedure, roughly eight and four, respectively, the welfare gains from trade would be mis-measured by a hundred percent. Namely, an estimate for θ of eight would generate a 0.125-percent welfare increase for a percent fall in the domestic share, while an estimate of four suggests a 0.25-percent welfare gain from trade, twice as high as the original calculation. These differences illustrate the importance of obtaining better estimates of trade elasticity.

8. Robustness

8.1. The Number of Goods

The estimation routine requires us to take a stand on the number of goods in the economy. We argue that the appropriate way to view this issue is to ask: how many goods are needed to numerically approximate the infinite number of goods in the model? Thus, the number of goods chosen should be judged on the accuracy of the approximation relative to the computational cost. The choice of the number of goods should not be judged on the basis of how many goods actually exist in the “real world” because this value is impossible to know or

discipline.

To understand our argument, recall that our estimation routine is based on a moment condition that compares a biased estimate from the data with a biased estimate using artificial data. In Section [3.4](#)

Table 7 also reports a side effect of using a low number of goods—zero trade flows between countries predicted by the model in places where we observe positive trade flows in the data. Table 7 reports the fraction of zeros that the model produces in instances where there are positive trade flows observed in the data. With only 5,000 goods, using the 2005 ICP data set, in almost half of the instances where trade flows are observed in the data, the model generates a zero. While not as severe, ten percent of positive trade flows are assigned zeros with the EK data. Results of this nature suggest increasing the number of goods to minimize the number of wrong zeros, as well.

8.2. Country-Specific Effects

The price data used in our estimation were collected at the retail level. As such, they necessarily reflect local (distribution) costs, sales taxes and mark-ups. These market frictions do not affect our estimates of the elasticity parameter, for as long as they are country- but not good-specific. The basic way to see this is to note that any country-specific effects will cancel out in the denominator of (13). This is another reason for using β as a moment in our estimation routine rather than some other moment.

8.3. Measurement Error

Measurement error in price data is a general concern in empirical work. In our estimation, error of this nature may artificially generate *larger* maximal price differences than implied by the underlying model. This would result in estimates of θ that are biased downwards. An advantage of our estimation approach is that one can potentially address this issue directly. For example, one can take a stand on the form of measurement error, introduce the simulated measurement error into the artificial data set, and potentially estimate it jointly with the trade elasticity. While we feel a formal treatment of this issue is beyond the scope of this paper, we did perform some Monte Carlo experiments with additive log-normal measurement error. We found that the magnitude of measurement error needed to affect our results was extreme.

8.4. Variable Mark-ups

The price data used in our estimation likely reflect retail mark-ups, which are not only country-, but also retailer-specific. In order to check whether such variable mark-ups affect our results, we make use of a richer price data set. In particular, we obtain price data from the EIU Worldwide Cost of Living Survey, which spans 77 of the original 123 countries

we consider. More importantly, the data are comprised of 111 tradable goods per country, and the price of each product is recorded once in a supermarket and once in a mid-price store. We repeat our exercise by first using the prices of items collected in mid-price stores, which appear to be cheaper on average, and then the prices found in supermarkets or chain stores. We postpone the results until section 8.5.1, since the level of detail in the EIU data allows us to also address aggregation bias, described there.

8.5. Aggregation

8.5.1. Data Approach

The basic-heading price data employed in our analysis are disaggregated; but, they are not at the individual-good level. For example, a price observation titled “rice” contains the average price across different types of rice sampled, such as basmati rice, wild rice, whole-grain rice, etc. Suppose that basmati rice is the binding good for a pair of countries. In the ICP data, we compute the difference between the average price of rice between the two countries, which is smaller than the price difference of basmati rice, if the remaining types of rice are more equally priced across the two countries. In this case, trade barriers are underestimated and, consequently, the elasticity of trade is biased upwards.¹⁷

In order to alleviate the aggregation problem, Table 8 presents estimates of the elasticity parameter using EIU’s good-level price data set, which spans a subset of 77 countries from our original data set, but provides prices for 111 individual tradable goods in two types of retail stores.¹⁸

The results in Table 8 suggest that aggregation causes a downward bias on trade-barrier estimates, resulting in trade-elasticity estimates that are biased upwards. Indeed, when we use the highly disaggregate EIU dataset, the elasticity of trade falls to 2.47-2.60. However, retail mark-ups do not seem to bias the estimates, since the elasticity of trade is not dramatically different whether high- or low-end store prices are used.

8.5.2. Model Approach

A more structural way to address aggregation bias is to view price data through the lenses of a monopolistic competition framework (ex. Melitz (2003) and Chaney (2008)). In these

¹⁷Our aggregation argument is different from the argument by Imbs and Mejean (2009), who demonstrate that imposing equal elasticities across disaggregated sectors of the economy results in lower elasticity of substitution estimates than ones obtained by allowing for heterogeneity.

¹⁸The results from the Step 1 gravity regressions are presented in Table 11 and Table 12.

Table 8: Estimation Results With EIU Data

	Estimate of θ (S.E.)	β_1	β_2
Cheap Stores			
Data Moments	—	4.17	5.11
Exactly Identified Case	2.47 (0.02)	4.17	—
Overidentified Case	2.48 (0.02)	4.19	5.09
Expensive Stores			
Data Moments	—	4.39	5.23
Exactly Identified Case	2.60 (0.02)	4.39	—
Overidentified Case	2.54 (0.02)	4.29	5.21

models, varieties produced by firms with identical productivity draws from different source countries can be thought of as varieties of a good produced with a particular productivity level. Then, a basic-heading price would represent the average price of all varieties produced by firms with a particular productivity draw originating from different source countries. Simonovska and Waugh (2011) explore the implications of the monopolistic competition micro-structure for estimates of the elasticity of trade.

9. Conclusion

In this paper, we estimate the elasticity of trade using a simulated method of moments estimator that exploits micro-price data. Our estimates of the elasticity of trade for 123 countries that comprise most of world output range from 2.47 to 4.42. These results imply a doubling in the measured welfare gains from trade, relative to existing estimates obtained following the approach of EK.

The analysis in our paper has broader implications than merely arriving at unbiased estimates of the elasticity of trade. Results from Arkolakis, Costinot, and Rodriguez-Clare (2011) suggest that heterogeneous firm and production models provide no value added for aggregate outcomes over models that abstract from heterogeneity. Our methodological approach suggests otherwise.

In this paper, we exploit the micro-level structure of EK's model to provide an estimate of the elasticity of trade, which is the key parameter to measuring the welfare gains from trade.

The important insight is that our approach to estimating this key parameter would not have been possible in models without heterogeneous outcomes. Thus, while the EK, Melitz (2003) and Chaney (2008) models may provide no new additional gains from trade, their structure allows us to provide a better estimate of the elasticity of trade than a simple Armington model would have allowed. The ability to use both measurement and theory in ways that alternative models would not allow is an important component of the value added that new heterogeneous firm and production models of international trade provide.

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A. Data Appendix

A.1. Trade Shares

To construct trade shares, we used bilateral trade flows and production data as follows:

$$\frac{X_{ni}}{X_n} = \frac{\text{Imports}_{ni}}{\text{Gross Mfg. Production}_n - \text{Exports}_n + \text{Imports}_n},$$

$$\frac{X_{nn}}{X_n} = 1 - \sum_{k \neq n}^N \frac{X_{ki}}{X_n}.$$

Putting the numerator and denominator together is simply computing an expenditure sh552Tf99.48010T

level. We then used concordance tables between four-digit SITC and three-digit ISIC codes provided by the UN and further modified by Muendler (2009).²⁰ We restrict our analysis to manufacturing bilateral trade flows only—namely, those that correspond with manufacturing as defined in ISIC Rev.#2.

The denominator is gross manufacturing production minus manufactured exports (for only the sample) plus manufactured imports (for only the sample). Gross manufacturing production data are the most serious data constraint we faced. We obtain manufacturing production data for 2004 from UNIDO for a large sub-sample of countries. We then imputed gross manufacturing production for countries for which data are unavailable as follows: We first obtain 2004 data on manufacturing (MVA) and agriculture (AVA) value added, as well as population size (L) and GDP for all countries in the sample. We then impute the gross output (GO) to manufacturing value added ratio for the missing countries using coefficients resulting from the following regression:

$$\log\left(\frac{MVA}{GO}\right) = \beta_0 + \beta_{GDP}C_{GDP} + \beta_L C_L + \beta_{MVA}C_{MVA} + \beta_{AVA}C_{AVA} + \epsilon,$$

where β_x is a 1x3 vector of coefficients corresponding to C_x , an $N \times 3$ matrix which contains $[\log(x), (\log(x))^2, (\log(x))^3]$ for the sub-sample of N countries for which gross output data are available.

A.2. Prices

The ICP price data we employ in our estimation procedure is reported at the basic-heading level. A basic heading represents a narrowly-defined group of goods for which expenditure data are available. For example, basic heading “1101111 Rice” is made up of prices of different types of rice, and the resulting value is an aggregate over these different types of rice. This implies that a typical price observation of “Rice” contains different types of rice, as well as different packaging options that affect the unit price of rice within and across countries.

According to the ICP Handbook, the price of the basic heading “Rice” is constructed using a transitive Jevons index of prices of different varieties of rice. To illustrate this point, suppose that the world economy consists of three countries, A , B , C and ten types of rice, 1-10. Further suppose that consumers in country A have access to all 10 types of rice; those in country B only have access to types 1-5 of rice; and those in country C have access to types

²⁰The trade data often report bilateral trade flows from two sources. For example, the exports of country A to country B can appear in the UN Comtrade data as exports reported by country A or as imports reported by country B . In this case, we take the report of bilateral trade flows between countries A and B that yields a higher total volume of trade across the sum of all SITC four-digit categories.

4-6 of rice. Although all types of rice are not found in all three countries, it is sufficient that each pair of countries shares at least one type of rice.

The ICP obtains unit prices for all available types of rice in all three countries and records a price of 0 if the type of rice is not available in a particular country. The relative price of rice between countries A and B , based on goods available in these two countries, $p_{AB}^{A,B}$, is a geometric average of the relative prices of rice of types 1-5

$$p_{AB}^{A,B} = \left[\prod_{j=1}^5 \frac{p_A(j)}{p_B(j)} \right]^{\frac{1}{5}}.$$

Similarly, one can compute the relative price of rice between countries A and C (B and C) based on varieties available in both A and C (B and C). The price of the basic heading "Rice" reported by the ICP is:

$$p_{AB} = \left[p_{AB}^{A,B} p_{AB}^{A,B} \frac{p_{AC}^{A,C}}{p_{BC}^{B,C}} \right]^{\frac{1}{3}},$$

which is a geometric average that features not only relative prices of rice between countries A and B , but also cross-prices between A and B linked via country C . This procedure ensures that prices of basic headings are transitive across countries and minimizes the impact of missing prices across countries.

Thus, a basic-heading price is a geometric average of prices of varieties that is directly comparable across countries.

B. Proofs

Below, we describe the steps to proving Lemmata 1 and 2. The key part in Lemma 1 is deriving the distribution of the maximal log price difference. We then prove Propositions 1 and 2.

B.1. Proof of Lemma 1, Lemma 2, and Proposition 1

First, we derive the distribution of the maximal log price difference. The key insight is to work with direct comparisons of goods' prices (i.e., do not impose equilibrium and work from the equilibrium price distribution) and to compute the distribution of log price differ-

ences and then the distribution of the maximal log price difference.

Having obtained the distribution of the maximum log price difference, we show that the expected value of the maximum log price difference is biased in a finite sample and the estimator $\hat{\beta}$ is biased.

B.1.1. Preliminaries

In deriving the distribution of maximum log price differences, we will work with a re-labeling of the production functions and exponential distributions following an argument in Alvarez and Lucas (2007). They relate the pdfs of the exponential and Frèchet distributions. The claim is that if $z_i \sim \exp(T_i)$, then $y_i \equiv z_i^{-\frac{1}{\theta}} \sim \exp(-T_i y^{-\theta})$.

Repeat the procedure for importer n in the numerator.

Given these definitions, (b.2) can be rewritten as:

$$(v_{ni}(z))^\theta = \frac{\min \{ \tilde{z}_n, w_i^\theta \tau_{ni}^\theta z_i \}}{\min \{ \tilde{z}_i, w_n^\theta \tau_{in}^\theta z_n \}} \quad (\text{b.3})$$

Define $\epsilon_{ni}(z) = \log(v_{ni}(z))$. Taking logs of expression (b.3) gives:

$$\begin{aligned} \theta \epsilon_{ni}(z) = & \min \{ \log(\tilde{z}_n), [\theta \log(w_i) + \theta \log(\tau_{ni}) + \log(z_i)] \} \\ & - \min \{ \log(\tilde{z}_i), [\theta \log(w_n) + \theta \log(\tau_{in}) + \log(z_n)] \} \end{aligned} \quad (\text{b.4})$$

Next, we argue that $\theta \epsilon_{ni}(z) \in [-\theta \log(\tau_{in}), \theta \log(\tau_{ni})]$. For any good z , $\theta \epsilon_{ni}(z)$ can satisfy one and only one of the following three cases:

1. Countries n and i buy good z from two different sources. Then,

$$\theta \epsilon_{ni}(z) = \log(\tilde{z}_n) - \log(\tilde{z}_i) \quad (\text{b.5})$$

2. Country n buys good z from country i . Assuming that trade barriers don't violate the triangle inequality, it must be that i buys the good from itself. Then,

$$\theta \epsilon_{ni}(z) = \theta \log(w_i) + \theta \log(\tau_{ni}) + \log(z_i) - \theta \log(w_i) - \log(z_i) = \theta \log(\tau_{ni}) \quad (\text{b.6})$$

3. Country i buys good z from n . Then it must be that n buys the good from itself, so:

$$\theta \epsilon_{ni}(z) = \theta \log(w_n) + \log(z_n) - \theta \log(w_n) - \theta \log(\tau_{in}) - \log(z_n) = -\theta \log(\tau_{in}) \quad (\text{b.7})$$

We claim that the following ordering occurs: $-\theta \log(\tau_{in}) \leq \log(\tilde{z}_n) - \log(\tilde{z}_i) \leq \theta \log(\tau_{ni})$. To show this, we need to consider the following two scenarios:

1. Countries n and i buy good z from the same source k . Then,

$$\begin{aligned} \log(\tilde{z}_n) - \log(\tilde{z}_i) &= \log(w_k^\theta \tau_{nk}^\theta z_k) - \log(w_k^\theta \tau_{ik}^\theta z_k) \\ &= \theta(\log(\tau_{nk}) - \log(\tau_{ik})) \end{aligned} \quad (\text{b.8})$$

Clearly,

$$\theta(\log(\tau_{nk}) - \log(\tau_{ik})) \geq -\theta \log(\tau_{in}) \iff \tau_{in} \tau_{nk} \geq \tau_{ik},$$

where the latter inequality is true under the triangle inequality assumption.

Similarly,

$$\theta(\log(\tau_{nk}) - \log(\tau_{ik})) \leq \theta \log(\tau_{ni}) \iff \tau_{nk} \leq \tau_{ni}\tau_{ik},$$

again true by triangle inequality.

2. Country n buys good z from source a and country i from source b , $a \neq b$. We want to show that $-\theta \log(\tau_{in}) \leq \log(w_a^\theta \tau_{na}^\theta z_a) - \log(w_b^\theta \tau_{ib}^\theta z_b) \leq \theta \log(\tau_{ni})$.

Since n imported from a over b , it must be that:

$$w_a^\theta \tau_{na}^\theta z_a \leq w_b^\theta \tau_{nb}^\theta z_b \tag{b.9}$$

Similarly, since i imported from b over a , it must be that:

$$w_b^\theta \tau_{ib}^\theta z_b \leq w_a^\theta \tau_{ia}^\theta z_a \tag{b.10}$$

To find the upper bound, take logs of (b.9) and subtract $\log(w_b^\theta \tau_{ib}^\theta z_b)$ from both sides:

$$\log(w_a^\theta \tau_{na}^\theta z_a) - \log(w_b^\theta \tau_{ib}^\theta z_b) \leq \log(w_b^\theta \tau_{nb}^\theta z_b) - \log(w_b^\theta \tau_{ib}^\theta z_b) \tag{b.11}$$

It suffices to show that the right-hand side is itself below the upper bound since, by transitivity, so is the left-hand side (which is the object of interest).

$$\begin{aligned} \log(w_b^\theta \tau_{nb}^\theta z_b) - \log(w_b^\theta \tau_{ib}^\theta z_b) &\leq \theta \log(\tau_{ni}) \\ \iff \theta \log(\tau_{nb}) - \theta \log(\tau_{ib}) &\leq \theta \log(\tau_{ni}) \\ \iff \tau_{nb} &\leq \tau_{ni}\tau_{ib}, \end{aligned} \tag{b.12}$$

which is true by triangle inequality.

The argument for the lower bound is similar. Take logs of (b.10), multiply by -1 (and reverse inequality) and add $\log(w_a^\theta \tau_{na}^\theta z_a)$ to both sides:

$$\log(w_a^\theta \tau_{na}^\theta z_a) - \log(w_b^\theta \tau_{ib}^\theta z_b) \geq \log(w_a^\theta \tau_{na}^\theta z_a) - \log(w_a^\theta \tau_{ia}^\theta z_a) \tag{b.13}$$

It suffices to show that the right-hand side is itself above the lower bound since, by

transitivity, so is the left-hand side (which is the object of interest).

$$\begin{aligned}
& \log(w_a^\theta \tau_{na}^\theta z_a) - \log(w_a^\theta \tau_{ia}^\theta z_a) \geq -\theta \log(\tau_{in}) \\
\iff & \theta \log(\tau_{na}) - \theta \log(\tau_{ia}) \geq -\theta \log(\tau_{in}) \\
\iff & \tau_{in} \tau_{na} \geq \tau_{ia},
\end{aligned} \tag{b.14}$$

which is true by triangle inequality.

Hence, $\theta \epsilon_{ni}(z) \in [-\theta \log(\tau_{in}), \theta \log(\tau_{ni})]$.

Next, we proceed to derive the distribution of $\theta \epsilon_{ni}(z) = \log(\tilde{z}_n) - \log(\tilde{z}_i)$. First, we derive the pdfs of its two components.

Let $y_i \equiv \log(\tilde{z}_i)$. Then $\tilde{z}_i = \exp(y_i)$. The pdf of y_i must satisfy:

$$\begin{aligned}
f(y_i) dy_i = g(\tilde{z}_i) d\tilde{z}_i & \Rightarrow f(y_i) = \tilde{\lambda}_i \exp(-\tilde{\lambda}_i \tilde{z}_i) \frac{d\tilde{z}_i}{dy_i} \\
& \Rightarrow f(y_i) = \tilde{\lambda}_i \exp(-\tilde{\lambda}_i \exp(y_i)) \exp(y_i) \\
& \Rightarrow F(y_i) = 1 - \exp(-\tilde{\lambda}_i \exp(y_i))
\end{aligned} \tag{b.15}$$

The same holds for n .

Now that we have the pdf's of the two components, we can define the pdf of $\epsilon \equiv \theta \epsilon_{ni}(z) \in [-\theta \log(\tau_{in}), \theta \log(\tau_{ni})]$ as follows:

$$f(\epsilon) \equiv f_{y_n - y_i}(x) = \int_{-\infty}^{\infty} f_{y_n}(y) f_{y_i}(y - x) dy, \tag{b.16}$$

where we have used the fact that y_n and y_i are independently distributed hence, the pdf of their difference is the convolution of the pdfs of the two random variables.

Substituting the pdfs of y_n and y_i into (b.16) yields:

$$\begin{aligned}
f(\epsilon) &= \int_{-\infty}^{\infty} \tilde{\lambda}_n \exp(-\tilde{\lambda}_n \exp(y)) \exp(y) \tilde{\lambda}_i \exp(-\tilde{\lambda}_i \exp(y - \epsilon)) \exp(y - \epsilon) dy \\
&= \frac{-\tilde{\lambda}_n \tilde{\lambda}_i}{(\tilde{\lambda}_n \exp(\epsilon) + \tilde{\lambda}_i)^2} \left[\frac{\tilde{\lambda}_n \exp(y + \epsilon) + \tilde{\lambda}_i \exp(y) + \exp(\epsilon)}{\exp \left\{ \exp(y) (\tilde{\lambda}_n + \tilde{\lambda}_i \exp(-\epsilon)) \right\}} \right]_{y=-\infty}^{y=+\infty}
\end{aligned} \tag{b.17}$$

Let $v(y)$ be the expression in the bracket.

$$\lim_{y \rightarrow -\infty} v(y) = \frac{0 + 0 + \exp(\epsilon)}{\exp \{0\}} = \exp(\epsilon) \tag{b.18}$$

For the upper bound, we use l'Hopital rule:

$$\begin{aligned}
\lim_{y \rightarrow \infty} v(y) &= \lim_{y \rightarrow \infty} \frac{\tilde{\lambda}_n \exp(y + \epsilon) + \tilde{\lambda}_i \exp(y)}{\exp \left\{ \exp(y) (\tilde{\lambda}_n + \tilde{\lambda}_i \exp(-\epsilon)) \right\} \exp(y) (\tilde{\lambda}_n + \tilde{\lambda}_i \exp(-\epsilon))} \\
&= \lim_{y \rightarrow \infty} \frac{\tilde{\lambda}_n \exp(\epsilon) + \tilde{\lambda}_i}{\exp \left\{ \exp(y) (\tilde{\lambda}_n + \tilde{\lambda}_i \exp(-\epsilon)) \right\} (\tilde{\lambda}_n + \tilde{\lambda}_i \exp(-\epsilon))} \\
&= 0
\end{aligned} \tag{b.19}$$

Thus, (b.17) becomes:

$$f(\epsilon) = \frac{\tilde{\lambda}_n \tilde{\lambda}_i \exp(\epsilon)}{(\tilde{\lambda}_n \exp(\epsilon) + \tilde{\lambda}_i)^2} \tag{b.20}$$

The corresponding cdf is:

$$F(\epsilon) = 1 - \frac{\tilde{\lambda}_i}{\tilde{\lambda}_n \exp(\epsilon) + \tilde{\lambda}_i} \tag{b.21}$$

Given that ϵ is bounded, we can compute the truncated pdf as:

$$\begin{aligned}
f_T(\epsilon) &= \frac{f(\epsilon)}{F(\theta \log(\tau_{ni})) - F(-\theta \log(\tau_{in}))} \\
&= \gamma^{-1} \frac{\tilde{\lambda}_n \tilde{\lambda}_i \exp(\epsilon)}{(\tilde{\lambda}_n \exp(\epsilon) + \tilde{\lambda}_i)^2},
\end{aligned} \tag{b.22}$$

where:

$$\gamma = -\frac{\tilde{\lambda}_i}{\tilde{\lambda}_n \exp(\theta \log(\tau_{ni})) + \tilde{\lambda}_i} + \frac{\tilde{\lambda}_i}{\tilde{\lambda}_n \exp(-\theta \log(\tau_{in})) + \tilde{\lambda}_i} \tag{b.23}$$

Similarly, the truncated cdf is:

$$F_T(\epsilon) = \gamma^{-1} \int_{-\theta \log(\tau_{in})}^{\epsilon} f(t) dt \tag{b.24}$$

Now that we have these distributions, we compute order statistics from them, which allow us to characterize the trade barriers estimated from price data. We use the following result: Given L observations drawn from pdf $h(x)$, the pdf of the r -th order statistic (where $r = L$

is the max and $r = 1$ is the min) is:

$$h_r(x) = \frac{L!}{(r-1)!(L-r)!} H(x)^{r-1} (1-x)^{L-r}$$

Finally, one can rewrite equation (b.30) via integration by parts as:

$$E[\max_{z \in L}(\log(p_n(z)) - \log(p_i(z)))] = \log \tau_{ni} - \frac{1}{\theta} \int_{-\theta \log(\tau_{in})}^{\theta \log(\tau_{ni})} F_{\max}(\epsilon, L) d\epsilon \quad (\text{b.31})$$

$$\log \tau_{ni} = E[\max_{z \in L}(\log(p_n(z)) - \log(p_i(z)))] + \frac{1}{\theta} \int_{-\theta \log(\tau_{in})}^{\theta \log(\tau_{ni})} F_{\max}(\epsilon, L) d\epsilon, \quad (\text{b.32})$$

which implies the following strict inequality:

$$\log \tau_{ni} > E[\max_{z \in L}(\log(p_n(z)) - \log(p_i(z)))] = \Psi_{ni}(L; \mathbf{S}, \tilde{\tau}_i, \tilde{\tau}_n), \quad (\text{b.33})$$

where the strict inequality simply follows from the inspection of the CDF $F_{\max}(\epsilon, L)$ which has positive mass below the point $\theta \log(\tau_{ni})$. This then proves claim 1. in Lemma 1.

To prove claim 2. in Lemma 1, we compute the difference in the expected values of log prices between two countries. We show that they are equal to the (scaled) difference in the price parameters Φ .

Rather than working with the distribution described above, it is more convenient to directly compute the expectation of log prices using the equilibrium price distribution. Note that EK show that the cdf and pdf of prices in country i are $G(p) = 1 - \exp(-\Phi_i p^\theta)$ and $g(p) = p^{\theta-1} \theta \Phi_i \exp(-\Phi_i p^\theta)$, respectively.

For any country i , define the expectation of logged prices as

$$E[\log(p_i(z))] = \int_0^\infty \log(p) g(p) dp \quad (\text{b.34})$$

Substituting the pdf of prices and then utilizing some algebra to find an appropriate change in variables, expression (b.34) yields

$$E[\log(p_i(z))] = \int \log(p / \mathbf{p})$$

change of variables allows us to rewrite the above as

$$\begin{aligned} E[\log(p_i(z))] &= \int_0^\infty \log(p) \theta \Phi_i \exp(\theta \log(p)) \exp(-\Phi_i \exp(\theta \log(p))) \frac{dp}{p} \\ &= \int_0^\infty x \theta \Phi_i \exp(\theta x) \exp(-\Phi_i \exp(\theta x)) \frac{\theta}{\theta} dx \end{aligned}$$

Let $y = \theta x$, so that $dy/dx = \theta$; then, another change of variables gives

$$E[\log(p_i(z))] = \frac{1}{\theta} \int_0^\infty y \Phi_i \exp(y) \exp(-\Phi_i \exp(y)) dy$$

Let $t = \Phi_i \exp(y)$, so that $dt/dy = \Phi_i \exp(y)$ and $y = \log(t/\Phi_i)$. Then,

$$\begin{aligned} E[\log(p_i(z))] &= \frac{1}{\theta} \int_0^\infty \log\left(\frac{t}{\Phi_i}\right) \exp(-t) dt \\ &= \frac{1}{\theta} \left\{ \int_0^\infty \log(t) \exp(-t) dt - \int_0^\infty \log(\Phi_i) \exp(-t) dt \right\} \\ &= -\frac{1}{\theta} \{\gamma + \log(\Phi_i)\}, \end{aligned} \tag{b.35}$$

where γ is the Euler-Mascheroni constant. Finally, using (b.35) and taking the expected difference in log prices between country n and country i , the scaled Euler-Mascheroni constant cancels between the two countries and leaves the following expression

$$\begin{aligned} E[\log(p_n(z))] - E[\log(p_i(z))] &= -\frac{1}{\theta} \{\log(\Phi_n) - \log(\Phi_i)\} \\ &\equiv \Omega_{ni}(\mathbf{S}, \tilde{\tau}_n, \tilde{\tau}_i), \end{aligned} \tag{b.36}$$

which then proves claim 2. in Lemma 1.

B.1.3. Proof of Lemma 2 and Proposition 1

To prove Lemma 2 and Proposition 1, we invert EK's estimator for the elasticity of trade:

$$\frac{1}{\hat{\beta}} = -\frac{\sum_n \sum_i \left(\log \hat{\tau}_{ni} + \log \hat{P}_i - \log \hat{P}_n \right)}{\sum_n \sum_i \log \left(\frac{X_{ni}/X_n}{X_{ii}/X_i} \right)} \tag{b.37}$$

Given the assumption that the trade data are fixed, equation (b.37) is linear in the random variables $\log \hat{\tau}_{ni}$ and $(\log \hat{P}_n - \log \hat{P}_i)$. With this observation, taking expectations of these

random variables yields

$$E\left(\frac{1}{\hat{\beta}}\right) = \frac{1}{\theta} \left\{ -\frac{\sum_n \sum_i (\theta \Psi_{ni}(L) - (\log \Phi_i - \log \Phi_n))}{\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)} \right\} < \frac{1}{\theta}, \quad (\text{b.38})$$

by substituting in for the expectation of the maximum log price difference using (b.30), and the difference in expectations of log prices using (b.36). Inspection of the bracketed term above implies that the following strict inequality must hold,

$$1 > \left\{ -\frac{\sum_n \sum_i (\theta \Psi_{ni}(L) - (\log \Phi_i - \log \Phi_n))}{\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)} \right\} > 0, \quad (\text{b.39})$$

with the reason being that $\Psi_{ni}(L) < \log \tau_{ni}$ from Lemma 1; otherwise, the bracketed term would correspond exactly with equation (5) in logs and, thus, equal one. Now, inverting the expression above and applying Jensen's inequality results in the following:

$$E(\hat{\beta}) \geq \left[E\left(\frac{1}{\hat{\beta}}\right) \right]^{-1} = \theta \left\{ -\frac{\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)}{\sum_n \sum_i (\theta \Psi_{ni}(L) - (\log \Phi_i - \log \Phi_n))} \right\} > \theta, \quad (\text{b.40})$$

with the strict inequality following from (b.38) and (b.39). This proves Proposition 1.

B.2. Proof of Proposition 2

In this subsection, we prove Proposition 2. To prove the claims in Proposition 2, we start with claim 1.

To prove claim 1., we argue that the sample maximum of scaled log price differences is a consistent estimator of the scaled trade cost. In particular, we argue that as the sample size becomes infinite, the probability that the sample scaled trade cost is arbitrarily close to the true scaled trade cost is one.

To see this, consider an estimate of the scaled trade barrier, given a sample of L goods' prices,

$$\theta \log \hat{\tau}_{ni}^L = \theta \left\{ \max_{\ell=1, \dots, L} (\log p_n(\ell) - \log p_i(\ell)) \right\}. \quad (\text{b.41})$$

The cdf of this random variable is the integral of its pdf, which is given in expression (b.28), over the compact interval in which the scaled logged price difference lies, $[-\theta \log \tau_{in}, \theta \log \tau_{ni}]$.

Denote this cdf by F_{max}^L . From (b.28), $F_{max}^L \equiv (F_T)^L$, where F_T is the truncated distribution of the scaled log price difference over the domain $[-\theta \log \tau_{in}, \theta \log \tau_{ni}]$. By definition, F_T and F_{max}^L take on values between zero and one, as they are cdfs. In particular, for any realization $x < \theta \log \tau_{ni}$, $F_T(x) < 1$. For any $L > 1$, $F_{max}^L(x) = (F_T(x))^L \leq F_T(x) < 1$.

We refer the reader to Davidson and MacKinnon (2004) for a proof of the well known result that the sample average is both an unbiased and consistent estimator of the mean. Since the difference operator is continuous, the difference in the sample average of logged price is an unbiased and consistent estimator of the difference in mean logged prices. Finally, multiplying these sample averages by a scalar θ , a continuous operation, ensures convergence to true difference in the price terms Φ .

We have argued that the two components in the numerator converge in probability to their true parameter counterparts, as the sample size becomes infinite. Taking the difference of these two components, summing over all country pairs (n, i) , and dividing by the scalar $\left[-\sum_n \sum_i \log\left(\frac{X_{ni}/X_n}{X_{ii}/X_i}\right)\right]$, all of which are continuous operations, allows us to conclude that

$$\text{plim}_{L \rightarrow \infty} \sum_n \sum_i \left(\theta \log \hat{\tau}_{ni}^L - \theta [\log \hat{P}_n - i X_{ni} \tau_{ni}] \right)$$

inL

B.3. Deriving the Inverse Marginal Cost Distribution

To simulate the model, we argue that by using the coefficients \mathbf{S} estimated from the gravity regression (22), we have enough information to simulate prices and trade flows. The key insight is that the S 's are sufficient to characterize the inverse marginal cost distribution. Thus, we can sample from this distribution and then compute equilibrium prices and trade flows.

To see this argument, let $z_i \sim F_i(z_i) = \exp(-T_i z_i^{-\theta})$ and define $u_i \equiv z_i/w_i$. The pdf of z_i is $f_i(z_i) = \exp(-T_i z_i^{-\theta}) \theta T_i z_i^{-\theta-1}$. To find the pdf of the transformation u_i , $m_i(u_i)$, use the fact that $f_i(z_i) dz_i = m_i(u_i) du_i$, or $m_i(u_i) = f_i(z_i) (du_i/dz_i)^{-1}$. Let $\tilde{S}_i = T_i w_i^{-\theta}$. Using $f_i(z_i)$, \tilde{S}_i , and the fact that $du_i/dz_i = 1/w_i$, we obtain:

$$\begin{aligned}
 m_i(u_i) &= f_i(z_i) \left(\frac{du_i}{dz_i} \right)^{-1} = \exp(-T_i z_i^{-\theta}) \theta T_i z_i^{-\theta-1} \left(\frac{1}{w_i} \right)^{-1} \\
 &= \exp \left(-T_i z_i^{-\theta} \frac{w_i^{-\theta}}{w_i^{-\theta}} \right) \theta T_i z_i^{-\theta-1} \left(\frac{1}{w_i} \right)^{-1} \frac{w_i^{-\theta}}{w_i^{-\theta}} \\
 &= \exp \left(-\tilde{S}_i \frac{z_i^{-\theta}}{w_i^{-\theta}} \right) \theta \tilde{S}_i \frac{z_i^{-\theta-1}}{w_i^{-\theta-1}} \\
 &= \exp \left(-\tilde{S}_i u_i^{-\theta} \right) \theta \tilde{S}_i u_i^{-\theta-1}
 \end{aligned}$$

Clearly $m_i(u_i)$ is the pdf that corresponds to the cdf $M_i(u_i) = \exp(-\tilde{S}_i u_i^{-\theta})$, which concludes the argument.

Table 9: 2005 ICP Data, Step 1 Country-Specific Estimates

Country	\hat{S}_i	S.E.	ex_i	S.E.	Country	\hat{S}_i	S.E.	ex_i	S.E.	Country	\hat{S}_i	S.E.	ex_i	S.E.
Angola	-1.04	0.21	-2.67	0.35	Fiji	-0.58	0.20	-2.06	0.31	Nepal	0.48	0.24	-3.00	0.32
Argentina	1.13	0.18	2.34	0.25	Finland	1.09	0.17	2.15	0.23	New Zealand	-0.25	0.30	3.17	0.24
Armenia	0.83	0.20	-3.91	0.29	France	0.39	0.16	5.09	0.22	Nigeria	-0.85	0.25	-1.00	0.29
Australia	0.24	0.16	3.59	0.23	Gabon	-1.07	0.18	-1.52	0.27	Norway	0.33	0.37	1.88	0.23
Austria	0.39	0.16	2.71	0.22	Gambia, The	-2.40	0.22	-2.32	0.34	Oman	-0.19	0.36	-0.74	0.26
Azerbaijan	-0.03	0.20	-2.76	0.28	Georgia	-2.78	0.19	0.70	0.27	Pakistan	0.55	0.29	2.03	0.23
Bangladesh	0.76	0.18	0.46	0.24	Germany	0.40	0.16	5.57	0.22	Paraguay	0.04	0.36	-0.74	0.28
Belarus	1.27	0.18	-0.98	0.25	Ghana	-1.32	0.21	0.44	0.29	Peru	0.47	0.24	1.10	0.25
Belgium	-2.75	0.16	8.26	0.22	Greece	0.78	0.16	0.58	0.23	Philippines	-0.34	0.39	2.64	0.24
Benin	-0.62	0.22	-3.66	0.36	Guinea	-1.76	0.22	-2.16	0.33	Poland	0.84	0.34	1.76	0.23
Bhutan	0.37	0.30	-5.45	0.43	Guinea-Bissau	-0.40	0.28	-5.77	0.48	Portugal	-0.20	0.24	2.71	0.23
Bolivia	0.28	0.19	-1.65	0.29	Hungary	0.86	0.17	0.98	0.23	Romania	0.60	0.25	0.75	0.23
Bosnia and Herzegovina	1.14	0.23	-3.68	0.32	Iceland	-0.26	0.18	-0.55	0.26	Russian Federation	1.32	0.34	2.12	0.23
Botswana	0.97	0.25	-3.73	0.37	India	0.94	0.16	3.53	0.25	Rwanda	0.09	0.27	-5.05	0.36
Brazil	1.30	0.16	3.67	0.23	Indonesia	1.34	0.16	3.07	0.23	Sierra Leone	-0.97	0.25	-3.61	0.41
Brunei Darussalam	1.68	0.25	-5.15	0.37	Iran, Islamic Rep.	1.02	0.21	-0.85	0.28	Saudi Arabia	0.70	0.30	0.70	0.28
Bulgaria	0.30	0.17	0.39	0.24	Ireland	-3.21	0.16	6.39	0.22	Senegal	-0.86	0.27	-0.63	0.25
Burkina Faso	0.32	0.20	-4.07	0.31	Israel	0.59	0.17	1.70	0.24	Slovak Republic	-0.31	0.26	1.34	0.23
Burundi	-1.52	0.20	-3.12	0.34	Italy	0.58	0.16	4.56	0.22	Slovenia	1.02	0.38	-0.20	0.24
Cameroon	1.54	0.21	-3.34	0.30	Japan	1.51	0.16	4.89	0.23	South Africa	0.41	0.25	3.61	0.23
Canada	-0.27	0.16	4.59	0.22	Jordan	-0.25	0.18	-0.65	0.25	Spain	0.29	0.31	4.09	0.22
Cape Verde	-0.37	0.21	-4.86	0.38	Kazakhstan	0.28	0.18	-0.03	0.26	Sri Lanka	-0.14	0.42	0.65	0.25
Central African Republic	0.55	0.25	-4.67	0.36	Kenya	-0.53	0.16	-0.07	0.23	Sudan	-0.12	0.33	-3.47	0.32
Chad	0.54	0.24	-6.49	0.40	Korea, Rep.	1.04	0.16	4.38	0.22	Swaziland	2.10	0.38	-3.30	0.33
Chile	0.27	0.18	1.96	0.25	Kyrgyz Republic	0.03	0.20	-2.86	0.30	Sweden	0.75	0.31	3.34	0.22
China	1.13	0.16	5.74	0.23	Lao PDR	1.43	0.27	-3.92	0.35	Switzerland	0.10	0.25	3.69	0.27
Colombia	0.38	0.17	0.50	0.24	Latvia	-0.46	0.19	-0.10	0.26	Syrian Arab Republic	-0.34	0.31	-0.86	0.26
Comoros	-0.84	0.27	-4.54	0.42	Lebanon	0.60	0.20	-2.29	0.28	Tajikistan	1.10	0.37	-3.19	0.34
Congo, Dem. Rep.	-0.65	0.24	-2.31	0.34	Lesotho	1.09	0.30	-5.44	0.44	Tanzania	-1.01	0.26	-1.41	0.31
Congo, Rep.	-0.95	0.21	-1.08	0.30	Lithuania	0.67	0.21	-0.88	0.29	Thailand	0.86	0.29	3.57	0.28
Cte d'Ivoire	0.78	0.21	-1.22	0.30	Macedonia, FYR	0.41	0.18	-2.71	0.27	Togo	-1.40	0.25	-1.34	0.27
Croatia	1.08	0.16	-1.29	0.24	Malawi	-0.63	0.19	-2.59	0.28	Tunisia	0.34	0.36	-0.30	0.24
Cyprus	-0.86	0.17	0.45	0.24	Malaysia	-1.43	0.16	6.58	0.22	Turkey	0.93	0.28	2.38	0.23
Czech Republic	0.43	0.16	2.02	0.23	Mali	-1.03	0.23	-2.66	0.32	Uganda	-0.71	0.29	-2.30	0.26
Denmark	-0.24	0.16	3.63	0.23	Mauritania	-1.97	0.23	-1.79	0.33	Ukraine	1.41	0.24	0.88	0.28
Djibouti	-2.04	0.24	-2.37	0.38	Mauritius	-1.63	0.17	1.44	0.24	United Kingdom	-0.29	0.32	5.59	0.22
Ecuador	-0.24	0.18	0.12	0.26	Mexico	0.21	0.16	2.61	0.24	United States	0.06	0.34	6.87	0.22
Egypt, Arab Rep.	0.44	0.17	0.62	0.23	Moldova	-0.47	0.19	-2.12	0.29	Uruguay	-0.51	0.29	1.40	0.27
Equatorial Guinea	0.47	0.24	-4.24	0.39	Morocco	-0.39	0.17	1.32	0.23	Venezuela, RB	0.72	0.29	-0.60	0.26
Estonia	-1.74	0.17	1.61	0.24	Mozambique	-0.16	0.22	-2.06	0.33	Vietnam	-0.44	0.24	2.69	0.28
Ethiopia	-0.66	0.21	-2.15	0.31	Namibia	1.09	0.23	-3.64	0.33	Zambia	-3.99	0.30	2.59	0.27

Table 10: EK Data, Step 1 Country-Specific Estimates

Country	\hat{S}_i	S.E.	ex_i	S.E.	Country	\hat{S}_i	S.E.	ex_i	S.E.
Australia	-0.20	0.15	0.54	0.24	Japan	2.54	0.13	1.74	0.21
Austria	0.50	0.12	-1.65	0.18	Netherlands	-3.09	0.12	0.80	0.18
Belgium	-4.38	0.12	0.98	0.18	New Zealand	-1.42	0.15	0.37	0.24
Canada	-0.46	0.13	1.06	0.22	Norway	-0.34	0.12	-1.01	0.18
Denmark	-1.16	0.12	-0.67	0.18	Portugal	-0.28	0.12	-1.38	0.19
Finland	0.82	0.12	-1.33	0.18	Spain	1.56	0.12	-1.35	0.18
France	1.15	0.12	0.05	0.18	Sweden	0.05	0.12	-0.06	0.18
Germany	1.44	0.12	0.82	0.18	United Kingdom	0.52	0.12	0.89	0.18
Greece	-0.38	0.12	-2.51	0.18	United States	1.34	0.13	2.83	0.22
Italy	1.81	0.12	-0.12	0.18					

Table 10: EIU Data, Step 1 Country-Specific Estimates

Country	\hat{S}_i	S.E.	ex_i	S.E.	Country	\hat{S}_i	S.E.	ex_i	S.E.	Country	\hat{S}_i	S.E.	ex_i	S.E.
Argentina	0.71	0.17	0.74	0.24	Iceland	-0.06	0.17	-3.09	0.24	Poland	0.56	0.16	0.26	0.23
Australia	-0.23	0.16	2.19	0.24	India	0.54	0.16	1.76	0.24	Portugal	-0.03	0.16	0.31	0.23
Austria	0.11	0.16	1.31	0.23	Indonesia	1.01	0.16	1.39	0.23	Romania	0.13	0.16	-0.42	0.23
Azerbaijan	0.06	0.17	-5.28	0.25	Iran, Islamic Rep.	0.75	0.18	-2.71	0.26	Russian Federation	1.17	0.16	0.55	0.24
Belgium	-2.79	0.16	6.16	0.23	Ireland	-3.13	0.16	4.65	0.23	Saudi Arabia	0.22	0.18	-0.59	0.26
Brazil	0.59	0.16	2.33	0.23	Israel	0.08	0.17	0.37	0.24	Senegal	-0.70	0.17	-3.76	0.25
Brunei Darussalam	1.59	0.21	-7.49	0.32	Italy	0.35	0.16	2.93	0.23	Slovak Republic	-0.45	16 .31 0	0.23	

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Table 12: Step 1 Trade Cost Estimates and Summary Statistics

Geographic Barriers	ICP 2005 Data		EK Data		EIU Data	
	Parameter Estimate	S.E.	Parameter Estimate	S.E.	Parameter Estimate	S.E.
[0, 375)	- 5.30	0.21	-2.89	0.14	-5.02	0.19
[375, 750)	- 6.29	0.14	-3.56	0.10	-5.28	0.11
[750, 1500)	- 7.27	0.09	-3.87	0.07	-5.71	0.07
[1500, 3000)	- 8.50	0.06	-4.10	0.15	-6.63	0.05
[3000, 6000)	- 9.65	0.04	-6.15	0.09	-7.70	0.04
[6000, maximum]	-10.35	0.05	-6.60	0.10	-8.41	0.04
Shared border	1.25	0.12	0.44	0.14	1.04	0.16
Summary Statistics						
	ICP 2005 Data		EK Data		EIU Data	
No. Obs	10, 513		342		4, 607	
TSS	152, 660		2, 936		47, 110	
SSR	30, 054		76.56		8, 208	
σ_v^2	2.93		0.25		1.84	