


Price Delegation or Not? The Effect of Heterogeneous Sales Agents

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In this study, we examine the effect of the differences in both sales ability and reservation utility on the design of the pricing scheme and compensation contract under asymmetric information. Heterogeneity with ability-dependent reservation utility generates conflicted screening and pooling effects that preclude separating and pooling equilibria, respectively; with which agents may work harder under either centralized or delegated pricing scheme than if they were homogeneous and, in certain scenarios, no premiums (information rents) are paid. These findings are driven by the dynamics between the differences in agents' reservation utilities and in their effort costs or rewards that arise when their true types are concealed. We show that optimal separating contracts generate the same profit under centralized and delegated pricing because separating contracts under centralization retain the pricing flexibility of delegation. However, a certain form of pooling contract under delegated pricing can outperform the optimal pooling contract under centralization because the upside of pricing flexibility under delegation dominates the downside caused by reduced effort incentives. Under the optimal contracts, delegated pricing is as profitable to the firm as centralized pricing when the difference of reservation utilities is small or when the difference is large but the ability gap is small, and delegation is preferred when the difference of reservation utilities is moderate or when both the difference and the ability gap are large.

Key words: price delegation; sales compensation; agent heterogeneity; effort cost and reservation utility; separating and pooling contracts

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1. Introduction

Delegation of pricing authority is a critical issue in organization design for firms that rely on agents to sell products and services. Varied degrees of price delegation are observed in different industries. Stephenson et al. (1979) surveyed medical supplies and equipment trading firms and discovered that sales personnel have no, limited, and full pricing authorities in 29%, 48%, and 23% of the sample, respectively. Similar findings are reported for financial services, pharmaceutical, consumer goods, industrial goods industries (Hansen et al. 2008), and industrial machinery and electrical engineering sectors (Frenzen et al. 2010). The amount of superior customer demand information that sales agents have and

the form of compensation contract are suggested to be important factors that affect price delegation (Stephenson et al. 1979).

In an early study, Weinberg (1975) examined the effect of the form of compensation contract on delegation and suggested that price delegation benefits a firm and its agents when commissions for the latter are a percentage of the gross margin, rather than that of the sales revenue. Lal (1986) documented that delegation is more profitable for the firm than centralization if agents possess certain information that the firm does not know. Mishra and Prasad (2004) showed that centralization outperforms delegation when sales agents' private information about the stochastic part of demand can be revealed to the firm through their contract choice. Essentially, Lal (1986) and Mishra

and Prasad (2004) found a determinant of price delegation: agents' private information unknown to the firm.

Using data from a survey of 201 firms, Lo et al.

and compensation contract to make the heterogeneous sales force work effectively. Therefore, managers should assess the differences in agents' abilities and reservation utilities before choosing between centralized and delegated pricing. We extend our base model by considering uncertain demands, correlation across sales territories, and continuous type; and the main results of the base model remain qualitatively true under these variations.

The remainder of the study can be organized as follows. Section 2 presents the literature review. Section 3 defines the models for centralized and delegated pricing. Section 4 describes the contract menus for the two models and examines the firm's preference on delegation or centralization. Section 5 extends our base model. Section 6 concludes the study with a summarized discussion. All proofs are provided in an online supplement.

2. Literature Review

In an early work on sales agent price delegation, Weinberg (1975) stated that both the firm and the agent can benefit from price delegation when the marginal cost is constant and the commission is based on a percentage of the gross margin. Lal (1986) used an agency theory framework to show that price delegation is more profitable for the firm than price centralization when the salesperson possesses relevant private information that is unavailable to the firm. Joseph (2001) analyzed two factors that may affect the price delegation decision, namely, the endogenous sales behavior under price delegation and the amount of superior information that the sales agent possesses about a customer's willingness to pay; these factors are among the several ones that were suggested by Stephenson et al. (1979). Joseph (2001) found that if the sales effort cost of pursuing high-quality customers is either relatively low or relatively high, then full price delegation is optimal, whereas limited price delegation is optimal for the intermediate levels of such effort cost. Bhardwaj (2001) investigated how the competition in price and sales effort affects delegation decisions. He found that firms should delegate when the price competition is intense, but centralized pricing is preferable under high levels of sales effort competition.

Mishra and Prasad (2004, 2005) demonstrated that in monopolized and competitive settings, centralized pricing performs at least as well as delegated pricing (for the firm) if the sales agent's private information is revealed by his choice of contract. They also noted that the nature of the private information (i.e., about the agent's selling ability or market condition) may not affect the results stemming from the firm's price delegation decision with homogeneous reservation

utility of agents. Nagar (2002) used survey data to empirically establish that lower-level managers who are given more pricing authority receive higher power incentive schemes, and managers with greater abilities receive more incentive compensation. Lo et al. (2016) showed that sales agents with greater abilities (i.e., experiences and skills) are granted more pricing authority. Simester and Zhang (2014) examined the "internal lobbying" phenomenon when sales representatives possess private information about demands, and they derived conditions under which the firm prefers such lobbying over price delegation. Lim and Ham (2014) conducted a laboratory economics experiment to examine the relationship between price delegation and managerial profits. Their experiment revealed that price delegation is more frequently selected when the firm awards a bonus to sales agents after observing their decisions. This study is different from the above mentioned works in that we consider the heterogeneity of sales agents in terms of both sales ability and reservation utility and show that type-dependent reservation utility has a significant effect on the firm's pricing delegation decision.

The literature on sales force compensation is extensive. Basu et al. (1985) considered a homogeneous and risk-averse sales force in the context involving moral hazard and proposed a nonlinear optimal compensation plan. However, Lal and Staelin (1986) discovered that the nonlinear compensation contract described by Basu et al. (1985) may not be optimal if the sales force is heterogeneous, and information asymmetry is present. Lal and Srinivasan (1993) discussed linear compensation plans for single- and multi-product sales forces. By assuming *ex ante* symmetric information, they demonstrated through comparative statics that the improvements in alternative job opportunities can increase salaries but cannot affect commission rates, which determine the sales effort. By contrast, our model features the type-dependent reservation utility that affects not only agents' payments but also their effort decisions. As previously mentioned, Rao (1990) proposed a menu of quota-based compensation plans for a heterogeneous sales force with identical reservation utility and private information on abilities. He further showed that only the lowest agent type does not receive information rent and only the highest one delivers the first best effort. Raju and Srinivasan (1996) described scenarios where the performance of quota-based contracts nearly matches that of Basu et al. (1985) optimal plan.

Park (1995) and Kim (1997) demonstrated that bonuses awarded for meeting the sales quota may induce the first best efforts of agents when binding participation constraints are present in a moral

hazard problem. In a similar setting, Oyer (2000) demonstrated that a quota-based plan may result in the first best efforts of agents who do not face binding participation constraints. Kala and Shi (2001) and Murthy and Mantrala (2005) investigated the use of sales contests as a relative performance-based incentive scheme. In this study, we design a compensation contract for a heterogeneous sales force characterized by type-dependent reservation utility under different pricing schemes. We show that both high- and low-type agents can make the first best effort without rent under certain conditions.

Several scholars have considered different sales force incentive problems. Mantrala et al. (1994) studied the compensation of a heterogeneous sales force that sells multiple products. Joseph and Thevaranjan (1998) examined the roles played by monitoring and incentivizing sales agents in a compensation scheme. Misra et al. (2005) considered agents' risk attitudes in the firm's compensation of a heterogeneous sales force. Caldieraro and Coughlan (2009) showed how the interaction between territory allocation and sales force compensation affects the firm's profit. Chen (2000, 2005) explored sales force incentive problems in connection with inventory decisions. Chen and Xiao (2012) studied a three-layer supply chain, in which a manufacturer sells a product through a reseller, who then relies on its own sales agent to sell in the end market. Yang et al. (2013) examined the effect of emotions on the choice between sales contests and quotas when sales territories are imbalanced. Chu and Lai (2013) investigated sales force contracting when excess demands lead to lost sales, but the demand information is censored by the inventory level. Dai and Jerath (2013) considered the firm's joint decisions regarding inventory level and sales force contract design. Chen et al. (2016) compared forecast-based contracts with menus of linear contracts when sellers exert effort to acquire information on market conditions and increase demands. Rubel and Prasad (2016) proposed a dynamic model for the design of sales force compensation plans when the effect of the selling effort on sales in one period persists for several periods. In contrast to the existing research, we focus on the effect of type-dependent reservation utility on the pricing scheme selection and compensation contract design of a firm with a heterogeneous sales force.

Reservation utility of type dependence has been investigated in the economics literature, for example, Lewis and Sappington (1989), Maggi and Rodriguez-Clare (1995), Laffont and Tirole (1990), Jullien (2000), Armstrong and Sappington (2004). These works analyzed the properties of the optimal contract when the agent's reservation utility relates to the type. One of the characteristics of type-dependent reservation

utility model is that the incentive compatibility (IC) and individual rationality (IR) constraints of all types can be binding differently. Recently, some works considered the type-dependent reservation utility in the operations management, such as Chakravarty and Zhang (2007), Cakanyildirim et al. (2012) and Can et al. (2019). Our research develops the pricing scheme and compensation contract in the context of sales force management with type-dependent reservation utility, and provides insights into the scenario when heterogeneous sales agents are employed.

3. Model

The manager (she) of a firm that employs heterogeneous sales agents

$$s = s_0 + \theta e - bp, \quad (1)$$

where s_0 is the market potential,² b is the price elasticity, and s_0 and b are positive. The specification of a tractable linear response function is reasonable for many market situations and is common in the literature (Bhardwaj 2001, Chen 2005).

For clarity, we restrict the discussion to two agent types:³ high (H) and low (L) types with respective abilities θ_H and θ_L , where $\theta_H > \theta_L > 0$. R_i is used to represent the reservation utility of a type- i agent, where $i = H$ or L and $R_H \geq R_L > 0$. The sales force may comprise many individual agents, and each is either a high type or a low type. The proportions ρ and $1 - \rho$ ($\rho \in (0, 1)$) of the high- and low-type agents in the job market, respectively, are common knowledge. We assume that $2b > \theta_H^2$ and s_0 is sufficiently large to ensure that for any R_i , the firm's profit is nonnegative.⁴ These assumptions are common in the literature (Laffont and Tirole 1988).

Let $c(e)$ denote the *effort cost* or the cost of exerting effort level e . We assume that $c(e)$ increases with e , and at an increasing rate (Basu et al. 1985):

$$c(e) = e^2/2. \quad (2)$$

Let $\{t(q, \theta), p(\theta)\}$ be the contracts under centralized pricing, where q is the sales quota, t is the agents' compensation, and p is the price. The contracts specify the product price and the amount that the firm will pay to the agent for meeting the quota. Given that the

4. Main Results

4.1. Contracts under Centralized Pricing

In this section, we first derive the optimal separating contracts under centralized pricing. Apart from the ability to determine the payments to agents for realizing the quotas, the separating contracts have the self-selection feature. On the basis of the proposed deterministic demand function, according to Harris and Townsend (1981), the optimal scheme under centralized pricing can be described using contracts $\{t_H, q_H, p_H\}$ and $\{t_L, q_L, p_L\}$. Given that the optimal separating contracts are not always possible, we also examine the pooling contract (i.e., unique contract $\{t, q, p\}$). The comparison of the optimal separating and pooling contracts can establish an optimal strategy under centralization.

We use $r > 1$ to denote the ability ratio of the high-type to the low-type agent, $r = \theta_H/\theta_L$ and $\Delta R \geq 0$ to denote the difference of reservation utilities between the two agent types, $\Delta R = R_H - R_L$. To facilitate the presentation of the optimal decisions, the following terms are defined.

$$\left(\begin{array}{l} \psi_1 = \frac{1-\rho}{1-\rho/r^2}, \quad \psi_2 = \frac{\rho}{1-(1-\rho)r^2}, \quad r_c = \sqrt{\frac{1}{1-\rho} \left(1 - \frac{\rho\theta_H^2}{2b}\right)} \\ K_1 = \frac{1}{2}(1-r^{-2}) \left(\frac{s_0\psi_1\theta_L}{2b-\psi_1\theta_L^2}\right)^2, \quad K_2 = \frac{1}{2}(1-r^{-2}) \left(\frac{s_0\theta_L}{2b-\theta_L^2}\right)^2 \\ K_3 = \frac{1}{2}(r^2-1) \left(\frac{s_0\theta_H}{2b-\theta_H^2}\right)^2, \quad K_4 = \frac{1}{2}(r^2-1) \left(\frac{s_0\psi_2\theta_H}{2b-\psi_2\theta_H^2}\right)^2. \end{array} \right) \quad (7)$$

It is easy to show that $0 < \psi_1 < 1$ and $K_1 < K_2 < K_3$, and $\psi_2 > 1$ and $K_3 < K_4$ when $r < r_c$. In addition, these values of K constitute four distinct thresholds for the reservation utility difference, and r_c serves as a threshold for the ability ratio under centralized pricing. The following proposition summarizes the decisions under the optimal separating and pooling contracts.

PROPOSITION 1. *Under centralized pricing: (A) the optimal separating contracts exist when (i) $\Delta R \leq K_1$, (ii) $K_2 \leq \Delta R \leq K_3$, (iii) $\Delta R \geq K_4$ and $r < r_c$; (B) the optimal pooling contract exists for any value of ΔR , except when $K_2 < \Delta R < K_3$. The decisions with respect to the optimal separating and pooling contracts are presented in Tables A1 and A2 in the Appendix, respectively.*

Thresholds K_1 and K_2 are defined as follows: $K_1 = \frac{1}{2}(1-r^{-2}) \left(\frac{s_0\psi_1\theta_L}{2b-\psi_1\theta_L^2}\right)^2$ and $K_2 = \frac{1}{2}(1-r^{-2}) \left(\frac{s_0\theta_L}{2b-\theta_L^2}\right)^2$.

ΔR	Contract	Pr m	Pr m	rt	rt
ΔR		P_H	P_L	H	L
$\Delta R \leq K_1$	Separating	$K_1 - \Delta R$	0	Same	Lower
$K_1 < \Delta R < K_2$	Pooling-L	$K_2 - \Delta R$	0	Lower	Same
$K_2 \leq \Delta R \leq K_3$	Separating	0	0	Same	Same
$K_3 < \Delta R < K_4$	Pooling-H	0	$\Delta R - K_3$	Same	Higher
$\Delta R \geq K_4$	Separating	0	$\Delta R - K_4$	Higher	Same
	Pooling-H	0	$\Delta R - K_3$	Same	Higher

that in the optimal contract for homogeneous agents (with ability θ_i), agents' optimal sales effort is calculated as $s_0\theta_i/(2b - \theta_i^2)$.

When $\Delta R \leq K_1$, the optimal contracts are separating ones, and the high-type agent receives a positive premium, whereas no premium is offered to the low-type agent. The premium $K_1 - \Delta R$ increases with the low-type agent's quota. Compared with that in the homogeneous case, the quota for the low-type agent under this scenario (low quota q_{L1}^*) is distorted downward to reduce the premium; such distortion also reduces the low-type agent's effort. When $K_1 < \Delta R < K_2$, the optimal contract is a pooling one for the low-type agent, and the high type receives a premium (because he needs less effort to reach the quota). When $K_2 \leq \Delta R \leq K_3$, no premium is necessary under the optimal contracts (separating), and both agent types exert the same effort as if they were homogeneous. When $K_3 < \Delta R < K_4$ or when $\Delta R \geq K_4$ and $r \geq r_c$, the optimal contract is a pooling one for the high type. In this case, the low-type agent receives a positive premium and exerts greater effort than in the absence of a premium. When $\Delta R \geq K_4$ and $r < r_c$, the optimal contracts become separating ones, and the low-type agent receives a positive premium that decreases with the high-type agent's quota. Therefore, compared with the homogeneous case, the firm sets a higher quota (high quota q_{H2}^*) for the high-type agent to reduce the low-type agent's premium and thus encourages the former to increase his effort.

For a heterogeneous sales force with a common reservation utility, Rao (1990) found that all, except the agent with the lowest ability receive a premium, and all, except the agent with the highest ability expend less effort than the agents who were members of a homogeneous sales force. However, this conclusion is not applicable for our setup with type-dependent reservation utility. Under centralized pricing, when $K_2 \leq \Delta R \leq K_3$, both agent types receive no premium and work as hard as they would if the sales forces were homogeneous. When $\Delta R > K_3$, the low-type agent receives a positive premium, whereas the high-type one receives none; two agent types can

work as hard as or even harder than they would if the sales forces were homogeneous.

For a general principal-agent problem with a continuous type of reservation utility relation, Lewis and Sappington (1989) found that the optimal contract involves pooling, and Maggi and Rodriguez-Clare (1995) showed that the condition when the pooling can occur depends on the relationship between reservation utility and type. Our result reveals explicitly how the optimal contracts (separating or pooling) rely on the difference of reservation utilities, and we only require a high reservation utility for a high-type agent.

4.2. Contracts under Delegated Pricing

In this subsection, we consider problem P_d . Examining the optimal separating contracts for P_c , we can propose the following possible solution for P_d ($i = H$ or L):

$$t_i(s, p) = \begin{cases} t_i^* & \text{if } p = p_i^* \text{ and } s = q_i^* \\ t_0 & \text{otherwise,} \end{cases}$$

where $\{t_i^*, q_i^*, p_i^*\}$ are from the optimal separating contracts for P_c (Table A1), and t_0 is sufficiently small and cannot satisfy agents' reservation utilities. Clearly, when $\{t_H(s, p), t_L(s, p)\}$ is offered, a high-type agent will choose $t_H(s, p)$ with pricing at p_H^* and realizing sales q_H^* , whereas a low-type agent will choose $t_L(s, p)$ with pricing at p_L^* and realizing sales q_L^* .

In other words, when pricing is delegated to the agent, the firm can set the contract such that if the price desired by the firm (under centralization) is not selected by the agent, the compensation to the agent is less than his reservation utility. Since the same price and realized sales can be anticipated under price delegation, the firm will achieve the same profit under either price delegation or price centralization. Similar arguments are used by Lal (1986) and Mishra and Prasad (2004). In summary, on the basis of the deterministic demand function, when the optimal separating contracts exist under centralized pricing (delegated pricing), the firm can design the optimal separating contracts under delegation (centralization) to realize the same profit.

However, under centralized pricing for some reservation utility difference ΔR , the optimal separating contracts do not exist due to the conflicted screening effect (Table 1). When the optimal contract under centralization is the pooling contract, the performance of price centralization relative to price delegation remains unclear. Similar to the method of Lal (1986), we will not solve for the optimal solution under delegated pricing, but instead develop a feasible solution for the firm to provide reference for selecting centralized or delegated pricing.

We propose the following contract form, $t(s, p) = \alpha + (p - y) \times s$, where α is the fixed compensation awarded to the agent, and y is the share received by the firm from the agent for each unit of sales. This form is commonly adopted under price delegation (e.g., Bhardwaj 2001), and we refer to it as margin-based commission (MBC) contract since $p - y$ denotes the commission that the agent obtains for each sale. Under this form, the pair of contracts offered by the firm becomes $\{(\alpha_H, y_H), (\alpha_L, y_L)\}$, and substituting them into the firm's problem \mathbf{P}'_d yields the following \mathbf{P}'_d .

$$\begin{aligned} \mathbf{P}'_d : \max \Pi_d(\alpha_H, y_H, \alpha_L, y_L) &= \rho(y_H \times s_{HH} - \alpha_H) + (1 - \rho)(y_L \times s_{LL} - \alpha_L). \\ (I) \quad &\alpha_H + (p_{HH} - y_H)s_{HH} - c(e_{HH}) \geq R_H \\ (II) \quad &\alpha_L + (p_{LL} - y_L)s_{LL} - c(e_{LL}) \geq R_L \\ \text{s.t. (III)} \quad &\alpha_H + (p_{HH} - y_H)s_{HH} - c(e_{HH}) \geq \alpha_L + (p_{HL} - y_L)s_{HL} - c(e_{HL}). \\ (IV) \quad &\alpha_L + (p_{LL} - y_L)s_{LL} - c(e_{LL}) \geq \alpha_H + (p_{LH} - y_H)s_{LH} - c(e_{LH}) \\ (V) \quad &(p_{ix}, e_{ix}) = \operatorname{argmax} \alpha_x + (p_{ix} - y_x)s_{ix} - c(e_{ix}), \quad i, x = H \text{ or } L \end{aligned} \tag{8}$$

Before presenting the results, the following terms are defined.

$$\left\{ \begin{aligned} V_1^s &= \frac{s_0^2(\theta_H^2 - \theta_L^2)(2b - \theta_H^2)}{2(2b - \theta_L^2)[2b - \theta_H^2 + \rho(\theta_H^2 - \theta_L^2)/(1 - \rho)]^2}, \\ V_2^s &= \frac{s_0^2(\theta_H^2 - \theta_L^2)(2b - \theta_L^2)}{2(2b - \theta_H^2)[2b - \theta_L^2 - (1 - \rho)(\theta_H^2 - \theta_L^2)/\rho]^2}, \\ V_1^p &= \frac{s_0^2(\theta_H^2 - \theta_L^2)[2b - (1 - \rho)\theta_H^2 - \rho\theta_L^2]^2}{2(2b - \theta_H^2)(2b - \theta_L^2)[2b - (1 - 2\rho)\theta_H^2 - 2\rho\theta_L^2]^2}, \\ V_2^p &= \frac{s_0^2(\theta_H^2 - \theta_L^2)[2b - (1 - \rho)\theta_H^2 - \rho\theta_L^2]^2}{2(2b - \theta_H^2)(2b - \theta_L^2)[2b - 2(1 - \rho)\theta_H^2 + (1 - 2\rho)\theta_L^2]^2}, \\ r_d &= \sqrt{1 + \rho(2b - \theta_L^2)/[(1 - \rho)\theta_L^2]}. \end{aligned} \right. \tag{9}$$

We can verify that $V_1^s < V_1^p < V_2^p$. In addition, $V_2^p < V_2^s$ if $r < r_d$.

PROPOSITION 2. For MBC contract $t(s, p) = \alpha + (p - y) \times s$ under price delegation: (A) a unique pair of optimal separating plans exists provided that (i) $\Delta R \leq V_1^s$ or (ii) $\Delta R \geq V_2^s$ and $r < r_d$; otherwise, no optimal separating plans exist; and (B) a unique optimal pooling plan exists except for $< \Delta R < K_2^s$. The optimal decisions in the separating and pooling plans are presented in Tables A3 and A4, respectively.

For MBC contract $t(s, p) = \alpha + (p - y) \times s$, the optimal separating plans (i.e., $\{\alpha_H, y_H\}$ and $\{\alpha_L, y_L\}$ in Table A3) show that $y_H^* = 0$ and $\alpha_H^* < 0$ when

$\Delta R \leq V_1^s$, that is, the firm does not collect revenue from each unit of sales, instead the agent should pay a lump sum to the firm for the total quantity he intends to sell (i.e., buy out from the firm and then sell to customers). The implication of this scenario is that if the reservation utility difference is small, then the firm should offer the high-type agent a buyout contract, and the low-type agent a regular contract (i.e., $y_L^* > 0$). However, if the reservation utility difference is large and the ability ratio is small, the low-type agent is offered a buy-

out contract. In this case, the high-type agent is offered an "enhanced" buyout contract, where he receives a bonus from the firm for each unit of sales ($y_H^* < 0$). It is interesting that the firm can separate different agent types only by granting one or both agent types total sales control (i.e., offering a buyout contract when the pricing has already been delegated). The expression V_1^s (V_2^s) is the difference between the reward of the high-type agent and the reward of the low-type agent when the selected contract is intended for the low (high) type. Similar to the case of centralized pricing, V_1^s and V_2^s serve as the thresholds of the reservation utility difference that determine if separating plans are possible. The conflicted screening effect appears when (i) $V_1^s < \Delta R < V_2^s$ and (ii) $\Delta R \geq V_2^s$ and $r \geq r_d$.

When the conflicted screening effect arises, the firm should consider the delegated pooling MBC contract $\{\alpha, y\}$. Note that for $\Delta R \leq V_1^p$ ($\Delta R \geq V_2^p$), the IR constraint for the low- (high-) type agent is binding (from the proof of Proposition 2 in the Appendix). This result implies that under the respective conditions, the optimal pooling MBC contract is essentially designed for either agent type (i.e., the pooling of the low/high-type agent).

Similarly, V_1^p (V_2^p) is the difference between the rewards of the high- and low-type agents when the optimal pooling MBC contract is of the low (high) type. For convenience, we refer to the V function as the reward difference under delegated pricing. When $V_1^p < \Delta R < V_2^p$, no pooling MBC contract can simultaneously satisfy the two IR constraints due to the conflicted pooling effect. Therefore, under delegated

pricing, neither optimal separating nor pooling MBC contracts exist when $V_1^p < \Delta R < V_2^p$ because the conflicted screening and conflicted pooling effects are both operative. When $\Delta R \leq V_1^s$ or when $\Delta R \geq V_2^s$ and $r < r_d$, the optimal separating and pooling MBC contracts can exist. Under these circumstances, the firm performs better with the former than with the latter. Table 2 summarizes the optimal MBC contracts under delegated pricing for the entire spectrum of the reservation utility difference. Similar to centralization, the pooling MBC contract can be adopted under delegation only when separating ones are not available.

Table 2 also presents the premiums received by the two agent types with the optimal MBC contracts and compares the respective efforts the agents exert with the efforts if the agents were part of a homogeneous sales force. From Proposition 2, the optimal effort of type- i agent weakly decreases in y_i because y_i is the per unit profit that the firm receives from the agent. When $\Delta R \leq V_1^s$, separating MBC contracts are offered, and the firm sets a positive y_L to reduce the premium received by the high-type agent, although at the cost of the lower effort from the low-type one. When $V_1^s < \Delta R \leq V_1^p$, however, the firm offers a pooling MBC contract designed for the low-type agent and sets a positive y to reduce the premium given to the high-type agent, consequently garnering a reduced effort from two types. When $V_2^p \leq \Delta R < V_2^s$, a pooling MBC contract for the high-type agent is offered, and the low-type agent receives a positive premium. In this case, the firm sets $y < 0$ for the optimal plan (i.e., a buyout contract) to minimize the premium, and both agent types exert higher efforts than if they were part of a homogeneous sales force. When $\Delta R \geq V_2^s$ and $r < r_d$, separating MBC contracts are offered, and the low-type agent receives a positive premium. To reduce this premium, the firm (i) sets $y_H < 0$, which motivates the high type to exert more effort than in the homogeneous agents scenario, and (ii) sets $y_L = 0$, which motivates the low type to exert the same effort as in that scenario. If $r \geq r_d$, then a pooling MBC contract is optimal for $\Delta R \geq V_2^s$, which is the same as that for $V_2^p \leq \Delta R < V_2^s$.

In conclusion, under delegated pricing with MBC contract, if $\Delta R \geq V_2^p$: (a) a low-type agent always

receives a positive premium, whereas a high-type agent receives none and (b) the high- and low-type agents always work harder or equally hard, as they would if the sales forces were homogeneous. Thus, irrespective of whether the firm’s pricing scheme is delegated or centralized, either agent type (high or low) with type-dependent reservation utility may receive zero premium and exert the same or greater effort than if he were a part of a homogeneous sales force.

4.3. Delegated or Centralized

To determine the right pricing scheme, we compare the performances of the contracts under centralized and delegated pricing. It is easy to verify for the K and V thresholds (i.e., effort cost and reward differences), that $K_2 < V_2^p$. For the ability ratio thresholds, $r_c < r_d$. The firm’s pricing strategy and contract choice can now be identified from the findings in sections 4.1 and 4.2.

PROPOSITION 3. (A) When the centralized optimal contracts are separating contracts for (i) $\Delta R \leq K_1$, (ii) $K_2 \leq \Delta R \leq K_3$, or (iii) $\Delta R \geq K_4$ and $r < r_c$, centralization and delegation can perform the same for the firm. (B) When the centralized optimal contract is pooling contract, delegation with the optimal MBC contract $t(s,p) = \alpha + (p - y) \times s$ performs better than centralization.

With the optimal separating contracts under centralization, the firm has the flexibility to set different prices for different agent types. This allows the firm to anticipate the agent’s pricing under delegation and set the anticipated price of different agent types in the centralized contract. Therefore, the optimal centralized and delegated separating contracts perform the same for the firm.

Note that the conflicted screening effect arises in certain ranges of the reservation utility difference and ability ratio, which excludes the existence of the optimal separating contracts under centralized pricing. In such a case, the optimal contract under centralization is the pooling one. However, under delegated pricing, for the MBC contract, the conflicted screening effect does not arise under certain conditions within the same ranges. Note that the optimal separating MBC contracts can always generate higher profit for the

Range of ΔR	Contract Type	High-type Agent Premium (P_H)	Low-type Agent Premium (P_L)	High-type Agent Effort (e_H)	Low-type Agent Effort (e_L)
$\Delta R \leq V_1^s$	Separating	$V_1^s - \Delta R$	0	Same	Lower
$V_1^s < \Delta R \leq V_1^p$	Pooling-L	$V_1^p - \Delta R$	0	Lower	Lower
$V_1^p < \Delta R < V_2^p$	u r r u m	N/A	N/A	N/A	N/A
$V_2^p \leq \Delta R < V_2^s$	Pooling-H	0	$\Delta R - V_2^p$	Higher	Higher
$\Delta R \geq V_2^s$	$r < r_d$: Separating	0	$\Delta R - V_2^s$	Higher	Same
	$r \geq r_d$: Pooling-H	0	$\Delta R - V_2^p$	Higher	Higher

firm than the optimal pooling one (Table 2). Therefore, to determine centralization or delegation when the optimal contract under centralization is pooling, we should first compare between centralized pooling and delegated pooling (of MBC contract).

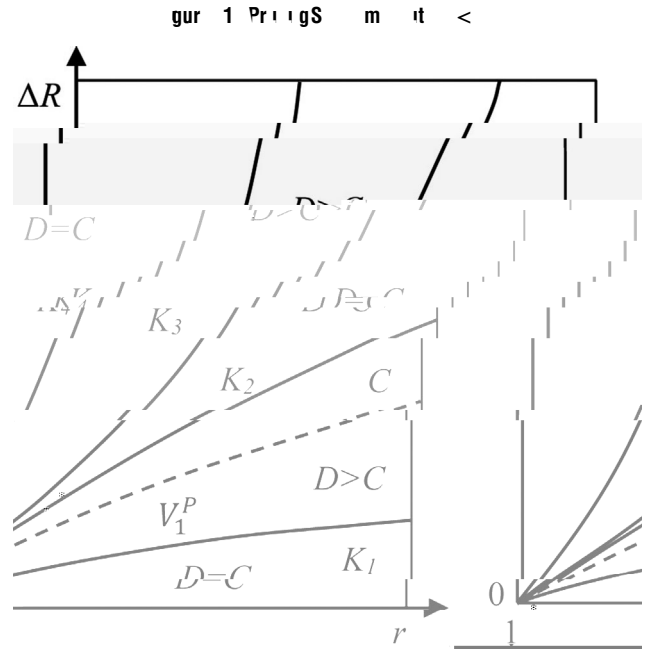
With delegated pooling, different agent types can set different prices despite having a single contract. By contrast, there is only a single price with centralized pooling. Thus, delegated pooling allows for greater pricing flexibility than centralized pooling. While, the comparison of Propositions 1 and 2 shows that the low-type agent always exerts less effort under delegated optimal pooling MBC contract than under centralized optimal pooling contract. Therefore, choosing between delegated and centralized pooling requires an evaluation of the trade-off between the benefit of pricing flexibility and the cost of reducing the incentive for sales effort.

PROPOSITION 4. *When the pooling contract is offered under both pricing schemes, the firm can benefit from selecting delegated pricing (with the optimal MBC contract $t(s,p) = \alpha + (p - y) \times s$) over centralized pricing (with the optimal pooling contract).*

Based on the fact that the optimal separating MBC contracts (if available) work better than the pooling one, and together with Proposition 4, we have a full explanation of Proposition 3(B). Figure 1 illustrates the results of Proposition 3 when the ability ratio is small (i.e., $r < r_c$), where C and D represent centralization and delegation, respectively. When $r \geq r_c$, in the region $\Delta R \geq K_4$, delegation with the optimal MBC contracts always works better than centralization with the optimal pooling contract. In the region $V_1^P < \Delta R < K_2$, the firm selects centralization because there is no equilibrium MBC contract under delegation.

Lal (1986) showed that delegation and centralization are identical to the firm when there is no information asymmetry between the firm and the agent; while when the agent has more precise information about demand, delegation is preferred by the firm. The private information in Lal (1986) is acquired after the agent signs the contract and exerts effort. Different from Lal (1986), in our model, the agent possesses private information on ability and reservation utility (type-dependent) before signing the contract. Our results show that when there is asymmetric information between the firm and the agent, delegation and centralization can also work identically for the firm under certain conditions.

Mishra and Prasad (2004) considered the same sequence of events as in our model, but the agents in their model have the same reservation utility. They discovered that the performance of the centralized



separating contracts for the firm is at least as good as that of the delegated separating contracts. Our result of Proposition 3(A) extends their findings in the scenario of type-dependent reservation utility when the difference of reservation utilities is small or when the difference is large but the ability gap is small, that is the conflicted screening effect does not appear under centralization. While when a conflicted screening effect is present under centralized pricing, the optimal contract becomes the pooling one. In this scenario, delegated pricing with the optimal separating MBC contracts can eliminate this effect when the difference of reservation utilities is moderate (i.e., $K_1 < \Delta R \leq V_1^P$) or large with moderate ability ratio (i.e., $\Delta R \geq V_2^P$ and $r_c \leq r < r_d$); delegation with the optimal pooling MBC contract performs better than centralization when $V_1^P < \Delta R < \min\{V_1^P, K_2\}$ or $\Delta R \geq V_2^P$ and $r \geq r_d$.

Lo et al. (2016) mentioned that agents who sell similar industrial equipment products are typically paid in accordance with the same compensation plan, which is not tailored to individual agents' characteristics. They also highlight that under the same contract, the more capable sales agents are granted higher pricing authority. The findings of Mishra and Prasad (2004) regarding the choice of centralization is based on the assumption that the firm designs different contracts for different types of sales agents. Hence, their analysis cannot explain the observation of Lo et al. (2016) regarding a unique contract with delegation. Our results, which are derived from the perspective of type-dependent reservation utility, can provide an explanation for the phenomenon where the firm offers a unique contract to agents

with different abilities while delegating the pricing decision.

5. Extensions

5.1. Pricing Scheme and Compensation under Sales Uncertainty

The deterministic demand of the base model leads to the problem of false moral hazard, since the firm can infer the agent's effort from the realized sales and the prices charged.⁵ In this subsection, by relaxing this assumption, we examine how sales uncertainty affects the firm's decisions and our main findings in section 4.

Now consider the uncertain realized sales \tilde{s} :

$$\tilde{s} = s + \varepsilon = s_0 + \theta e - bp + \varepsilon, \quad (10)$$

where ε represents the random noise with $E(\varepsilon) = 0$. The additive form of the uncertainty is commonly used in literature (Holmstrom and Milgrom 1991). Moreover, ε is independent of agents. Considering the presence of uncertainty, \tilde{s} is observed (not s of

same across territories. For simplicity, we assume a unidirectional and exogenous cross-territory effect (e.g., Abhishek et al. 2016), which can be modeled through the realized sales for territories A and B:

$$s_A = s_{0A} + \theta_A e_A - bp + \tau s_B \quad \text{and} \quad s_B = s_{0B} + \theta_B e_B - bp,$$

where subscripts A and B represent territory A and B, respectively, and τ , $\tau \in [-1, 1]$ denotes the correlation across the territories and represents the change in the sales in territory A imposed by the unit sales in territory B. Provided that the ability and reservation utility of the agent in territory A are common knowledge, we concentrate on the centralization or delegation decision of the firm in territory B. Under centralized pricing, the firm decides the price(s) and compensation contracts to maximize the total expected profit from the two territories. Under delegated pricing, given that the agent sets the price in territory B, the contract for territory A also depends on the price in B due to the same price strategy. By solving the firm's problems under centralization and delegation, we obtain Proposition 6.

PROPOSITION 6. *The results from our base model remain qualitative when a correlation is present among the sales territories. The regions (of reservation utility difference) where the conflicted screening effect exists shrink when the positive correlation increases or when the negative correlation decreases.*

When $\tau > 0$, the correlation across sales territories is positive, which means that each unit of sales in the new territory B generates τ units of additional sales in territory A. This phenomenon occurs due to the “network effect” (Abhishek et al. 2016). Otherwise, the sales in territory B negatively affects territory A (i.e., $\tau < 0$). Proposition 6 first asserts that the results from the base model hold qualitatively. The optimal separating contracts perform equally under centralized and delegated pricing. Delegation with the optimal MBC contracts can perform better than centralization with the optimal pooling contract if the conflicted screening effect exists under centralized pricing. Note that the increase in the correlation signifies a strong positive correlation or a large absolute value of the negative correlation ($|\tau|$). This proposition also shows that the regions, where delegated pricing with the optimal MBC contracts works better than the centralized optimal pooling contract, shrink if the positive correlation increases (i.e., $\tau > 0$ and τ increases) or the negative correlation decreases (i.e., $\tau < 0$ and $|\tau|$ decreases). That is, when the sales in territory B lead to more increase (for $\tau > 0$) or less decrease (for $\tau < 0$) in sales in territory A, in more regions of reservation utility difference ΔR , the firm can avoid the discrimination

between centralization and delegation because the two pricing schemes with optimal separating contracts can perform equally.

5.3. Continuous Type

In this subsection, we check how our main results may change when the type distribution is continuous. Our main findings with two discrete types show that the optimal contracts under centralized pricing can be separating contracts or pooling contract. When the optimal contracts under centralization are separating, centralization and delegation perform equally since the centralized pricing can be set according to the agent type. When the optimal contract under centralization is pooling, delegation performs better than centralization because of the flexibility of utilizing agent type information. Consider the problem with continuous type and type-dependent reservation utility. When centralized optimal contract are separating, we can show, following Mishra and Prasad (2004), that centralization works at least as well as delegation because the centralized pricing can be made for each type individually. As such, we remain to see if a continuous region (of type) exists within which the centralized optimal contract is pooling, and how centralized and delegated pooling contracts perform.

Consider a general type distribution $F(\theta)$ with density $f(\theta) > 0$ over $[\underline{\theta}, \bar{\theta}]$ ($0 < \underline{\theta} < \bar{\theta}$), and $\frac{F(\theta)}{f(\theta)}$ increasing in θ whereas $\frac{1-F(\theta)}{f(\theta)}$ decreasing in θ . The reservation utility $R(\theta)$ is an increasing function of type θ . Let $t(\theta)$ be the compensation and $e = g(q(\theta), p(\theta); \theta)$ be the effort for reaching quota $q(\theta)$ under centralized price $p(\theta)$. The principal-agent problem for the firm under centralization can be formulated as follows, where the superscript L represents continuous type.

$$P_c^L: \max \Pi_c(p(\theta), q(\theta), t(\theta)) = \int_{\underline{\theta}}^{\bar{\theta}} (p(\theta) \times q(\theta) - t(\theta)) f(\theta) d\theta$$

$$(IR) \quad t(\theta) - c(g(q(\theta), p(\theta); \theta)) \geq R(\theta) \text{ for all } \theta \in [\underline{\theta}, \bar{\theta}]$$

$$(IC) \quad t(\theta) - c(g(q(\theta), p(\theta); \theta)) \geq t(\hat{\theta}) - c(g(q(\hat{\theta}), p(\hat{\theta}); \theta))$$

for all $\theta, \hat{\theta} \in [\underline{\theta}, \bar{\theta}]$.

The second constraint in P_c^L can be restated as the decision problem of a type- θ agent i who announces type $\hat{\theta}$ to maximize his profit:

$$\max_{\hat{\theta}} V_i(\hat{\theta}; \theta) = t(\hat{\theta}) - c(g(q(\hat{\theta}), p(\hat{\theta}); \theta))$$

$$(IR) \quad V_i(\hat{\theta}; \theta) \geq R(\theta).$$

Assuming $R''(\theta) < 0$, a pooling region $\theta \in [\theta_1, \theta_2]$ ($\theta_1 \leq \theta_2$) exists with the optimal contract under centralization for the above principal-agent problem

(Lemma 5 in Lewis and Sappington 1989 and Proposition 3 in Maggi and Rodriguez-Clare 1995). With the existence of a pooling region, we now compare delegated pooling with centralized pooling. The firm's problem with delegated pooling contract $t(s,p(\theta))$ can be formulated as follows.

$$\mathbf{P}_d^L : \max \Pi_d(t(s,p(\theta))) = \int^{\bar{\theta}}$$

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Notes

¹This assumption is relaxed in an extension in which a correlation exists across the sales territories (section 5.2).

²The deterministic market potential assumption is relaxed in the extension (section 5.1), where we analyze the influence of the demand uncertainty. The main results are shown to be qualitatively unchanged. We thank the Senior Editor and Reviewers for suggesting this direction of extension.

³The base model of two agent types is extended to the continuous type in section 5.3.

⁴In the case of a centralized system, the firm determines the price and the effort that type- i agent should exert to maximize $p(s_0 + \theta_i e - bp) - e^2/2$. To ensure the interior solution, we need $2b > \theta_i^2$ to have the negative definite Hessian matrix of the objective function. Then, the optimal price and effort are expressed as $p = s_0/(2b - \theta_i^2)$ and $e = (s_0 \theta_i)/(2b - \theta_i^2)$, respectively. With the optimal price and effort, the maximum total profit under the centralized system is $s_0^2/[2(2b - \theta_i^2)]$, and the firm's maximum net profit is $s_0^2/[2(2b - \theta_i^2)] - R_i$. Hence, a sufficiently large s_0 can guarantee that the firm's profit is nonnegative.

⁵Laffont and Martimort (2001) called this moral hazard "false moral hazard" in page 274 because the agent does not have the freedom to choose his effort.

⁶Proposition 5 in Rao (1990), indicates that a necessary and sufficient condition for the optimal contracts and a menu of linear plans to be equivalent is the convexity of the optimal contracts in sales.

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