

# Labor Market Imperfect Information, On-the-job Training and the Employer Size-Wage Effect

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## Abstract

Using NLSY79 data, we find that large firms pay more to workers and train a higher proportion of their workforce. In addition, wage premiums associated with large employers are lower for trained workers than for untrained ones. Existing theories can not explain these empirical findings simultaneously. We then develop a two-period model of imperfect information that can reconcile all three stylized facts.

Keywords: size-wage premium, imperfect information, On-the-job Training.

JEL classification codes: D83; J31.

## 1 Introduction

Large firms pay more on average to workers of similar characteristics than small firms. Studies have shown that the wage gain associated with working in a large firm or establishment remains statistically significant and practically large even after controlling for unobserved worker heterogeneity,<sup>1</sup> and is remarkably stable over time and across countries with different labor market institutions. To put the magnitude of the size-wage premium into perspective, we quote [Brown and Medoff \(1989\)](#), “if a typical worker went from an establishment with employment one standard deviation below average to an establishment with employment one standard deviation above average, the employee would enjoy a wage increase of 8-12 percent, about as large as the union-nonunion differential in these data.”

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<sup>1</sup>[Moore \(1911\)](#) first documented this phenomenon for workers at Italian textile mills. For studies in U.S., see [Lester \(1967\)](#), [Personick and Barsky \(1982\)](#), [Mellow \(1982\)](#), [Brown and Medoff \(1989\)](#), [Brown et al. \(1990\)](#), [Idson and Feaster \(1990\)](#), [Troske \(1999\)](#). For studies in U.K. and other European countries, see [Main and Reilly \(1993\)](#), [Green et al. \(1996\)](#), [Abowd et al. \(1999\)](#), [Albæk et al. \(1998\)](#), [Winter-Ebmer and Zweimüller \(1999\)](#). Similar findings are also reported in developing countries, see e.g. [Velenchik \(1997\)](#), [Schaffner \(1998\)](#), and [Söderbom et al. \(2005\)](#).

The existence of the size-wage premium is puzzling and hard to rationalize within the perfect competition paradigm (see e.g. [Brown and Medoff, 1989](#)). While some studies incorporate labor market imperfections to explain the size-wage effect, as [Burdett and Mortensen \(1998\)](#) do with job search frictions, others challenge this empirical finding directly, noting that the observed wage differential is due to inadequate control of workers' productivities. For example, [Troske \(1999\)](#) and [Zabojnik and Bernhardt \(2001\)](#) suggest workers in large firms receive more training, thus are paid more as they are more productive.

In this paper, we first re-examine the size-wage premium phenomenon with the 1979 Youth Cohort of National Longitudinal Studies (NLSY79), specifically controlling for workers' training status. Consistent with earlier studies, we find that large firms pay more than small firms, even for untrained workers, and they also train a higher proportion of their workforce. Thus, we are able to rule out the training hypotheses as explanations for the size-wage effect. In addition, we also find that wage differential for trained workers is smaller than for untrained workers. [Brown and Medoff \(1989, page 1089\)](#) have also noted that "A striking regularity among the professional, technical, and managerial workers is the tendency for the wage differential to decline with increasing skill levels." No existing theories, including the random search model of [Burdett and Mortensen](#), can explain this piece of empirical evidence.

We then develop a two-period model of imperfect information that reconciles all three stylized facts. In this model, firms are identical ex ante, while workers are either of high type, with high productivity, or of low type, with low productivity. Firms post wages to attract workers they want to hire, and workers accept offers with the highest wage. At the beginning of the first period, neither firms nor workers know the type of any worker. However, when a worker applies for jobs, firms each observe a private signal that imperfectly indicates her type. In equilibrium, firms pay workers their expected productivities given the privately observed signals. Firms that post higher wages will hire more workers that are also more productive on average. Thus, workers of the same type are paid differently in different-sized firms, simply because they are pooled with workers of different average productivities. In the second period, firms receive another signal that imperfectly indicate workers' performance in the first period. Given the new information, incumbent firms make training decisions and post different wages for trained and untrained workers. In equilibrium, firms provide training only to those from whom they receive a good signal, but pay them according to pre-training expected productivities.

In identifying information imperfection as the source of size-wage premium, this paper falls into a large literature on labor market information that dates back to [Stigler \(1962\)](#) (see also [Spence, 1973](#) and [Gibbons and Katz, 1992](#)). This is different from the existing theories of wage dispersion that either assume workers have no knowledge about particular jobs when

applying, as in random search models, or restrict workers to apply to only a finite number of jobs at a time, as in the directed search / matching models.<sup>2</sup> According to our model, unobservable worker heterogeneity can explain a sizable portion of the observed size-wage premium, as reported in most empirical studies.<sup>3</sup> The remaining part of wage differentials that cannot be explained by unobservables is due to the pooling effect.

The rest of the paper is structured as follows. Section 2 presents our empirical findings using the 1979 cohort of National Longitudinal Studies of Youth (NLSY79) data. We also briefly review some existing theoretical models but find none of them could explain our findings simultaneously. In Sections 3 and 4, we present a two-period labor market model of imperfect information and discuss its implications. Section 5 concludes.

## 2 Empirical Regularities from NLSY79

We base our empirical work on NLSY79 for three reasons. First, it is a longitudinal data set that contains detailed individual characteristics, including variables that are usually not available in comparable data sources, e.g., the AFQT (Armed Forces Qualification Test) score that indicates pre-market human capital (see [Neal and Johnson, 1996](#)). Second, as sample individuals were young when the survey started, we can examine size-wage relationships for labor market entrants. This turns out to be important for the purpose of differentiating some alternative hypotheses. Last, NLSY79 contains very detailed on-the-job training information, which allow us to compare size-wage premiums for trained and untrained workers. In fact, no previous study has examined returns to training, i.e., wage differences between trained workers and untrained ones, for large and small firms separately.<sup>4</sup>

### 2.1 NLSY79 Data

NLSY79 contains detailed information about training and has been used extensively in the empirical literature. It contains 12,686 individuals aged 14-21 in 1978. The respondents were interviewed annually from 1979 to 1994, and every two years since then. It consists of a nationally representative cross-sectional sample, a supplemental sample, and a military sample. In this paper, we restrict all analyzes to the cross-sectional sample, and focus on the period 1986-2000 since no establishment size (or firm size) information is available in the 1981-1985 surveys. We do not use post-2002 data because some survey questions have been restructured.

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<sup>2</sup>See [Moen \(1997\)](#), [Shi \(2002\)](#), [Shimer \(2005\)](#) and [Albrecht et al. \(2006\)](#).

<sup>3</sup>See [Brown and Medoff \(1989\)](#) and other studies cited before.

<sup>4</sup>Most recent studies on return to training are based on NLSY79, see [Lynch \(1992\)](#), [Veum \(1995\)](#), and [Frazis and Lowenstein \(2005\)](#).

Despite its richness, training information has not been collected consistently in NLSY79 over time. The 1979-1986 surveys records only up to three formal training spells enrolled since last interview (thereafter called “current training spells”) and up to two training spells that was still ongoing at last interview (thereafter called “previous training spells”). This was followed by a year of absence of training information in 1987. In the 1988-2002 surveys, up to four current and three previous training spells are recorded. Supplemental questions, such as who paid for the training and the usefulness of training programs, were only asked in some of these surveys.

For the present analysis, we try to consistently use the following information for each training spell: type of training, starting date, ending date, a dummy on whether the spell is censored and total training hours. The type of training information is used to restrict the analysis to on-the-job training only. A training spell is classified as on-the-job training if it is “company training (type=8)” during the 1979-1986 surveys, “formal company training run by employer (type=8)” or “training programs at work not run by employer (type=9)” during the 1984-2000 surveys.

For a current training spell still going on at the date of interview, we update the information from the next survey. For example, to update the information of a training spell still going on at the date of interview in the 1988 survey, we find the “previous training spell” information from the 1989 survey. If the types of the two spells match, we then update the ending date, and other information accordingly. As NLSY79 does not provide identifiers that could link training spells across surveys unambiguously, we only update the information once and do not go further even if the training spell was still going on after updating. In that case, the interview date is recorded as the pseudo-ending date and a dummy is used to record the spell as censored.

We use a training dummy (training incidence) instead of actual training hours in this paper. As noted in [Barron et al. \(1997\)](#), training incidence contains much less measurement errors than training hours. Moreover, similar to [Veum \(1995\)](#), our preliminary regressions also suggest that in most cases, after controlling for training incidence, number of training hours is no longer statistically significant.

Establishment size information are taken from the question “

larger than the firm effect.

The analysis uses current job (or CPS job, job number 1) information for the period 1986-2000. We first transform nominal hourly wages into real wages using CPI-U (1982-1984=100), then exclude values that are greater than 100 dollars or less than 1 dollar. For each current job hourly wage, the following information are recorded: year of tenure, total labor market experience, union status on the job, industry, part-time status, establishment size, a dummy whether completed any on-the-job training spell on the current job, total accumulated on-the-job training hours. Variables such as gender, race, education, and AFQT score are also included.

To make sure that we are analyzing a homogeneous group of workers, we restrict our sample to white males that worked full-time (defined as 35 hours work per week and above) at non-union jobs in non-agricultural sectors. Table 1 describes the variables used in this paper.

## 2.2 Employer size-wage effect

Many studies have shown that large firms pay more on average to their workers, even after controlling for a set of variables that reflect productivity. However, employer size-wage effect has not been uniform across all industries of the economy. For example, [Lallemant et al. \(2005\)](#) show that the effect is generally much stronger in manufacturing industries than in service industries for European countries. Although not extensively documented in the literature, similar patterns are also true in U.S.. Table 2 gives industry level firm size-wage relationship based on the 2002 data provided by U.S. Small Business Administration (SBA). The data show that for retail trade and a couple of service industries, larger firms do not necessarily offer higher wages, even though no controls have been included at all.

With NLSY79 data, the first empirical test is to see whether we can observe size-wage effect. Following SBA data, we exclude two industries from all analyzes: retail trade and professional and other services. Sample summary statistics are given in Table 3. Note that the unit of observation is a person-year. The sample mean of natural log of hourly wage is 6.77, which corresponds to a real wage rate of \$8.74. In terms of education, 56% of the sample has a high school diploma or less, while 23% of the sample has at least a Bachelor's degree. On average, workers have 4 years of tenure with current employers and 11 years of total labor market experience. 83% of the sample work in small establishments, while 17% work in large ones, where large establishments is defined as those with at least 500 employees. Table 4 gives sample means for small and large establishments, respectively. Average wage rate for large establishments is substantially higher. Those who work for large establishments earn \$11.6 per hour on average, more than 40% higher than those in small establishments. On

the other hand, workers in large establishments also tend to be more productive, with more education, higher AFQT scores, longer tenure with current employers and more on-the-job and off-the-job training.

The following ordinary least squares (OLS) model controls for observable characteristics that affect productivities and wages.

$$Y_{it} = \beta L\_EST_{it} + X'_{it} \gamma + \epsilon_{it} \quad (1)$$

In equation (1), for worker  $i$ ,  $Y_{it}$  is the log hourly wage in year  $t$ ,  $L\_EST_{it}$  is a dummy variable for large establishment,  $X_{it}$  is the vector of other explanatory variables, including AFQT, schooling dummies, marriage dummies, regional dummies, local unemployment rate, tenure with current job, total labor market experience, survey year dummies and industry dummies.

Equation (2) is a panel data model, with  $C_i$  being the unobserved person effect that does not change over time.

In equation (3),  $TR_{it} = 1$  if person  $i$  has finished at least one on-the-job training spell on the current job by year  $t$ , and  $TR_{it} = 0$  otherwise.  $TRL_{it}$  is the interaction term of  $TR_{it}$  with  $L_{EST}_{it}$ . We also include interaction terms of  $L_{EST}_{it}$  with  $Tenure$  and  $TenureSQ/100$  in the vector  $X_{it}$  to control for possible different tenure effects in large and small establish-

usual random effects approach as in equation (4), but at the person-job level. The second is the fixed effects approach which uses only within job spell variations. In both of the previous two cases,  $C_i$  can be simply dropped because the person effect is included in  $\varepsilon_{iJ_{it}}$ . The last one is a two-level mixed model, accounting for both  $C_i$  and  $\varepsilon_{iJ_{it}}$  in the variance-covariance matrix

Table 7 reports the results. The random effects results based on job match effects are not greatly different from those based on person effects as in equation (4). Again, return to training is smaller in large establishments by 4% and this difference is statistically significant with a p-value of about 6%.

The fixed effects specification for equation (5) does not give sensible results, but are listed nevertheless for completeness. For example, tenure effect is estimated to be negative and labor market experience effect is very large. This is because that within a job spell, tenure and total labor market experience are perfectly collinear. Also, size-wage effect ( $L\_EST_{it}$ ) is estimated to be zero. Again, this is because that within a given job spell, variations on establishment size either comes from changes in the size of current establishment, or more likely, measurement errors. Nevertheless, the coefficient on  $TLL_{it}$  is both negative and large (-3.1%), suggesting return to training to be smaller in large establishments.

Results from the two-level mixed model are similar to those of random effects approach. Return to training is 2.9% in small establishments. The coefficient on  $TLL_{it}$  is -4.4% and significant at the 5% level. Also, as shown by the estimated coefficients of  $L\_Tenure$  and  $L\_TenureSQ/100$ , with both random effects and two-level mixed effects specifications, there does not seem to be a difference in terms of tenure effects in small and large establishments.

It should also be pointed out that there does not exist a single specification that is preferred to others. While fixed effects estimator is consistent even if person or job-match effects are correlated with the explanatory variables, it uses only within variations and the measurement error problem can be quite severe. Nevertheless, in all specifications there is strong evidence that return to training is lower in large establishments.

Our empirical results are not sensitive to small modifications in model specification, such as including occupation dummies, adding or dropping quadratic terms. We have also performed two additional robustness checks, one that also includes off-the-job training information in the model, and another that restricts all analyzes to the period of 1987-2000 and uses only employer paid on-the-job training spells. In both cases the main finding of lower size-wage premium for trained workers is unaffected. The results are not listed in this paper, but available from the authors upon request.

Some caveats may apply to our empirical analyzes. The first one concerns possible problems caused by measurement errors. However, [Barron et al. \(1997\)](#) suggest that measurement

errors in training variables are unrelated to establishment size. Thus, the difference in returns to training between small and large establishments would be even larger if there were no measurement errors, as first differencing attenuates the magnitude of all coefficients. The second one is related to a point raised by [Gibbons and Katz \(1992\)](#). If person effects or job-match effects are not constant for a worker or during a job spell, then even the fixed effects estimator is not consistent. However, a priori there is no reason to expect the effects to be different for different sized establishments. Thus, the possible impact on the estimated coefficient might be small. The third one is possible bias due to endogenous labor mobility, as discussed in [Gibbons and Katz \(1992\)](#). For example, model (4) estimated by fixed effects approach will only give effects for those who change jobs. Nevertheless, while the estimated parameters are biased for the whole sample, they are valid at least for the subpopulation of job changers and thus, remain informative. Model (5) considers unobserved job effects, thus is not directly subject to this criticism.

## 2.4 Do large establishments train more?

Previous studies (e.g., [Bishop, 1997](#)) have already found that large establishments train a higher proportion of their workers. In this subsection, we conduct the empirical examination ourselves using NLSY79 data, controlling for more detailed information such as AFQT.

$$TR_{it}^* = Z_{it} + v_{it} \quad (6)$$

$$TR_{it} = \begin{cases} 1 & \text{if } TR_{it}^* \geq 0 \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

In equations (6) and (7),  $TR_{it}^*$  is a latent variable that indicates the propensity to receive training,  $Z_{it}$  is a set of explanatory variables that include establishment size dummy, and  $v_{it}$  is the error term. In the simple Logit specification,  $v_{it} = \epsilon_{it}$ , while in the panel specifications,  $v_{it} = C_i + \epsilon_{it}$ .  $C_i$  is the unobserved person effect and  $\epsilon_{it}$  is a logistic error term. [Table 8](#) reports odds ratios for Logit, random effects Logit and fixed effects Logit specifications. Overall the results are consistent with the existing literature. Workers with higher education levels, longer tenure and more labor market experiences are more likely to receive on-the-job training. Controlling for other factors, workers in large firms are also significantly more likely to receive on-the-job training. The odds ratio is 2.2 and 2.3 in Logit and random effects Logit, and 1.7 in fixed effects Logit.

## **2.5 Discussions of existing theories**

In light of our new empirical findings, we discuss here some recent explanations for the size-wage premium that has not been examined in [Brown and Medoff](#)

smaller firms. In a competitive setting, this would translate into higher wage increases for trained workers in large firms.

Similarly, models have been proposed that attribute the observed size-wage premium to imperfect control of levels of training workers received in different sized firms. Troske (1999) argues that large firms not only hire more skilled workers, but also “produce” more skilled workers through training. Hu (2003) studies the hiring decisions of large firms and also hypothesizes that firm-specific human capital might explain the size-wage effect. Similarly, Zabochnik and Bernhardt (2001) develop a model in which incentives for workers to accumulate general human capital are provided by corporate tournaments. Due to differences in corporate structures and prize sizes, workers in large firms are induced to accumulate more general human capital and are thus paid more.

These training models predict no size-wage premium for untrained workers, which is grossly inconsistent with our empirical finding. The specific training model of Troske (1999) also implies that starting wages for workers in small firms should be *higher* than those in large firms, as workers and firms share the costs and benefits of specific training (Becker, 1975). Our data, on the contrary, suggest that large firms pay more even for job market entrants than small firms.

### **3 A Model of Labor Market Imperfect Information and On-the-job training**

The model analyzed here considers a two-period competitive labor market with no barriers to entry and exit. Firms are initially identical, have the same production technology, and produce the same output. The output is traded at a competitive market at a price  $P$  which we normalize to 1. Firms maximize total profit and have a discount rate of zero.

There is a continuum of workers that can be sorted into two types: high type and low type. High type (also referred to as type H) workers account for proportion  $\theta$  of the population, and low type (also referred to as type L) workers account for proportion  $1 - \theta$  of the population. A high type worker can produce some output if employed, while a low type worker will never be able to produce any output. Workers enter the labor market in the first period and retire at the end of the second period.

The proportion of the two types is common knowledge and known to all firms. However, an individual worker’s type is unknown to both the individual and firms initially.<sup>7</sup> Hence, information is symmetric at the beginning, though firms and workers may learn about workers’

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<sup>7</sup>Making an alternative assumption, namely allowing workers to know their own types, does not affect the main result in this model, but makes the analysis significantly more complicated.

types differently after some labor market experience. This

### 3.1 The first period

The first period starts with workers applying to all firms. While not knowing workers' types, firms each receive a private signal  $y_k \in \{h, l\}$  as an imperfect indicator of workers' types. Conditional on a worker being of high type, firm  $k$  observes signal "h" with probability  $\pi_H > 1/2$ , and observes "l" with probability  $1 - \pi_H$ . Conditional on a worker being of low type, firm  $k$  observes "l" with probability  $\pi_L > 1/2$  and observes "h" with probability  $1 - \pi_L$ . For simplicity, we assume private signals received by different firms are independent, and a worker recognized as low type by one firm may be taken as high type by another.

We let  $\pi_i = \pi$  for  $i = H, L$ ,<sup>8</sup> and assume that  $\pi \in (1/2, 1)$ . When  $\pi = 1/2$ , firms have no ability to differentiate high type workers from low type workers. When  $\pi = 1$ , firms can perfectly distinguish high type from low type workers. When  $1 > \pi > 1/2$ , firms have some but less than perfect ability to distinguish, and this is the case we focus on.

Given the signals received about workers' types, firms simultaneously make wage offers to those they want to hire. While some workers may receive multiple offers, they can only accept one. The wages workers receive in the first period are verifiable and will be known to firms in the second period, however, offers they receive are not verifiable and remains workers' private information. In this sense, learning is asymmetric between firms and workers, as workers may acquire more information about their own types after some market experience.

Having received all the wage offers, workers will choose a firm that offers the highest wage, provided the highest offer is greater than his reservation wage  $r$ . After that, production begins, and firms realize their profit.

### 3.2 The second period

At the beginning of this period, firms observe workers' performance in the previous period. However, due to technical limitation, they do not observe workers' output directly. Instead, they observe a signal  $s_j$  from each worker as an imperfect indicator of his performance and type.

Conditional on a worker being of high type, the incumbent firm observes a good signal "g" with probability  $\pi_H$  and observes a bad signal "b" with probability  $1 - \pi_H$ . Conditional on a worker being of low type, the incumbent firm observes "g" with probability  $\pi_L$  and observes a "b" with probability  $1 - \pi_L$ . For simplicity we assume  $\pi_H = 1 - \pi_L = \pi > 1/2$ ; the probability of mistaking a high type for low type and the probability of mistaking a low type for high type are the same.

Given the signals received, the incumbent firm updates its belief about workers' types

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<sup>8</sup>This assumption is made for simplicity and relaxing it will not affect our result.

using Bayes rule. If a firm  $k$  has a prior belief  $H_k$  of a worker being of high type, Bayes rule requires that its posterior belief be  $\mu_0$  if it receives a bad signal “b”, where

$$\mu_0 = \frac{H_k(1 - \alpha)}{H_k(1 - \alpha) + (1 - H_k)} < H_k$$

On the other hand, if it receives a good signal “g”, the posterior belief  $\mu_1$  should be

$$\mu_1 = \frac{H_k}{H_k + (1 - H_k)(1 - \alpha)} > H_k$$

Having acquired information on workers’ productivities, incumbent firms can provide a firm-specific training to some employees. Training increases high type workers’ productivity but not of the low type workers. After training, a high type worker can produce  $q > 1$  unit of output in the second period, while he can only produce one unit without training. A low type worker’s output, nonetheless, equals zero with or without training. Because of the firm specificity, training received at firm  $j$  does not increase workers’ output at firm  $k$  ( $k \neq j$ ). Training is costly, and it takes the incumbent firm a cost of  $c$ ,  $c > 0$ , to train one worker. When the per workers training cost is high, for example,  $c > (q - 1)$ , it would not be profitable to train any worker. On the other hand, when the cost equals zero, it is profitable to train every worker, unless firms know the worker involved is low type with certainty. Without loss of generality, we restrict our attention to situations where at least two firms provide training to workers from whom they receive a good signal “g”, and no firm provides training to those from whom they receive a bad signal “b”.

**Assumption 1.** *The parameter  $\alpha, c$  are such that*

$$\frac{(q - 1)}{1 + (1 - \alpha)(1 - \alpha)} > c > \frac{(1 - \alpha)(q - 1)}{(1 - \alpha) + (1 - \alpha)(1 - \alpha)}$$

Meanwhile, outside firms, though have no direct contact with the workers, can also observe a private signal about each worker’s performance. However, outside firms can only observe a coarser version of information received by the incumbent. Specifically, conditional on the incumbent firm observing a signal “g” (“b” respectively), outside firms observe a signal  $\tilde{g}$  ( $\tilde{b}$  respectively) with probability  $\nu \in (1/2, 1)$ , and observe  $\tilde{b}$  ( $\tilde{g}$  respectively) with probability  $1 - \nu$ . One interpretation of this assumption is that the signal each outside firm observes is some private distortion of a random variable (incumbent firm’s signal) that imperfectly indicates a worker’s type. For example, the incumbent firm may have an evaluation of performance of each employee, which imperfectly indicate his true types. Outside firms may learn about those evaluations through some indirect channels, which makes their information less accurate than that of the incumbent firm. We will investigate the case when  $1/2 < \nu < 1$ . That is, both the incumbent and outside firms have extra information to help them better

judge workers' type, but the information outside firms have is less accurate than that of the incumbent firm.

The information structure is very close to Schönberg (2007) and Golan (2005 2006). However, we differ from them by not allowing the incumbent firm to perfectly learn workers' true types after the first period. Learning is imperfect for the incumbent firm as well as for outside firms here, whereas learning is perfect for the incumbent firm in their models. Of course, if firms and worker are to interact for many periods, incumbent firms' belief may gradually converge to their true types, which corresponds to a special case of our model when  $\beta = 1$ .

After observing information about workers' types, firms start to make wage offers. The incumbent firm moves first by offering each employee the chance to renew contracts with wage  $w$ . Having observed the offers made by the incumbent firm, outside firms can make offers to workers. Before making offers, outside firms know the wages each worker received in the previous period as well as his training status. Workers choose the firm that offer the highest wage, but stay with the incumbent firm if its offer is at least as high as their outside offers. This implies that to retain workers, incumbent firms need to offer their employees at least as much as their outside offers.

After workers and firms are matched, production begins. A trained type H worker who stays with his previous employer produces  $q > 1$  unit of output, and a trained type H worker who changes employers, so as an untrained type H worker, produces one unit of output. A type L worker produces no output, irrespective of training status. When production is finished, firms realize their profits and workers exit the market.

### 3.3 Equilibrium concept

The solution concept we use is competitive equilibrium. A competitive equilibrium is characterized by the number of firms  $K$ , an equilibrium wage offer distribution  $F(W)$  and firms' training decision such that the following conditions are satisfied

- (a) Workers maximize wages giving the equilibrium wage offer;
- (b) Firms make wage offers and train decisions to maximize profit given their belief about workers' type and competing firms' choices;
- (c) Firms' belief about workers' type is derived from their prior belief using Bayes rule;
- (d) Firms each make zero total profit.

Note that even if firms each make zero total profit overall, they may have a positive or negative profit in any period. For example, firms' may make a positive profit in the second period, when the benefit from firm-specific training more than offsets the cost of training.

## **4 Main result**

In this model, workers are free to change employers and firms are free to fire workers. No long-term contracts can be beneficial either to firms or workers, so there is no loss of generality in restricting attention to spot-market contracting. In what follows we first show that there exists an equilibrium that generates size-wage premium.

**Claim 1.** Suppose firm  $k$  hires workers with average productivity of  $H_k$  in the first period. In the second period, firm  $k$  will offer

$$w_k^g(H_k) = \frac{H_k}{H_k + (1 - H_k)(1 - \beta)}$$

to those from whom it receives a good signal “g”, and will offer

$$w_k^b(H_k) = \frac{H_k(1 - \beta)}{H_k(1 - \beta) + (1 - H_k)}$$

to those from whom it receives a bad signal “b”.

Thus, no firm has monopsony power in this market; firms always pay a worker his pre-training expected productivity. This is so as outside firms know the average productivity of the incumbent firm, and competition forces pre-training profit to zero in the second period. Of course, this result holds only if the incumbent firm can not make any counter offers. When the incumbent can make counter offers, as in [Golan \(2005\)](#) and [Baron et al. \(2006\)](#), this may not be the case.

Claim 1 shows that in the second period, incumbent firms offer employees their pre-training expected productivity. As a result, no worker changes employer in the second period. However, this is not to say that every worker would stay with his current employer in the second period. In fact, job separation may occur when some workers, i.e., untrained workers at some firms, find wages they can get fall below their reservation wage in the second period. We will come back to this point after we characterize wage distribution in the first period.

The incumbent firm knows that it will pay each group of workers their pre-training expected productivities subsequently. Because of the firm specificity of training, it is profitable to train a worker as long as the expected increase in productivity more than offsets the training cost. Depending on parameter combinations, firms may find it profitable to train all workers regardless of signals received, train only those from whom a good signal “g” has been received, or provide no training at all. Let  $n_k$  ( $m_k$

*It provides no training to employees if and only if (9) is violated.*

Note that as  $\alpha > 1/2$ , condition (8) implies condition (9), but not the reverse; if it not profitable to train workers from whom firm  $k$  receives a good signal “g”, it will not be profitable to train those from whom firm  $k$  receives a bad signal “b”. The intuition is clear. Training cost per worker is the same for both groups of workers, those with a signal “g” and those with a signal “b”. However, those with a signal “g” are more likely to be of high type workers and therefore, the expected benefit from training is greater. It is more profitable to train workers with a good signal than those with a bad signal. Consequently, firm  $k$  trains both groups of workers if and only if the expected surplus from training workers with a signal “b” exceeds the cost of training them. When condition (8) fails but condition (9) holds, it is profitable to train those with a good signal but not profitable to train those with a bad signal. When condition (9) fails, training cost is so high that it is not profitable to train even good workers. No training will be provided in this case.

The previous result implies that firm  $k$ ' total profit in the second period equals  $\Pi_k$  if  $\Pi_k > 0$ , and zero otherwise. Note that

$$\Pi_k = n_k(q - 1) - N_k c \quad (10)$$

if condition (8) is satisfied, but

$$\Pi_k = (q - 1)n_k - [n_k + (1 - \alpha)m_k]c \quad (11)$$

if condition (9) holds but not condition (8) fails. In both cases, the average profit function  $\pi_k$  will be an increasing function of  $H_k$ , the average productivity of workers at firm  $k$ . To see that, we note that in the first case, average profit  $\pi_k$  equals

$$\pi_k(H_k) = \frac{\Pi_k}{N_k} = (q - 1)H_k - c, \quad (12)$$

while in the second case,

$$\pi_k(H_k) = \frac{\Pi_k}{N_k} = (q - 1)H_k - [H_k - (1 - \alpha)(1 - H_k)]c \quad (13)$$

Clearly,  $\pi_k$  is an increasing function of  $H_k$ .

Claim 1 and Lemma 1 summarize firms' choices in the second period. Incumbent firms pay each worker his pre-training expected productivity, and train a worker if and only if the expected surplus from training exceeds the cost  $c$ . After characterizing the first period wage distribution, we will come back for more on firms' training decisions. However, for time being, we will leave it as it is and go backward to determine firms' wage offers in the first period.

In the first period, firms do not know any worker's type for sure. However, they have some ability to tell high type workers from low type workers. Therefore, they are not going to offer

the same wage to every worker that applies. A further complication is that a worker may receive different wage offers from different firms. This is so as firms' ability to differentiate high type from low type workers are independent across firms, so one firm may think a worker as high type while another takes him as low type, regardless of his true type. Fortunately, the following two results significantly simplify our analysis.

**Claim 2.** *In equilibrium, no two firms offer the same wage in the first period.*

The claim shows that, in equilibrium, firms always offer different wages, as offering the same wage is not a best response given competing firms' offers. Hence, the equilibrium wage distribution can not be degenerated when there are more one firms active in equilibrium, which we will show shortly.

Suppose now there are  $K$  firms active in the market, denote the set of wages offered in the first period by firm  $j$  by  $W$

The measure of workers firm  $k$  hires equals

$$N_k = (1 - \alpha)^{k-1} + (1 - \alpha)^{k-1}(1 - \alpha)$$

Clearly, both the average productivity  $H_k$  and the measure of workers  $N_k$  hired by firm  $k$  decrease as  $k$  increases.

After firms  $1, 2, \dots, k-1, k$  have hired, the measure of workers remains to be hired will be

$$R_k = (1 - \alpha)^k + (1 - \alpha)^k,$$

and the average productivity of the remaining workers will be

$$S_k = \frac{(1 - \alpha)^k}{(1 - \alpha)^k + (1 - \alpha)^k} = \frac{[(1 - \alpha)/\alpha]^k}{[(1 - \alpha)/\alpha]^k + (1 - \alpha)}$$

Note that both  $R_k$  and  $S_k$  are strictly decreasing in  $k$ . As more and more firms have hired, the proportion of high type workers in the remaining pool decreases, so does the measure of unemployed workers. At certain point, it becomes unprofitable for another firm to hire, as the expected benefit from hiring a worker the firm recognizes as high type drops below the minimum wage  $r$  firm needs to pay. This implies that the equilibrium number of firms  $K$  is determined by the condition

$$H_k + \alpha_k(H_k) \geq r > H_{K+1} + \alpha_{K+1}(H_{K+1}) \quad (14)$$

In above we have showed that  $\alpha_k(H_k)$  is weakly increasing in  $H_k$ . The fact that  $H_k$  strictly decreases in  $k$  indicates  $\alpha_k(H_k)$  is a decreasing function of  $k$ . Hence, the number of firms  $K$  is uniquely determined. And firm  $K$  offers a wage of  $w_K$  to the workers it intends to hire, where

$$w_K = \max\{H_K + \alpha_K(H_K), r\}, \quad (15)$$

As firm  $K$  is the last one to hire, one may wonder whether firm  $K$  may just offer  $r$ , the minimum wage to workers it intends to hire and earn a positive profit when  $H_k + \alpha_k > r$  and  $H_N$

model is consistent with the traditional wisdom, and is in sharp contrast with that of [Burdett and Mortensen \(1998\)](#). In [Burdett and Mortensen](#), an increase in minimum wage decreases inefficient unemployment due to search friction, and thus, “*employment increases with the minimum wage even though atomistic wage competition, not classic monopsony in the formal sense of one buyer, characterizes the market structure.*”

Provided the reservation wage  $r$  is sufficiently small, the equilibrium wage offer in period one is not degenerate; there will be more than one firm, with each firm offering a different wage.

**Claim 5.** *Under the assumption that  $r < \frac{1}{2}$ , there are at least two firms active in the market, i.e.,  $K \geq 2$ .*

This result follows immediately from the assumption  $r < \frac{1}{2}$ , as

$$w_2 \geq H_2 = \frac{1}{2} > r,$$

and condition (15) implies that  $K \geq 2$ .

In above we have already given the conditions for a firm to train all employees, train only those from whom firm has a received a good signal “g”, and provide no training to any of their employees. Now that we have determined the wage and firm size distribution in the first period, we can further pin down firms’ training decisions in the second period.

**Claim 6.** *Under Assumption 1, at least two firms, firm 1 and 2, will provide training to the group of workers from whom a good signal “g” is received, no firm provides training to the group of workers from whom a bad signal “b” is received.*

Consequently, in the second period, only good workers, those from whom firms have received a good signal “g” will be trained. Given the above results, we are now ready to prove Proposition 1.

*Proof of Proposition 1.* Claim 1 through Claim 6 gives one equilibrium in which workers maximize wages in both periods, and firms maximize profits in wages offers and training decisions. In this equilibrium, workers maximize wages and firms maximize profit given beliefs about workers’ types. Firms’ beliefs are updated given information acquired using Bayes rule. Thus, neither firms nor workers has incentives to choose differently. In addition, each firm makes zero total profit. This confirms that the equilibrium outlines is indeed a competitive equilibrium of this model. In the equilibrium, in the first period, each firm  $k$  with size  $N_k$  pays wages  $w_k = H_k + \frac{1}{2}(H_k)$ , where

$$H_k = \frac{(1 - \frac{1}{2})^{k-1}}{(1 - \frac{1}{2})^{k-1} + (1 - \frac{1}{2})^{k-1}(1 - \frac{1}{2})}$$

and  $\phi(\cdot)$  is an increasing function of  $H_k$ .

The first period wage offers is decreasing in  $k$ , with firm 1 offering the highest wage  $w_1$  and firm  $K$  the lowest wage  $w_K$ . Given the wage distribution  $w_1 > w_2 > \dots > w_K$ , the measure of workers firm  $k$  hires equals

$$N_k = (1 - \alpha)^{k-1} + (1 - \alpha)^{k-1} \phi(H_k),$$

which decreases as  $k$  increases. Hence, in the first period, larger sized firms pay higher wages to workers of the same type than smaller size firms. This is also true after we control for workers' training status; trained workers (untrained workers respectively) at larger size firms get higher pay than trained workers (untrained workers respectively) at smaller size firms.

In the second period, firms only provide training to workers from whom a good signal "g" is received, as Claim 6 shows. In addition, Claim 1 shows that at any firm  $k$ , trained workers receive  $w_k^g(H_k)$  and untrained workers receive  $w_k^b(H_k)$ . Clearly,  $w_k^g(H_k) > w_k^b(H_k)$ , trained workers receive higher wages than untrained workers.  $\square$

We summarize our findings as follows. In the first period, each firm posts a different wage, and the wage posted by firm  $k$  is  $w_k = H_k + \phi(H_k)$ , which strictly decreases in  $k$ . Hence, firm 1 post the highest wage and firm  $K$  offers the lowest. Each firm makes offer only to those it wants of hire, i.e., workers from whom it receives a signal "h". As workers maximize wages they receive, firms 1 can get all the workers it intends to hire, while the other firms only hire from the remaining pool of workers they extend offers. While firms make offers simultaneously, job matching ends up much like a sequential selection process, with firm 1 being the first one to choose and firm  $K$  being the last one to choose. As a result, firm 1 ends up hiring more workers than all the other firms, and firm  $K$

when the wage they expect to get falls below their reservation wage in this period. When this occurs at a firm  $k$ , the measure of workers who leave the firm in the second period equals  $(1 - \beta)^{k-1} (1 - \beta) + (1 - \beta)^{k-1} (1 - \beta)$ . In addition, since  $H_k$  decreases as  $k$  increases, it follows immediately from Claim 1 that both  $w_k^g(H_k)$  and  $w_k^b(H_k)$  decrease in  $k$ . That is, after we controlling for workers' training status, larger firms pay higher wages to workers of the same type than smaller firms.

The fact that only workers with a good signal are trained has several implications. The first implication is that larger firms train disproportionately more workers than smaller firms.

**Corollary 1.** *The proportion of trained workers increases in firm size  $N_k$  and decreases in  $k$ .*

This result follows from the fact that firm size,  $N_k$  and the average quality of workers,  $H_k$ , both decrease in  $k$ . But the proportion of trained workers at firm  $k$ ,  $H_k + (1 - \beta)(1 - H_K)$ , is increasing in  $H_k$  and thus decreasing in  $k$ . This explains the empirical finding that larger firms train disproportionately more of their employees.

Another implication is that wage differentials between firms of different sizes will be smaller for trained workers than for untrained workers. In selecting workers to train, firms will try to identify productive workers to train. Because of this additional selection process, differences in average productivities for trained workers between firms of different sizes decreases. This helps to reduce wage differentials for trained workers.

**Proposition 2.** *Log wage differential is smaller for trained workers than for untrained workers.*

Hence, even though trained workers at a larger firm gets higher pay than trained workers at a smaller firm, the wage differential is smaller than the wage differential between untrained workers at the two firms. And the return to training is smaller at the larger firm than at the smaller firm. Previous researches, for example, the [Burdett and Mortensen \(1998\)](#) model, attribute the size-wage premium to frictions other than difference in workers' qualities. As a result, though being able to generate size-wage premium as an equilibrium outcome, they fail to reconcile size-wage premium with empirical finding on wage differential for trained workers.

In above we have identified one type of equilibrium, the equilibrium with size-wage premium. Note that the equilibrium with size-wage premium is not a single equilibrium and renaming of firms does not change any properties of the equilibrium. A question naturally arise, are there any other types of equilibrium? The answer is no, as the following result shows.

**Proposition 3.** *There exists no equilibrium other than the equilibrium with size-wage premium.*

Therefore, the equilibrium is unique up to renaming of the firms. This result is not surprising, as Claim 2 and Claim 3 already show that in any equilibrium, firms post different wages and each firm post one wage only. This ensures that no other equilibrium can exist.

Thus, our model also generate size-wage premium. However, unlike the equilibrium search model, the size-wage premium comes mainly from differences in average productivities across firms. Workers of the same ability may be paid differently because they are pooled with workers of different average productivities.

Consequently, as more information becomes available to help firms better sort workers in the second period, the wage differential between firms of different sizes will decrease; return to training is smaller for larger firms than for small firms. Hence, by emphasizing quality difference to explain the size-wage premium, our model helps reconcile the new findings with the other two stylized facts documented in the literature.

## 5 Conclusions

In this paper we make two contributions to the literature of size-wage premium. First, using NLSY79 data, we show that large establishments pay more to their workers than small establishments, and train a higher proportion of their workforce, thus confirm findings from previous studies. In addition, we find that return to training for workers in large establishments is lower than those in small establishments. This empirical finding is new and fairly robust across different specifications. No existing theories could explain these three stylized facts simultaneously.

Second, we develop a two-period model of labor market with heterogeneous workers and imperfect observability of worker type. The model generates implications that are consistent with all our empirical findings. Thus, we believe this paper has offered an alternative way of understanding the puzzling size-wage premium phenomenon in the labor market.

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## Appendix

**Proof of Claim 1.** We prove this result by showing that the incumbent firm can not make any profit except that from firm specific training. As the decision of training does not affect wage offers, we simplify the proof a bit by pretending there is no training at all. That is, for proof of this result, we can look at a special case where  $q = 1$  and  $c = 0$ .

In this case, firm  $k$  could not make any wage offers that result in positive profit in the second period. To see that, we first suppose firm  $k$  offers worker  $i$  an wage  $w_k^i(2)$  such that  $\sum_{i \in k} w_k^i(2) = \sum_{i \in k} H_k$ , where  $i \in k$  indicates sum over firm  $k$ 's employees, then an outside firm could make a profit by attracting all of  $k$ 's employee. This could be done even if the outside firm has acquired no extra information in the second period. Of course, it could do better with the additional information.

Since firm  $k$  earns zero profit, could it offer the same wage  $w_k^2 = H_k$  to all workers in the second period, irrespective of signals received? Suppose that is the case, an outside firm  $j$  could make a profit by offering  $w_k^2 + \epsilon$  to those from whom firm  $j$  observes a signal “ $\tilde{g}$ ”. Consequently, the expected productivity of the remaining pool for firm  $k$  would be strictly less than  $H_k$  which leads to a loss in this period. Hence we conclude that firm  $k$  offers each employee her pre-training expected productivity in the second period.

If a worker is hired by firm  $k$  in period one, the chance that he is type H equals  $H_k$ . Thus the posterior belief that he is of type H is

$$\mu^1(H_k) = \frac{H_k}{H_k + (1 - H_k)(1 - \epsilon)} > H_k$$

if he produces a good signal in period one, and is

$$\mu^0(H_k) = \frac{H_k(1 - \epsilon)}{H_k(1 - \epsilon) + (1 - H_k)} < H_k$$

otherwise. Zero profit condition implies the second period wage offer should be  $w_k^g = \mu^1(H_k)$ , and  $w_k^b = \mu^0(H_k)$  respectively.  $\square$

**Proof of Lemma 1.** As training is firm specific, the incumbent firm alone will capture the surplus from training. With no training, firm  $k$ 's profit in the second period would be

$$\Pi_k = n_k - [n_k + (1 - \epsilon)m_k]w_k^g - [(1 - \epsilon)n_k + m_k]w_k^b = 0,$$

where  $w_k^g$  and  $w_k^b$  are wages paid to those with a good signal and bad signal respectively.

If firm  $k$  provides training only to workers with a signal “ $g$ ”, its profit would be

$$\Pi_k = qn_k - [n_k + (1 - \epsilon)m_k]c - [n_k + (1 - \epsilon)m_k]w_k^g - [(1 - \epsilon)n_k + m_k]w_k^b,$$

which is greater than zero if and only if the condition in (9) is satisfied. That is, the expected surplus from training must exceeds the cost of training.

Similarly, for firm  $k$  to provide training to those with a signal “ $b$ ”, the expected surplus from training this group of workers must exceed the cost, i.e.,

$$(1 - \epsilon)n_k(q - 1) - [(1 - \epsilon)n_k + m_k]c \geq 0$$

Note that this is equivalent to

$$(1 - \beta)\{(q - 1)n_k - [n_k + \frac{1 - \beta}{\beta}m_k]c\} \geq 0,$$

which indicates

$$\{(q - 1)n_k - [n_k + \frac{1 - \beta}{\beta}m_k]c\} = (q - 1)n_k - [n_k + (1 - \beta)m_k]c \geq 0$$

as  $\beta > 1/2$ . Hence if it is profitable for firm  $k$  to train workers with a bad signal “b”, it would be profitable to train all workers.  $\square$

**Proof of Claim 2.** Suppose two firms, firm  $k$  and firm  $j$  offer the same wage  $w$ . Given the pool of workers available to the two firms, firms make offers to workers they reckon as type H workers. Let  $n_k$  (respectively  $n_j$ ) be measure of type H workers and  $m_k$  (respectively  $m_j$ ) be measure of type L workers who will receive firm  $k$ 's (respectively firm  $j$ 's) offer. Given the information that the two firms have similar information technology and they offer the same wage, it is clear that  $n_k = n_j$  and  $m_k = m_j$ . Also let  $n$  and  $m$  be the measure of type H and type L workers that receive offers from both firms. As the probabilities are independent, clearly  $n = n_k$  and  $m = m_k$ . As workers randomly choose a firm to work for, firm  $k$  will attract  $n_k - n/2$  measure of type H and  $m_k - m/2$  measure of type L workers. Zero profit condition implies that wage  $w$  offered by the the two firms must be

$$w = \frac{(n_k - n/2)}{n_k - n/2 + m_k - m/2} = \frac{(n_j - n/2)}{n_j - n/2 + m_j - m/2}$$

However, in this case, firm  $k$  could profit by offering a higher wage  $w + \epsilon$ . Doing so, its profit would be

$$\Pi'_k(w + \epsilon) = \left[ \left( \frac{n_k}{n_k + m_k} - \frac{(n_k - n/2)}{n_k - n/2 + m_k - m/2} \right) - \epsilon \right] (n_k + m_k)$$

If we let  $\tilde{N}^H, \tilde{N}^L$  be the measure of type H, type L workers in the pool of workers firms  $k$  and  $j$  hires from, then we have

$$\begin{aligned} n_k &= \tilde{N}^H, & n &= \tilde{N}^H/2, \\ m_k &= \tilde{N}^L(1 - \beta), & m &= \tilde{N}^L(1 - \beta)^2 \end{aligned}$$

The condition  $\beta > 1/2 > 1 - \beta$  indicates

$$\frac{n/2}{n/2 + m/2} = \frac{\tilde{N}^H/2}{\tilde{N}^H/2 + \tilde{N}^L(1 - \beta)^2} > \frac{\tilde{N}^H}{\tilde{N}^H + \tilde{N}^L(1 - \beta)} = \frac{n_k}{n_k + m_k}$$

So we have

$$\frac{n_k - n/2}{n_k + m_k - n/2 - m/2} > \frac{n_k}{n_k + m_k}$$

Hence, by offering a wage  $w + \epsilon$ , firm  $k$ 's profit strictly increase,  $\Pi(w + \epsilon) > 0 > \Pi(w)$ ; two firms offering the same wage  $w$  can not be part of any equilibrium. The same argument implies that more than two firms offering the same wage can not be part of any equilibrium  $\square$

**Proof of Claim 3.** Since firm 1 has the highest wage, any worker who receives its offer will accept the offer. Because of imperfect information, firm 1 may recognize a productive worker as type H with probability  $\alpha$  and take a unproductive worker as type H with probability  $1 - \alpha$ . Given the proportion of the two types in the population, Bayes rule requires that the probability of workers accepting firm 1's offer being of type H to be

$$H_1 = \frac{\alpha}{\alpha + (1 - \alpha)(1 - \alpha)}$$

Zero-profit condition implies that the first period wage equals

$$w_1(H_1) = H_1 + \alpha(H_1),$$

where  $\alpha(H_1)$  is firm 1's expected profit per worker in the second period. The probability that a randomly chosen worker not hired by firm 1 is of type H equals

$$S_1 = \frac{(1 - \alpha)}{(1 - \alpha) + (1 - \alpha)}$$

Now suppose firm 1 also offer another wage  $w'_1$ ,  $w'_1 \neq w^1$ , to some other workers  $\quad )$

)



**Proof of Proposition 2.** Two firms,  $k$  and  $j$ , with  $k$  be the larger firm. Let the measure of workers firm  $k$  (firm  $j$  respectively) employs be  $N_k$  ( $N_j$  respectively). Also let  $n_k$  ( $n_j$  respectively) be the measure of type H workers firm  $k$  (firm  $j$  respectively) hires, and  $m_k$  ( $m_j$  respectively) be the measure of type L workers firm  $k$  (firm  $j$  respectively) hires. By assumption,

$$n_k > n_j, \quad n_k/N_k > n_j/N_j \implies \frac{n_k}{n_j} > \frac{n_k + m_k}{n_j + m_j} \implies \frac{m_k}{m_j} > \frac{N_k}{N_j} > \frac{n_k}{n_j}$$

The wage differential between workers at firm  $k$  and  $j$  in the first period is

$$\Phi_{kj} = \frac{\{n_k + (q-1)n_k - [n_k + (1-\alpha)m_k]c\}/N_k}{\{n_j + (q-1)n_j - [n_j + (1-\alpha)m_j]c\}/N_j}$$

The wage differential between trained workers at firm  $k$  and  $j$  in the second period is

$$\Phi^t = \frac{n_k/[n_k + (1-\alpha)m_k]}{n_j/[n_j + (1-\alpha)m_j]} = \frac{n_k}{n_j} \cdot \frac{n_j + (1-\alpha)m_j}{n_k + (1-\alpha)m_k}$$

Let

$$\Gamma(\alpha) = \frac{n_j + (1-\alpha)m_j}{n_k + (1-\alpha)m_k}$$

Note that  $\Gamma' < 0$  and  $\Gamma(1/2) = N_j/N_k$ . By our assumption,  $\alpha > 1/2$ , so we conclude  $\Gamma < N_j/N_k$  and

$$\Phi^t < \frac{n_k/N_k}{n_j/N_j}$$

On the other hand, we note that

$$\frac{n_k + (q-1)n_k}{n_j + (q-1)n_j} = \frac{n_k}{n_j}, \quad \text{and} \quad \frac{[n_k + (1-\alpha)m_k]c}{[n_j + (1-\alpha)m_j]c} > \frac{n_k}{n_j}$$

because  $n_k/n_j > m_k/m_j$ . This implies that

$$\frac{n_k + (q-1)n_k - [n_k + (1-\alpha)m_k]c}{n_j + (q-1)n_j - [n_j + (1-\alpha)m_j]c} > \frac{n_k}{n_j},$$

and

$$\Phi > \frac{n_k/N_k}{n_j/N_j} > \Phi^t$$

The wage differential is smaller in the second period for trained workers than the wage differential in the first period.

The wage differential between untrained workers at firm  $k$  and  $j$  in the second period is

$$\Phi^u = \frac{(1-\alpha)n_k/[ (1-\alpha)n_k + m_k ]}{(1-\alpha)n_j/[ (1-\alpha)n_j + m_j ]} = \frac{n_k}{n_j} \cdot \frac{(1-\alpha)n_j + m_j}{(1-\alpha)n_k + m_k}$$

Because  $1 - \frac{1}{2} > 1/2$ ,  $\Gamma(1 - \frac{1}{2}) > N_j/N_K$ , which implies

$$\Phi^u > \frac{n_k/N_k}{n_j/N_j} > \Phi^t$$

To see that  $\Gamma'(\frac{1}{2}) < 0$  we differentiate it with respect to  $\frac{1}{2}$ , which gives

$$\begin{aligned} \Gamma' &= \frac{[n_k + (1 - \frac{1}{2})m_k](n_j - m_j) - [n_j + (1 - \frac{1}{2})m_j](n_k - m_k)}{[n_k + (1 - \frac{1}{2})m_k]^2} \\ &= \frac{[n_k n_j \{ [1 + \frac{1-\rho}{\rho} \frac{m_k}{n_k}] (1 - \frac{m_j}{n_j}) - [1 + \frac{1-\rho}{\rho} \frac{m_j}{n_j}] (1 - \frac{m_k}{n_k}) \}]}{[n_k + (1 - \frac{1}{2})m_k]^2} \\ &= \frac{[n_k n_j \{ \frac{2-\rho}{\rho} [\frac{m_k}{n_k} - \frac{m_j}{n_j}] \}]}{[n_k + (1 - \frac{1}{2})m_k]^2}, \end{aligned}$$

which is strictly negative as  $m_k/n_k > m_j/n_j$

□

**Proof of Proposition 3.** This follows immediately from Claim 2 and 3, which shows that in any equilibrium, each firm offers a different wage and only one wage in the first period. This implies that firms offer higher wages hire more workers in the first period. Firms choices in the second period follow from Claim 1 and Lemma 1.

□

Table 1: Variable Definitions

| <b>Variable</b> | <b>Description</b>  |
|-----------------|---|
| Y               | Natural logarithm of real wage, deflated by CPI-U (1982–1984 = 100)   |
| ED_L12          | Less than 12 years of schooling (less than high school)   |
| ED_12           | Equal to 12 years of schooling (high school graduates)  |
| ED_1315         | Between 13 to 15 years of schooling (some college)  |
| ED_16           | Equal to 16 years of schooling (college graduates)  |
| ED_G16          | More than 16 years of schooling (More than college graduates)   |
| MARR_NM         | A dummy = 1 if the person is never married  |
| MARR_SP         | A dummy = 1 if the person is married with spouse present  |
| MARR_OT         | A dummy = 1 if the person is married with spouse not present  |
| UNEMP           | Local unemployment rate categories: 1: 3%; 2: 3%–5.9%; 3: 6%–8.9%; 4: 9%–11.9%; 5: 12–14.9%; 6: $\geq 15\%$ |
| NE              | A dummy = 1 if the work is in the Northeast region  |
| NC              | A dummy = 1 if the work is in the North Central region  |
| WEST            | A dummy = 1 if the work is in the West region   |
| SOUTH           | A dummy = 1 if the work is in the South region  |
| AFQT            | Armed forces qualification test percentile score  |
| AFQTSQ/100      | Square of AFQT divided by 100   |
| TENURE          | Total years of tenure with current employer   |
| TENURESQ/100    | Square of TENURE divided by 100   |
| EXP             | Total years of labor market experience  |
| EXPSQ/100       | Square of EXP divided by 100  |
| S_EST           | A dummy = 1 if in an establishment with less than 500 employees, 0 otherwise                                |
| L_EST           | A dummy = 1 if in an establishment with at least 500 employees, 0 otherwise                                 |
| TR              | A dummy = 1 if completed at least one on-the-job training spell with current employer, 0 otherwise          |
| TRS             | Interaction term of TR with S_EST   |
| TRL             | Interaction term of TR with L_EST   |
| OFF_TR          | A dummy = 1 if completed at least one off-the-job training spell with current employer, 0 otherwise         |
| L_TENURE        | Interaction term of TENURE with L_EST   |

See next page

TABLE 1. Variable Definitions (Continued)

| <b>Variable</b> | <b>Description</b>   |
|-----------------|--|
| L_TENURESQ/100  | Interaction term of TENURESQ/100 with L_EST  |
| IND1            | A dummy = 1 if in the mining ind. (SIC: 47–57), 0 otherwise                        |
| IND2            | A dummy = 1 if in the construction ind. (SIC: 67–77), 0 otherwise                  |
| IND3            | A dummy = 1 if in the manufacturing ind. (SIC: 107–398), 0 otherwise               |
| IND4            | A dummy = 1 if in the public utilities ind. (SIC: 407–479), 0 otherwise            |
| IND5            | A dummy = 1 if in the wholesale trade ind. (SIC: 507–588), 0 otherwise             |
| IND6            | A dummy = 1 if in the financial services ind. (SIC: 707–718), 0 otherwise          |
| IND7            | A dummy = 1 if in the business and repair services ind (SIC: 727–759), 0 otherwise |
| IND8            | A dummy = 1 if in the personal services ind. (SIC: 769–798), 0 otherwise           |
| IND9            | A dummy = 1 if in the public administration ind. (SIC: 907–937), 0 otherwise       |
| WEIGHT          | NLSY79 Sampling Weight   |

Table 2: Firm Size-Wage Relationship, Year 2002, by Industries

|  | <b>Firm Size (Number of Employees)</b> |              |                |             |
|--|--|--------------|----------------|-------------|
|  | <b>0–19</b>                            | <b>20–99</b> | <b>100–499</b> | <b>500+</b> |
| Agriculture, forestry, fishing, & hunting      | 26                                     | 27           | N/A            | N/A         |
| Mining   | 39                                     | 43           | 50             | 58          |
| Utilities                                      | 32                                     | 46           | 52             | 68          |
| Construction                                   | 33                                     | 40           | 44             | 47          |
| Manufacturing                                  | 31                                     | 35           | 37             | 44          |
| Wholesale trade                                | 39                                     | 41           | 43             | 51          |
| Retail Trade                                   | 21                                     | 27           | 29             | 19          |
| Transportation & Warehousing                   | 28                                     | 30           | 32             | 40          |
| Information                                    | 44                                     | 46           | 51             | 55          |
| Finance & insurance                            | 46                                     | 55           | 56             | 61          |
| Real estate & rental & leasing                 | 30                                     | 32           | 34             | 35          |
| Professional, scientific, & technical services | 44                                     | 54           | 58             | 56          |
| Management of companies & enterprises          | 66                                     | 50           | 52             | 73          |
| Administrative & support & waste management    | 29                                     | 27           | 23             | 25          |
| Educational services                           | 21                                     | 22           | 26             | 29          |
| Health care & social assistance                | 39                                     | 33           | 27             | 34          |

Table 3: Summary Statistics, Whole Sample

| <b>Variable</b> | <b># of Observations</b> | <b>Mean</b> | <b>Standard Deviation</b> | <b>Min</b> | <b>Max</b> |
|-----------------|--------------------------|-------------|---------------------------|------------|------------|
| LNW             | 8972                     | 6.77        | 0.49                      | 4.61       | 9.10       |
| ED_L12          | 9261                     | 0.13        | 0.33                      | 0          | 1          |
| ED_12           | 9261                     | 0.43        | 0.49                      | 0          | 1          |
| ED_1315         | 9261                     | 0.23        | 0.42                      | 0          | 1          |
| ED_16           | 9261                     | 0.19        | 0.39                      | 0          | 1          |
| ED_G16          | 9261                     | 0.04        | 0.19                      | 0          | 1          |
| NE              | 9285                     | 0.19        | 0.39                      | 0          | 1          |
| NC              | 9285                     | 0.33        | 0.47                      | 0          | 1          |
| WEST            | 9285                     | 0.15        | 0.36                      | 0          | 1          |
| SOUTH           | 9285                     | 0.32        | 0.47                      | 0          | 1          |
| UNEMP           | 9148                     | 2.59        | 0.88                      | 1          | 6          |
| MARR_NM         | 9317                     | 0.28        | 0.45                      | 0          | 1          |
| MARR_SP         | 9317                     | 0.60        | 0.49                      | 0          | 1          |
| MARR_OT         | 9317                     | 0.12        | 0.33                      | 0          | 1          |
| AFQT            | 8919                     | 56.25       | 28.29                     | 1          | 99         |
| TENURE          | 9155                     | 4.26        | 4.26                      | 0.02       | 24.92      |
| EXP             | 9318                     | 11.34       | 4.56                      | 0.35       | 23.00      |
| TR              | 9318                     | 0.19        | 0.39                      | 0          | 1          |
| OFF_TR          | 9318                     | 0.15        | 0.35                      | 0          | 1          |
| S_EST           | 9165                     | 0.83        | 0.38                      | 0          | 1          |
| L_EST           | 9165                     | 0.17        | 0.38                      | 0          | 1          |

Table 4: Sample Means for the whole sample, small establishments and large establishments

| <b>Variable</b> | <b>Whole Sample</b> | <b>Small Establishments</b> | <b>Large Establishments</b> |
|-----------------|---------------------|-----------------------------|-----------------------------|
| LNW             | 6.77                | 6.71                        | 7.06                        |
| ED_L12          | 0.13                | 0.14                        | 0.05                        |
| ED_12           | 0.43                | 0.46                        | 0.28                        |
| ED_1315         | 0.23                | 0.22                        | 0.24                        |
| ED_16           | 0.19                | 0.16                        | 0.34                        |
| ED_G16          | 0.04                | 0.02                        | 0.10                        |
| NE              | 0.19                | 0.18                        | 0.23                        |
| NC              | 0.33                | 0.33                        | 0.35                        |
| WEST            | 0.15                | 0.16                        | 0.12                        |

Table 5: Establishment Size-Wage Effects: OLS, Random Effects, and Fixed Effects Estimates

|              | OLS                  | Random Effects       | Fixed Effects        |
|--------------|----------------------|----------------------|----------------------|
| L_EST        | 0.146***<br>(0.012)  | 0.066***<br>(0.012)  | 0.039***<br>(0.012)  |
| ED_L12       | -0.066***<br>(0.015) | -0.065**<br>(0.029)  |                      |
| ED_1315      | 0.174***<br>(0.012)  | 0.161***<br>(0.023)  |                      |
| ED_16        | 0.378***<br>(0.014)  | 0.368***<br>(0.029)  |                      |
| ED_G16       | 0.501***<br>(0.025)  | 0.525***<br>(0.052)  |                      |
| AFQT         | 0.004***<br>(0.001)  | 0.003**<br>(0.001)   |                      |
| AFQTSQ/100   | -0.001<br>(0.001)    | -0.001<br>(0.001)    |                      |
| UNEMP        | -0.031***<br>(0.005) | -0.024***<br>(0.004) | -0.022***<br>(0.005) |
| TENURE       | 0.033***<br>(0.003)  | 0.029***<br>(0.002)  | 0.025***<br>(0.002)  |
| TENURESQ/100 | -0.118***<br>(0.018) | -0.124***<br>(0.015) | -0.121***<br>(0.015) |
| EXP          | 0.027***<br>(0.005)  | 0.030***<br>(0.004)  | 0.032***<br>(0.004)  |
| EXPSQ/100    | -0.021<br>(0.018)    | -0.017<br>(0.014)    | -0.017<br>(0.015)    |

**Note.** Dependent variable is log hourly real wage. Number of observations is 8,130. The other explanatory variables are regional dummies, marriage dummies, and industry dummies. The base group workers are full-time white males with 12 years of schooling, work in a small-sized establishment. \*\*\* stands for significance at 1% level, \*\* stands for significance at 5% level, \* stands for significance at 10% level.

Table 6: Return to Training by Establishment Size: OLS and Person Effects Models

|                | <b>OLS</b>           | <b>Random Effects</b> | <b>Fixed Effects</b> |
|----------------|----------------------|-----------------------|----------------------|
| L_EST          | 0.149***<br>(0.023)  | 0.064***<br>(0.018)   | 0.033*<br>(0.019)    |
| TR             | 0.068***<br>(0.013)  | 0.037***<br>(0.012)   | 0.030**<br>(0.012)   |
| TRL            | -0.066**<br>(0.026)  | -0.060***<br>(0.022)  | -0.057**<br>(0.023)  |
| ED_L12         | -0.066***<br>(0.015) | -0.065**<br>(0.029)   |                      |
| ED_1315        | 0.171***<br>(0.012)  | 0.160***<br>(0.023)   |                      |
| ED_16          | 0.374***<br>(0.014)  | 0.365***<br>(0.029)   |                      |
| ED_G16         | 0.497***<br>(0.025)  | 0.524***<br>(0.052)   |                      |
| AFQT           | 0.004***<br>(0.001)  | 0.003**<br>(0.001)    |                      |
| AFQTSQ/100     | -0.001<br>(0.001)    | -0.001<br>(0.001)     |                      |
| UNEMP          | -0.031***<br>(0.005) | -0.024***<br>(0.004)  | -0.022***<br>(0.005) |
| TENURE         | 0.031***<br>(0.003)  | 0.027***<br>(0.003)   | 0.023***<br>(0.003)  |
| L_TENURE       | 0.005<br>(0.007)     | 0.007<br>(0.006)      | 0.008<br>(0.006)     |
| TENURESQ/100   | -0.108***<br>(0.02)  | -0.116***<br>(0.016)  | -0.113***<br>(0.017) |
| L_TENURESQ/100 | -0.028<br>(0.045)    | -0.033<br>(0.035)     | -0.037<br>(0.035)    |
| EXP            | 0.026***<br>(0.005)  | 0.029***<br>(0.004)   | 0.032***<br>(0.004)  |
| EXPSQ/100      | -0.019<br>(0.018)    | -0.016<br>(0.014)     | -0.016<br>(0.015)    |

Table 7: Return to Training by Establishment Size: Person plus Job Match Effects Models

|                | <b>Random Effects</b> | <b>Fixed Effects</b> | <b>Two-level Mixed Model</b> |
|----------------|-----------------------|----------------------|------------------------------|
| L_EST          | 0.072***<br>(0.019)   | -0.021<br>(0.025)    | 0.054***<br>(0.018)          |
| TR             | 0.033***<br>(0.013)   | 0.015<br>(0.015)     | 0.029**<br>(0.012)           |
| TRL            | -0.041*<br>(0.022)    | -0.031<br>(0.024)    | -0.044**<br>(0.021)          |
| ED_L12         | -0.035*<br>(0.020)    |                      | -0.056*<br>(0.029)           |
| ED_1315        | 0.177***<br>(0.017)   |                      | 0.162***<br>(0.023)          |
| ED_16          | 0.406***<br>(0.021)   |                      | 0.377***<br>(0.029)          |
| ED_G16         | 0.561***<br>(0.040)   |                      | 0.532***<br>(0.052)          |
| AFQT           | 0.004***<br>(0.001)   |                      | 0.004***<br>(0.001)          |
| AFQTSQ/100     | -0.001<br>(0.001)     |                      | -0.001<br>(0.001)            |
| UNEMP          | -0.027***<br>(0.004)  | -0.020***<br>(0.006) | -0.025***<br>(0.004)         |
| TENURE         | 0.027***<br>(0.003)   | -0.091***<br>(0.027) | 0.025***<br>(0.003)          |
| L_TENURE       | 0.004<br>(0.005)      | 0.012**<br>(0.006)   | 0.005<br>(0.005)             |
| TENURESQ/100   | -0.098***<br>(0.016)  | -0.059***<br>(0.017) | -0.098***<br>(0.015)         |
| L_TENURESQ/100 | -0.031<br>(0.031)     | -0.067**<br>(0.032)  | -0.033<br>(0.030)            |
| EXP            | 0.028***<br>(0.004)   | 0.145***<br>(0.028)  | 0.029***<br>(0.004)          |
| EXPSQ/100      | -0.026*<br>(0.016)    | -0.045**<br>(0.021)  | -0.022<br>(0.015)            |

Table 8: Logit Models for Training Determination (Odds Ratios)

|              | <b>Logit</b>        | <b>Random Effects<br/>Logit</b> | <b>Fixed Effects Logit</b> |
|--------------|---------------------|---------------------------------|----------------------------|
| L_EST        | 2.176***<br>(0.160) | 2.276***<br>(0.319)             | 1.669***<br>(0.278)        |
| ED_L12       | 0.665***<br>(0.097) | 0.395**<br>(0.168)              |                            |
| ED_1315      | 1.562***<br>(0.130) | 3.700***<br>(0.935)             |                            |
| ED_16        | 1.271***<br>(0.120) | 2.441**<br>(0.859)              |                            |
| ED_G16       | 1.750***<br>(0.282) | 6.741***<br>(3.337)             |                            |
| AFQT         | 1.021***<br>(0.006) | 1.027<br>(0.018)                |                            |
| AFQTSQ/100   | 0.989**<br>(0.005)  | 0.986<br>(0.017)                |                            |
| UNEMP        | 0.961<br>(0.036)    | 0.968<br>(0.066)                | 0.993<br>(0.075)           |
| TENURE       | 1.250***<br>(0.026) | 1.509***<br>(0.054)             | 1.526***<br>(0.067)        |
| TENURESQ/100 | 0.451***<br>(0.055) | 0.398***<br>(0.083)             | 0.807<br>(0.249)           |
| EXP          | 1.322***<br>(0.053) | 1.736***<br>(0.113)             | 1.664***<br>(0.115)        |
| EXPSQ/100    | 0.451***<br>(0.068) | 0.200***<br>(0.048)             | 0.214***<br>(0.278)        |